



School of Business,  
Economics and Law  
GÖTEBORG UNIVERSITY

# Monopoly

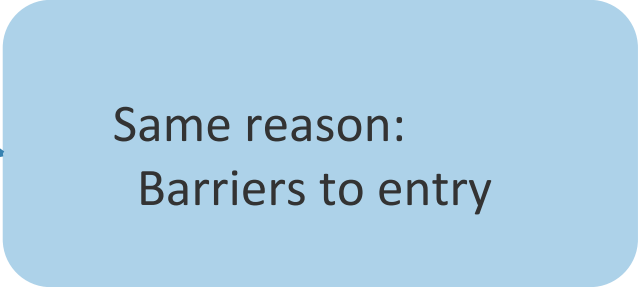
Johan Stennek

# Monopoly

- Q: Examples of monopoly?
  - SJ on the route Stockholm – Linköping?
  - Pharmaceutical companies with patent?
  - District heating?
  - Hemnet?

# Monopoly

- Q: How do you define monopoly?
- Definition – supply side
  - One firm producing the product
  - No close substitutes
  - Barriers to entry
- Definition – demand side
  - Many “small” buyers (consumers, small firms)
- Implication: Firm can set price without thinking about
  - Other firms (existing or not)
  - Individual consumers



Same reason:  
Barriers to entry

# Barriers to entry

- Q: Examples of entry barriers?
- Legal
  - Patents to protect R&D: pharmaceuticals (substitutes?)
  - Copy rights: Books (substitutes?)
  - Consumption control: liquor
  - Fiscal: gambling
- Economies of scale / market size
  - District heating in cities
  - Food retailing in rural areas
  - Telecom networks
- Exclusive access to essential resource
  - Natural resource
  - Exclusive distribution agreement
- Network effects
  - Hemnet

# Q: Why study monopoly?

- Still some important monopolies
  - Pharmaceuticals, district heating, ...
- Policy evaluations
  - competition policy: ban on exclusion + merger control
  - press subsidies
  - deregulation
- Preparation for studying competing firms

# Examples

- Pharmaceuticals
  - Huge costs for R&D
  - Patents for 20 years => Monopoly
- Striking stylized fact
  - Prices for the same drug differ hugely between countries

# Examples

- Lipitor
  - Reduces cholesterol
  - Manufacturer prices per dosage in 1998 (10 mg tablets)
    - US: \$ 1.46
    - Sweden: \$ 0.94
- Losec
  - Ulcer treatment
  - Manufacturer prices per dosage in 1998 (20 mg tablets)
    - US: \$ 2.99
    - Sweden: \$ 1.74

# Examples

**Average percentage deviation from European mean prices for 90 pharmaceutical products in 1998**

<i>Country</i>	<i>Deviation</i>
Greece	-28
Spain	-20
Portugal	-13
Italy	-13
France	-10
Finland	-2
Austria	-2
Norway	-1
Sweden	-1
Belgium	-1
Netherlands	+2
Denmark	+3
Germany	+11
United Kingdom	+19
Switzerland	+25



# Examples

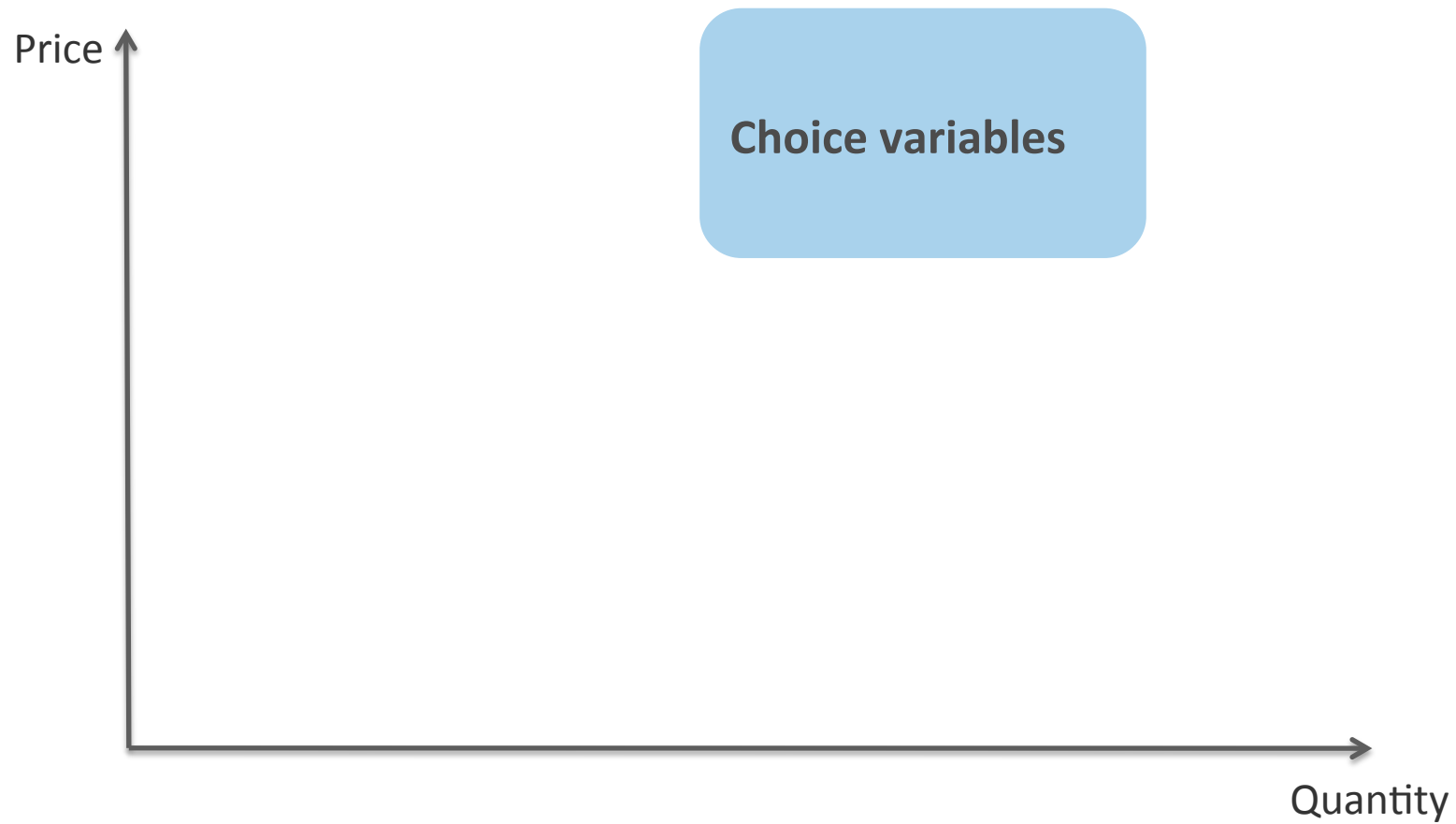
- Questions
  - Why are prices for the same good different in different geographical markets?
  - Why do prices differ from costs (= similar in all countries)?
  - Is this pattern good or bad?

# The monopoly model

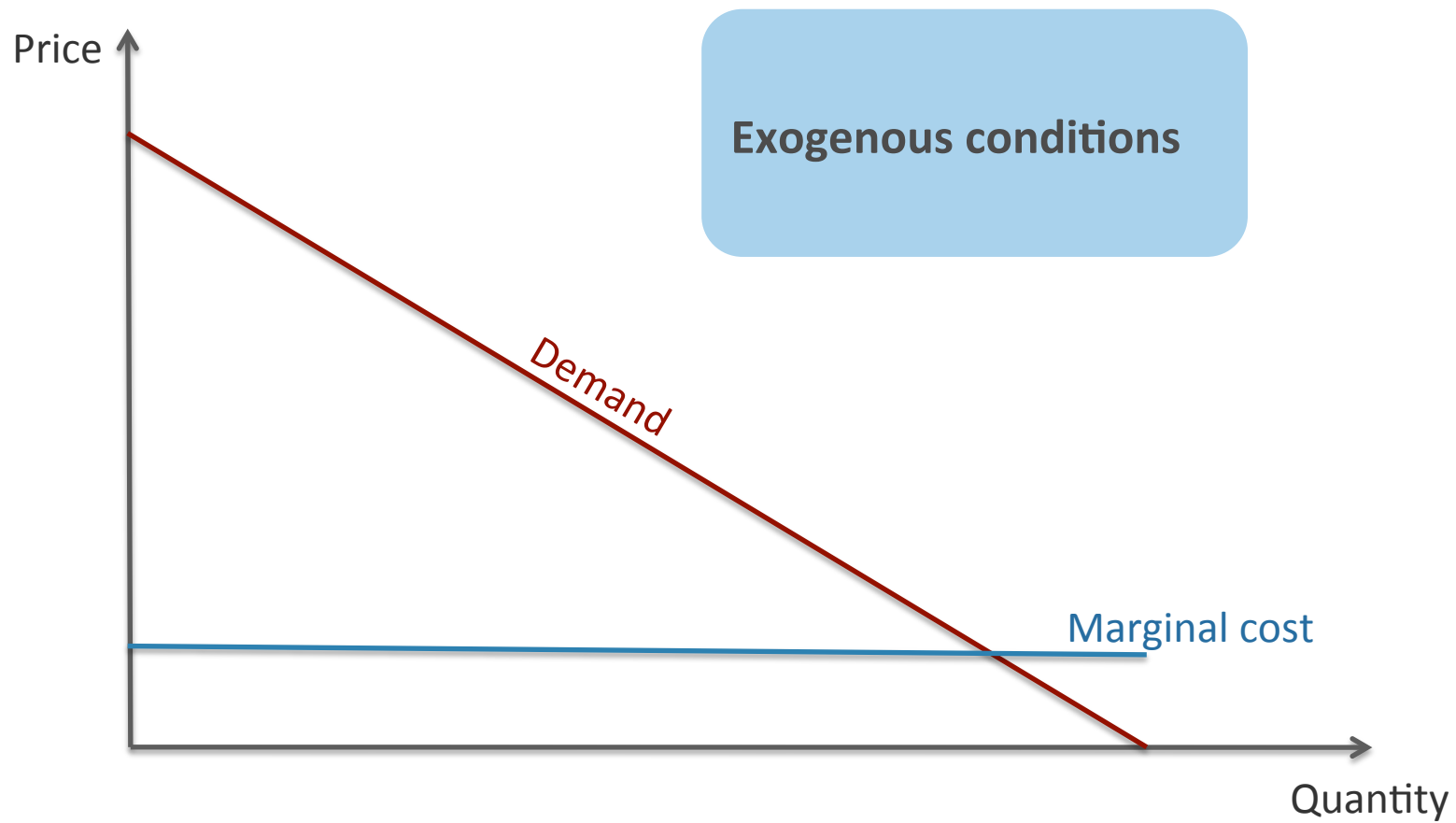
# Monopoly model

- Behavioral assumption
  - Firm wants to maximize profits
- Choice
  - Price
  - Quantity
- Exogenous conditions
  - Demand function  $[P(q) \text{ or } Q(p)]$
  - Cost function  $[C(q)]$

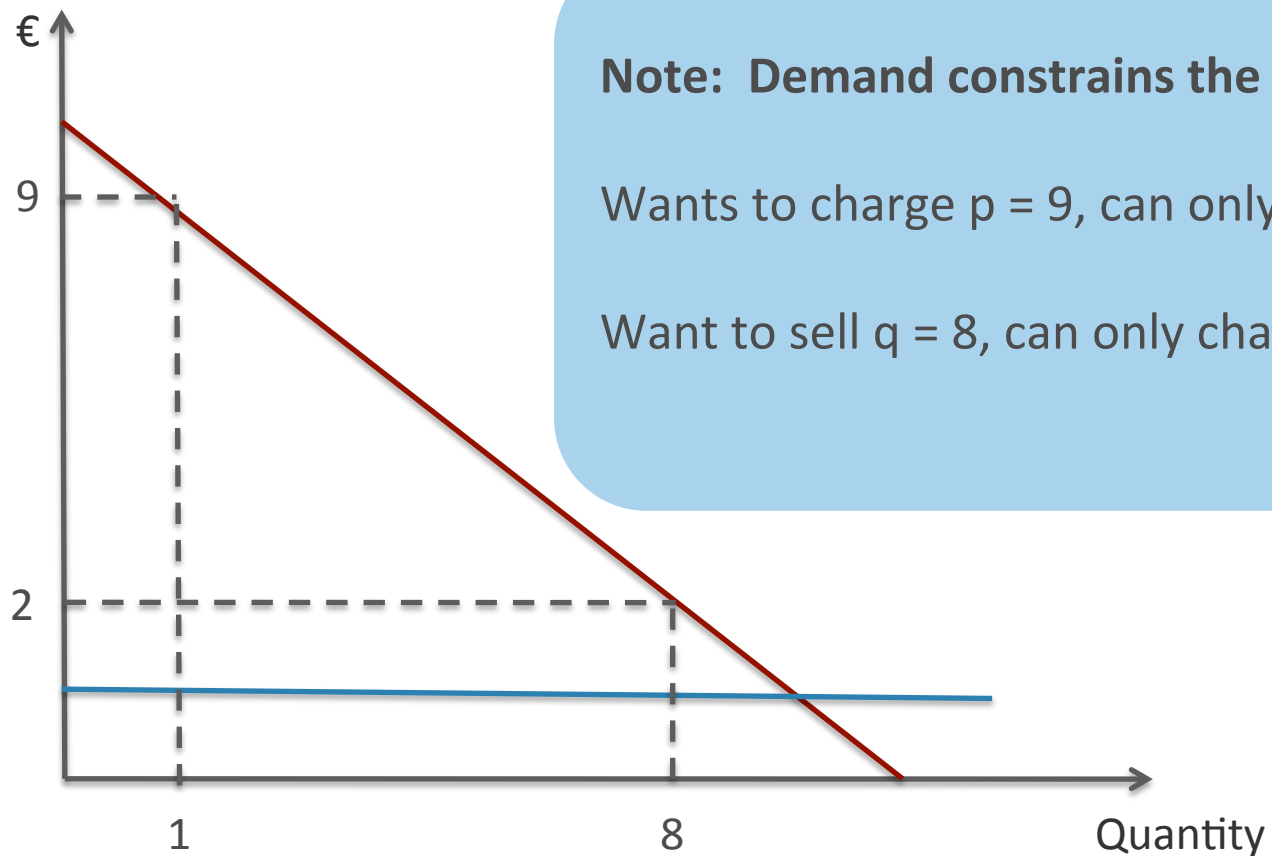
# Monopoly model



# Monopoly model



# Monopoly model

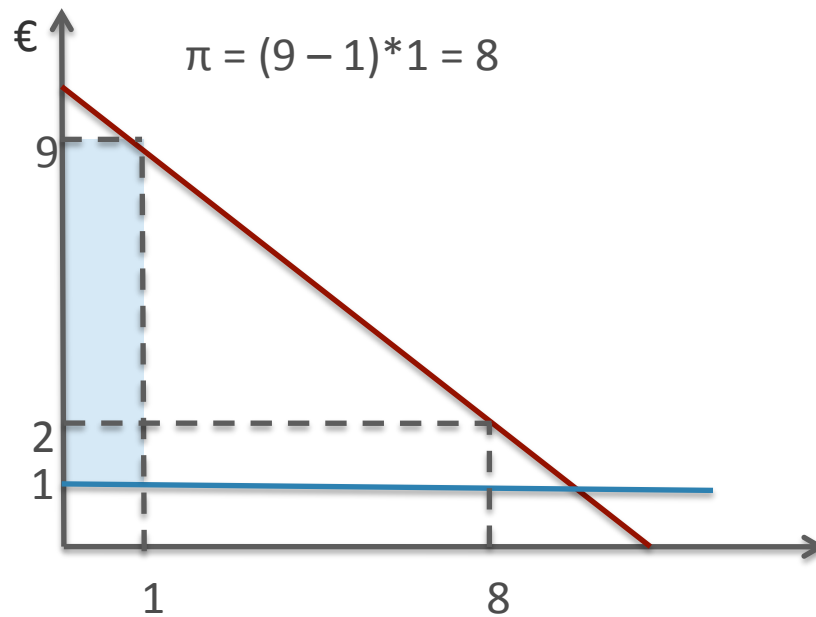


**Note: Demand constrains the monopolist**

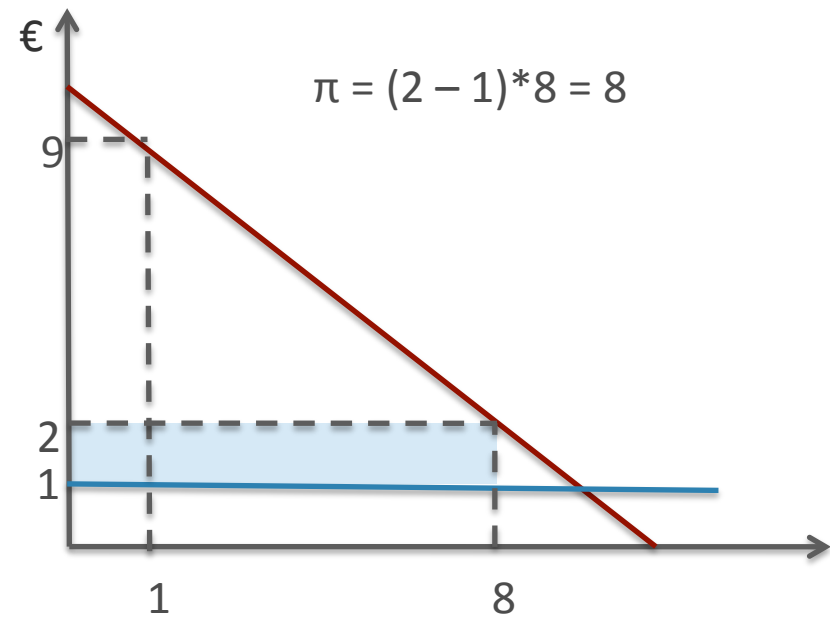
Wants to charge  $p = 9$ , can only sell  $q = 1$

Want to sell  $q = 8$ , can only charge  $p = 2$

# Monopoly model



Very high margin:  $8 = 9 - 1$   
Very low sales: 1  
=> low profit: 8



Very low margin:  $1 = 2 - 1$   
Very high sales: 8  
=> low profit: 8

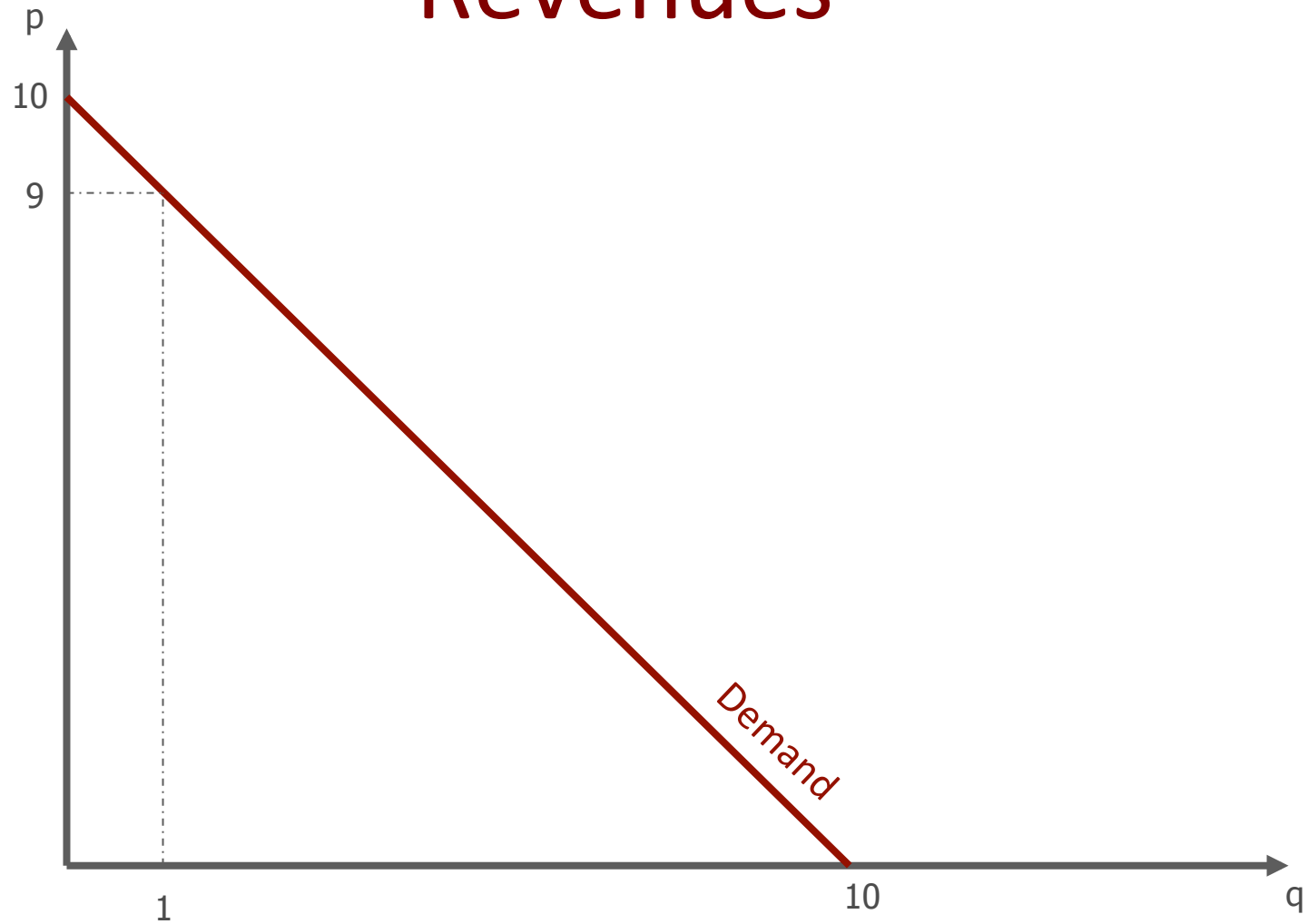
# Monopoly model

- Demand constrains the monopolists behavior
  - Trade-off between margin and sales
  - Need to strike a balance
- Now let's try to find this balance
  - Profit = Revenues - Cost
  - Need to study how revenues depend on sales

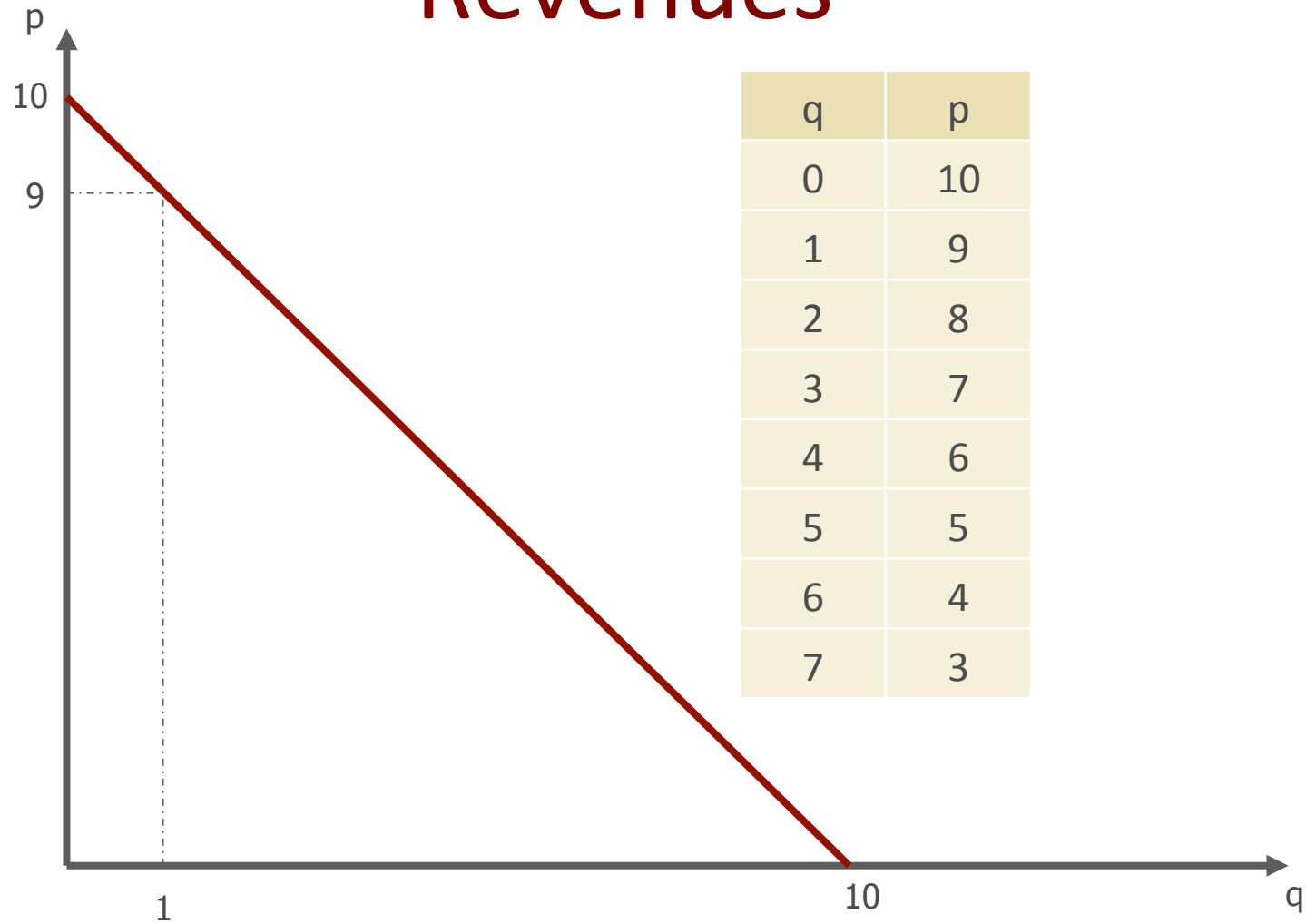


How do revenues depend on sales?

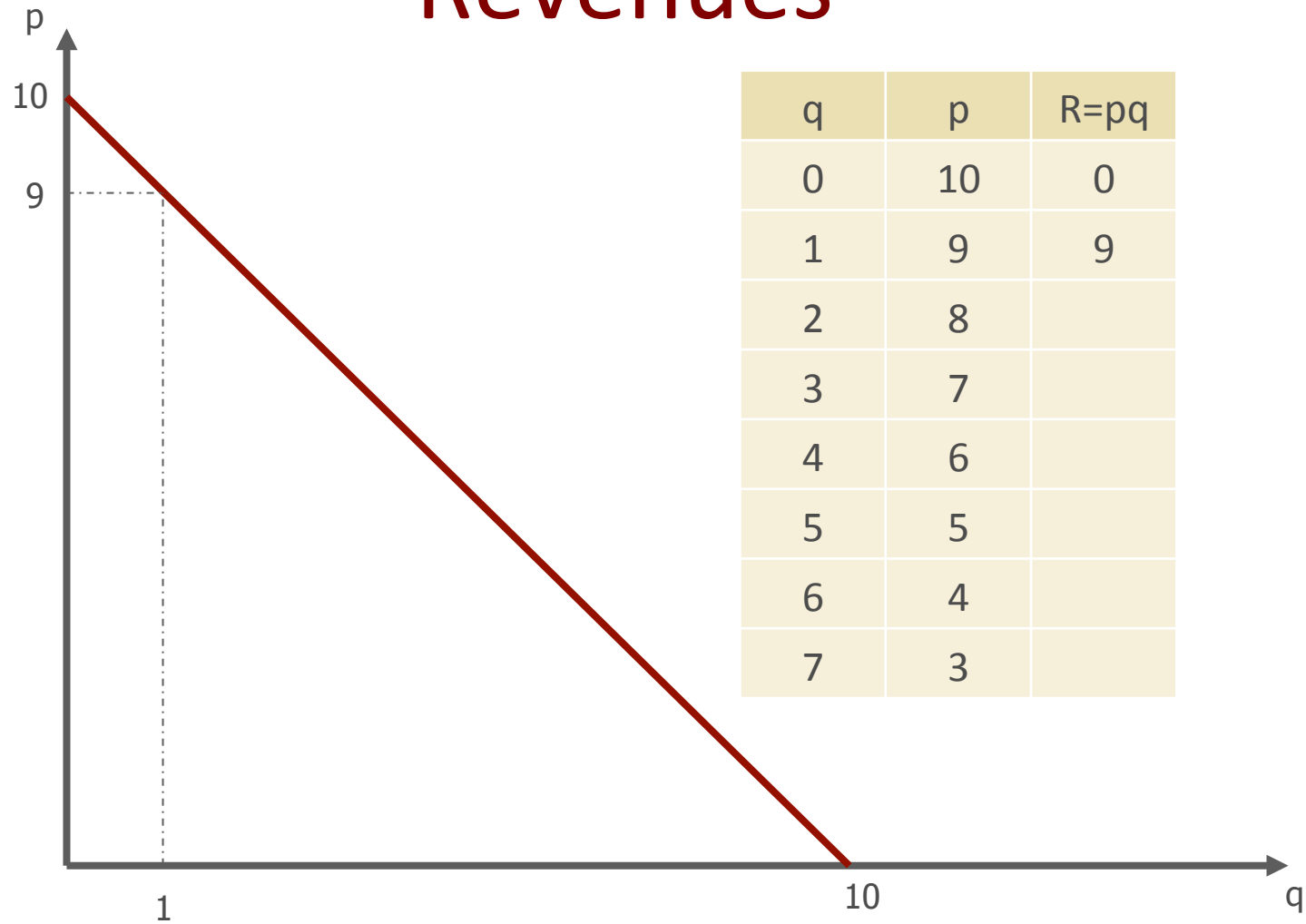
# Revenues



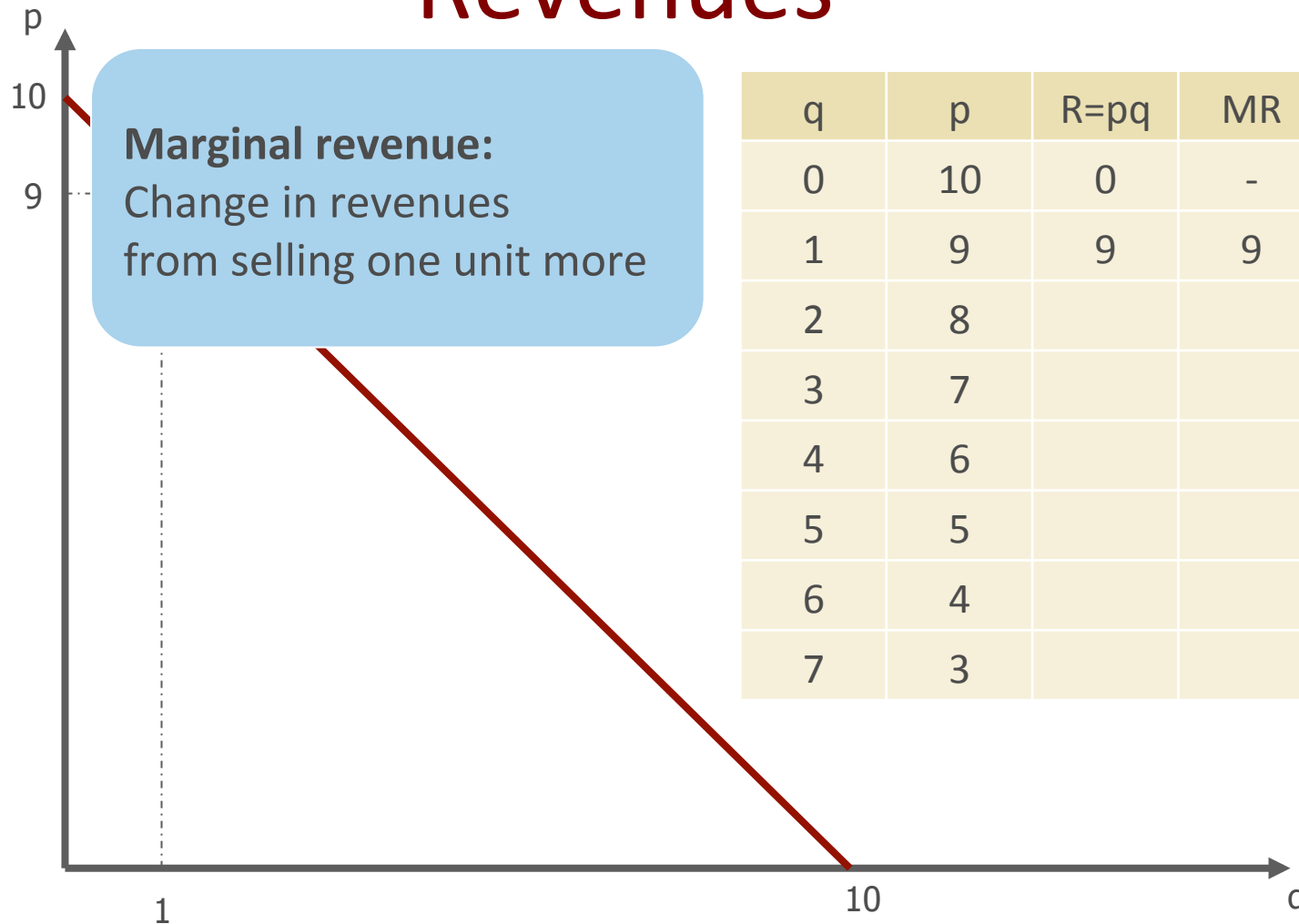
# Revenues



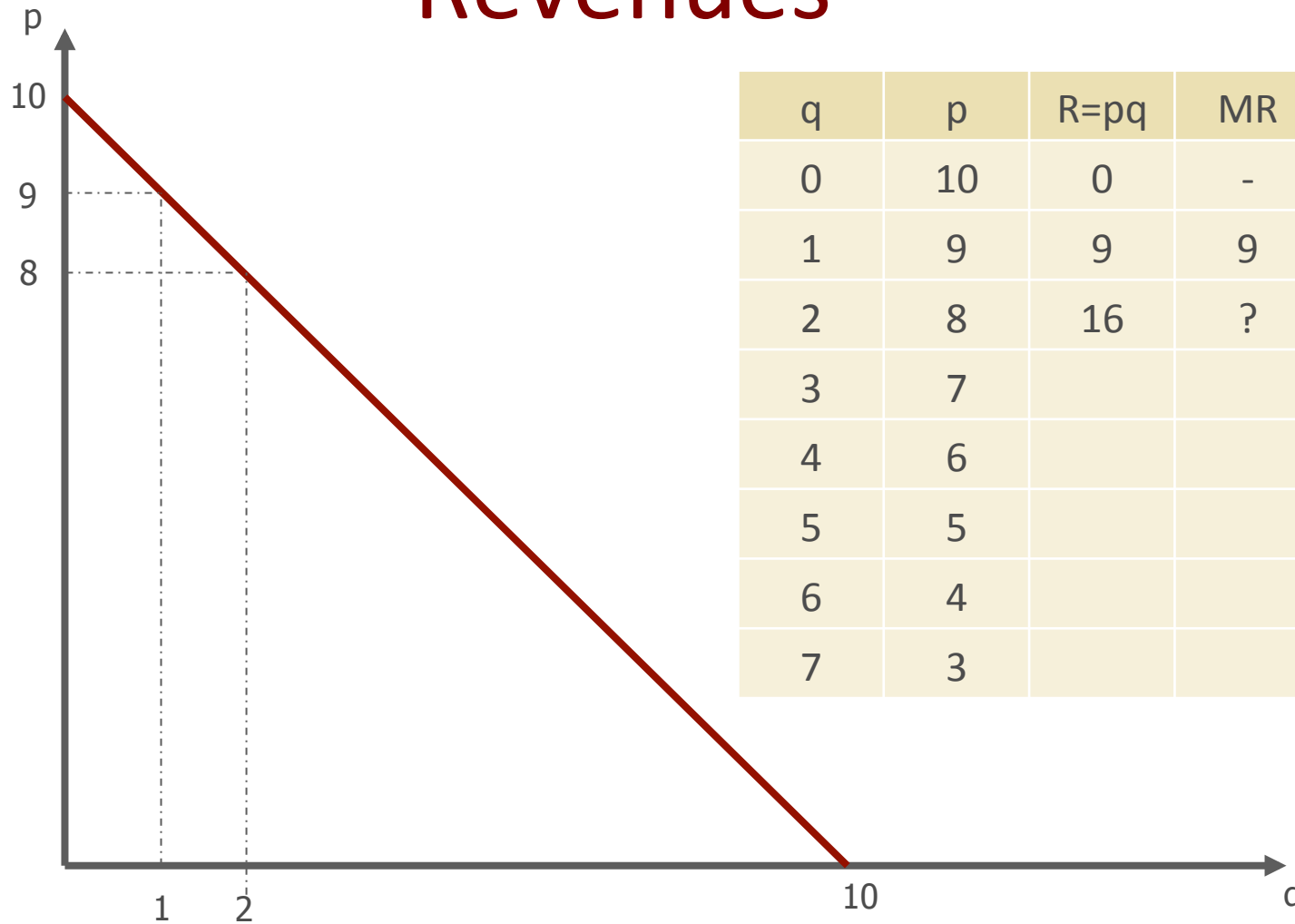
# Revenues



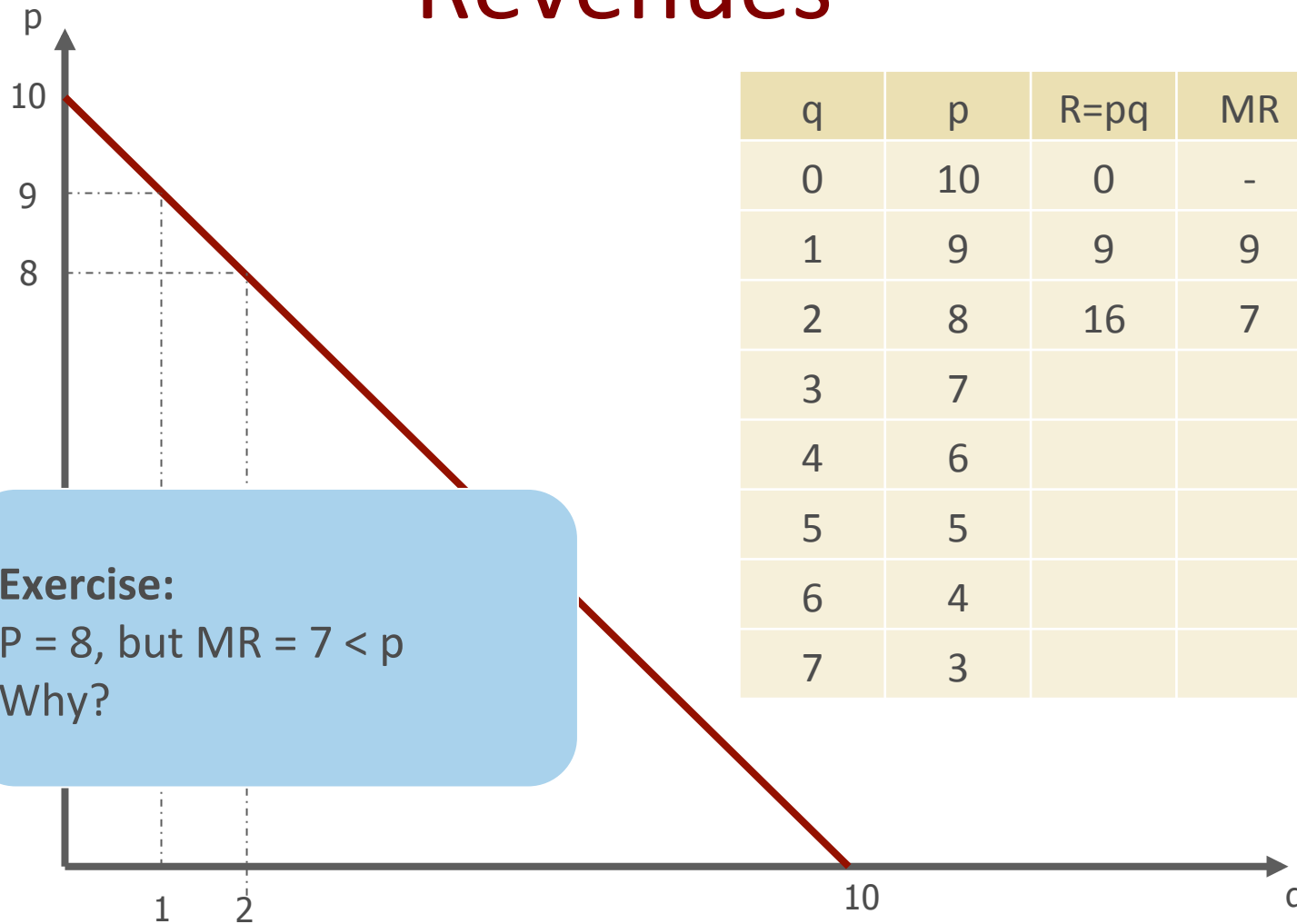
# Revenues



# Revenues

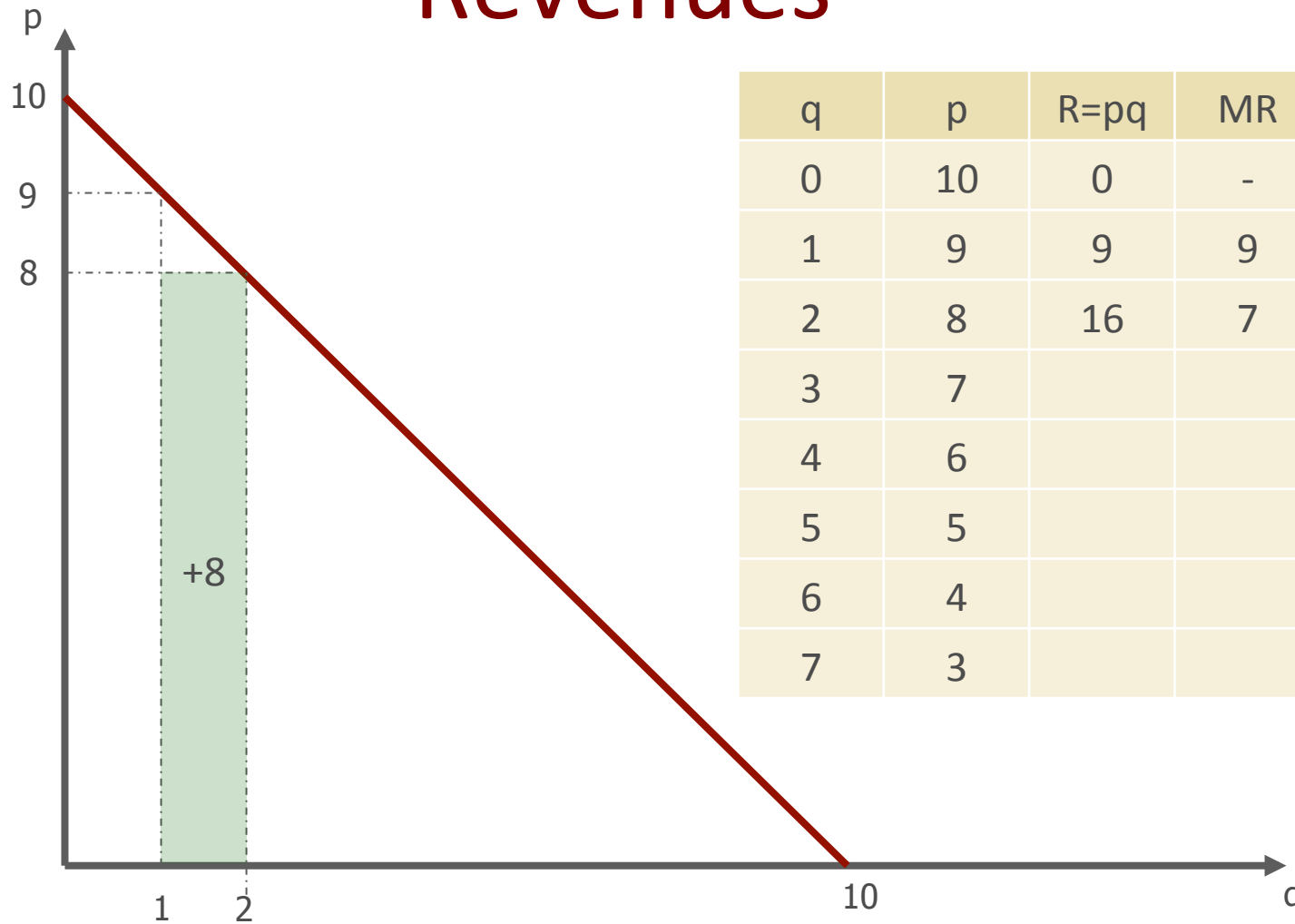


# Revenues



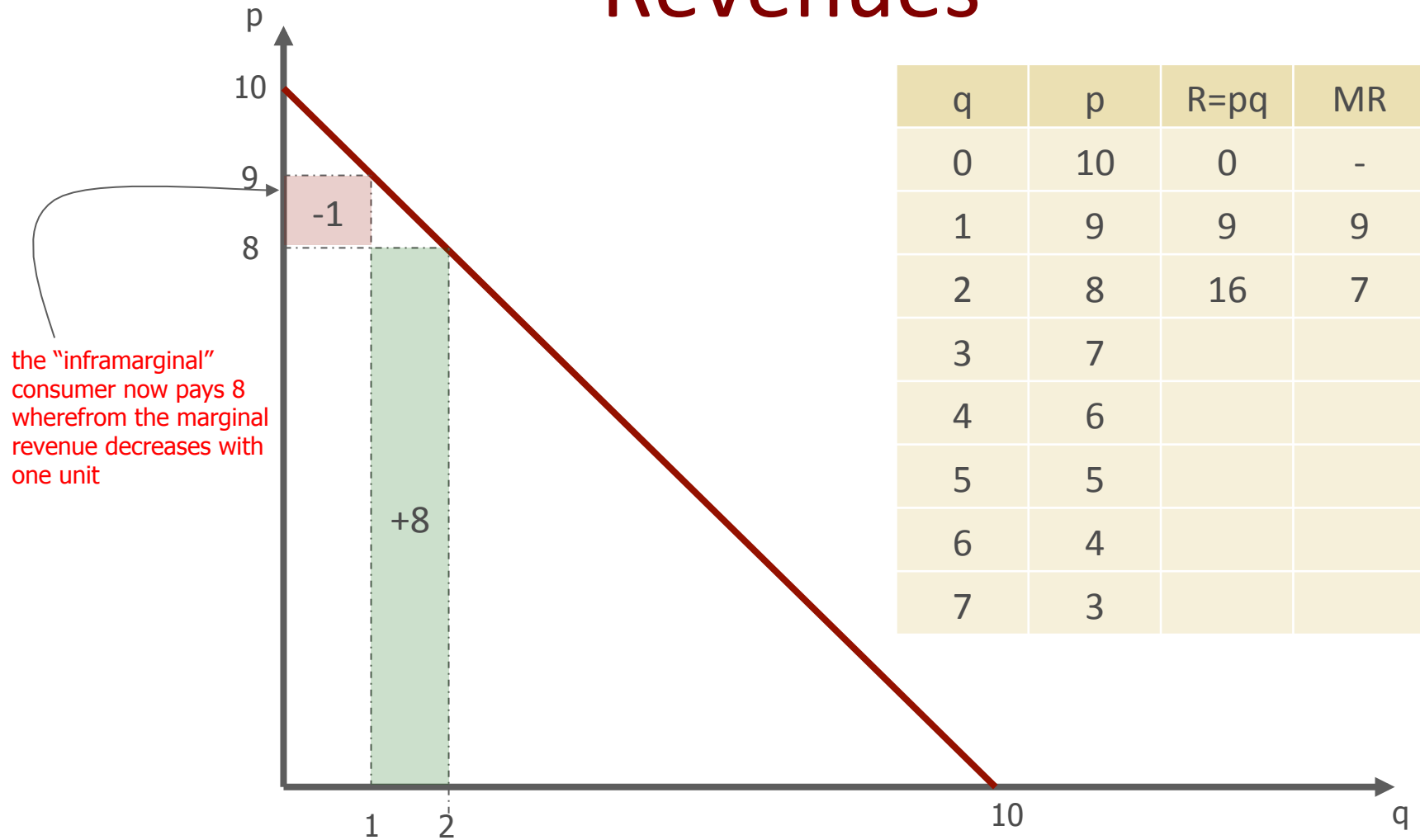
q	p	R=pq	MR
0	10	0	-
1	9	9	9
2	8	16	7
3	7		
4	6		
5	5		
6	4		
7	3		

# Revenues

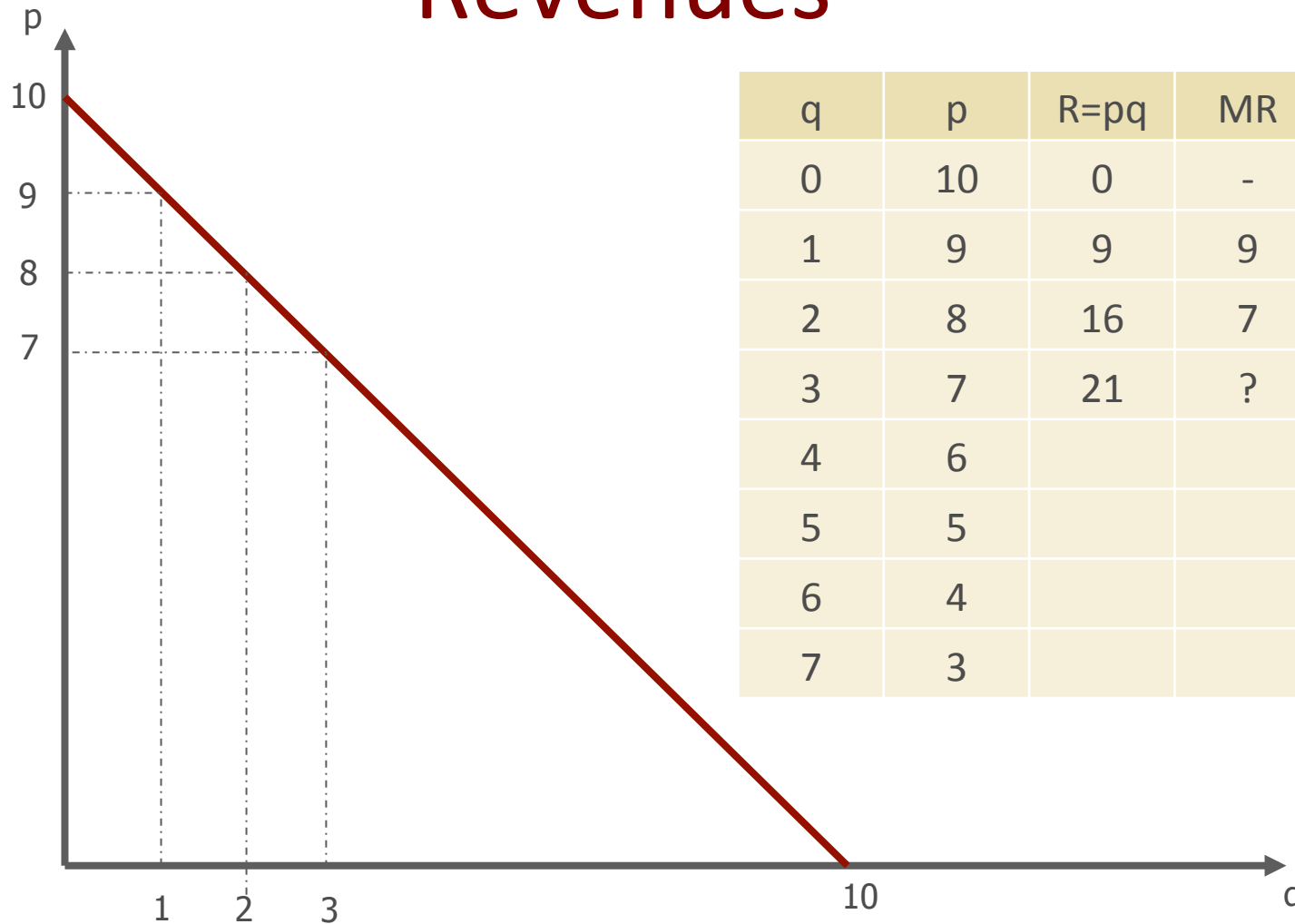




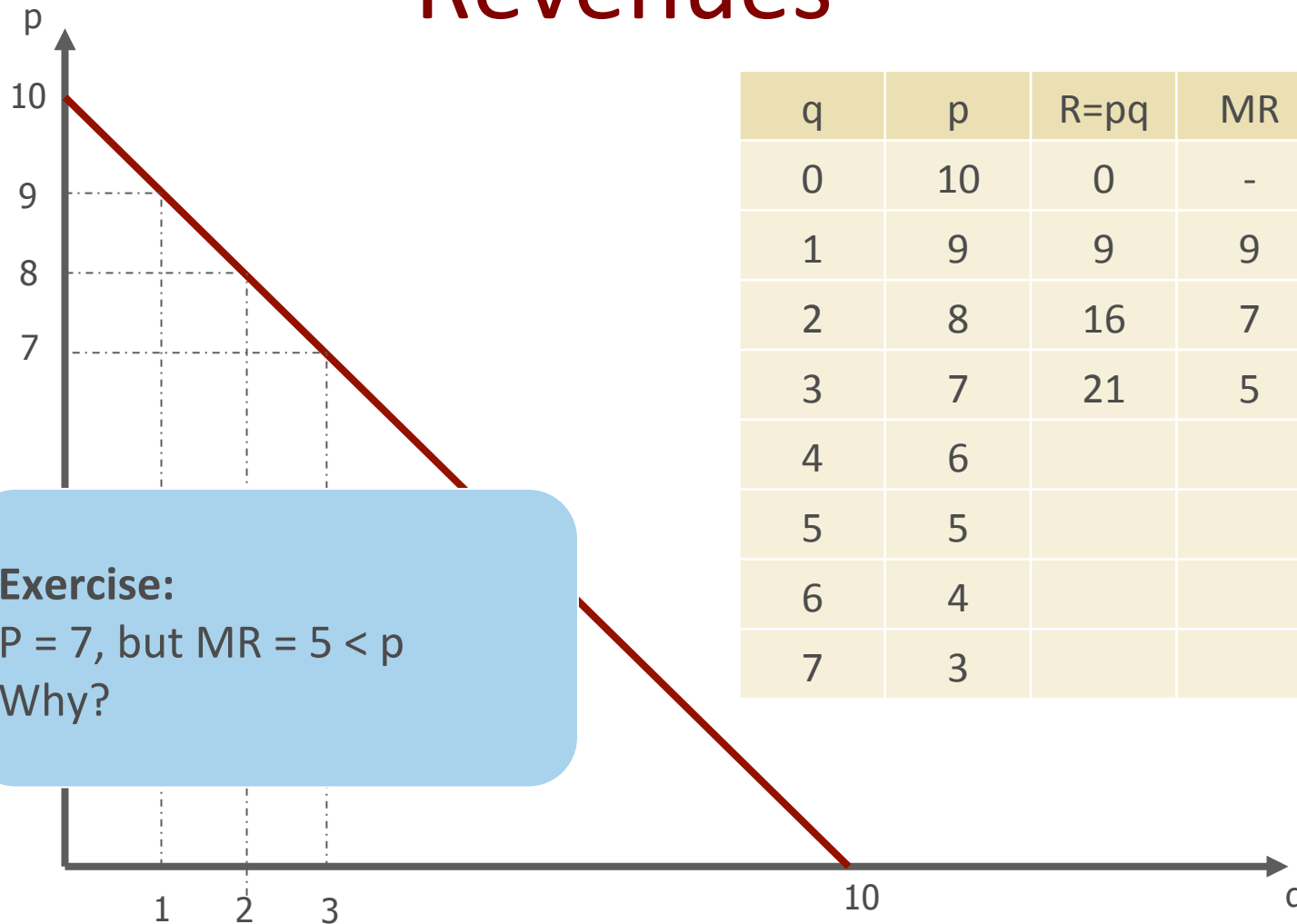
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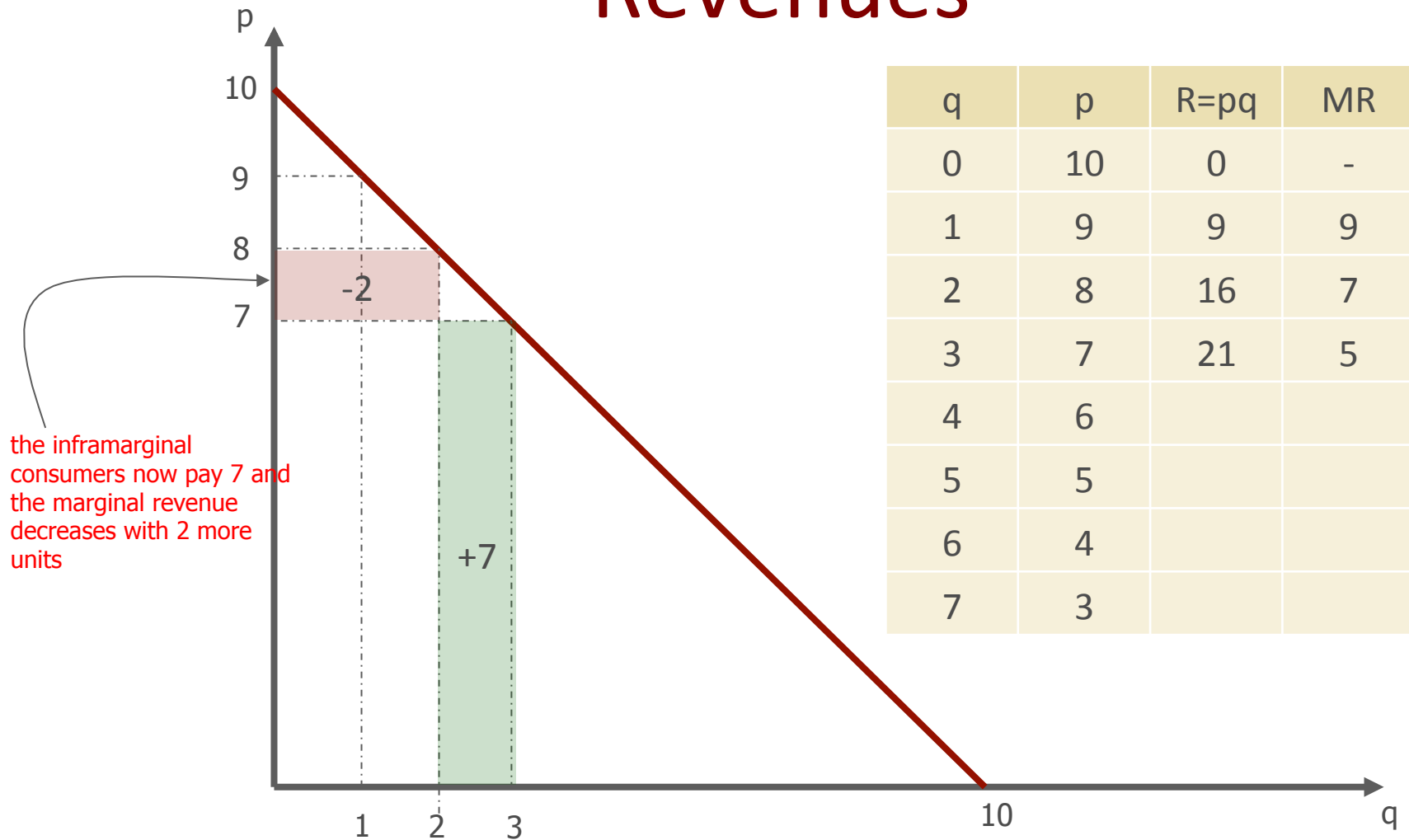
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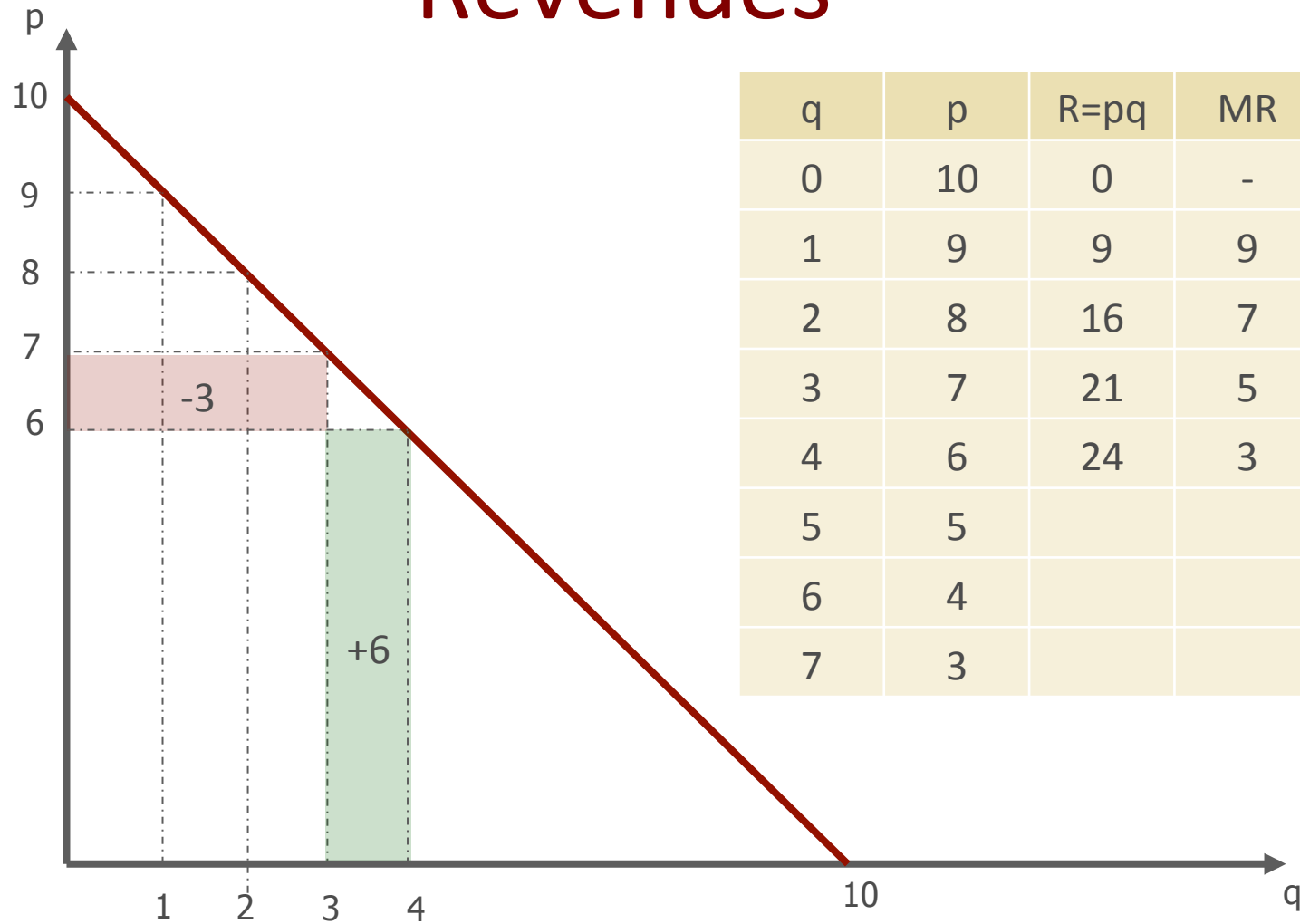
# Revenues



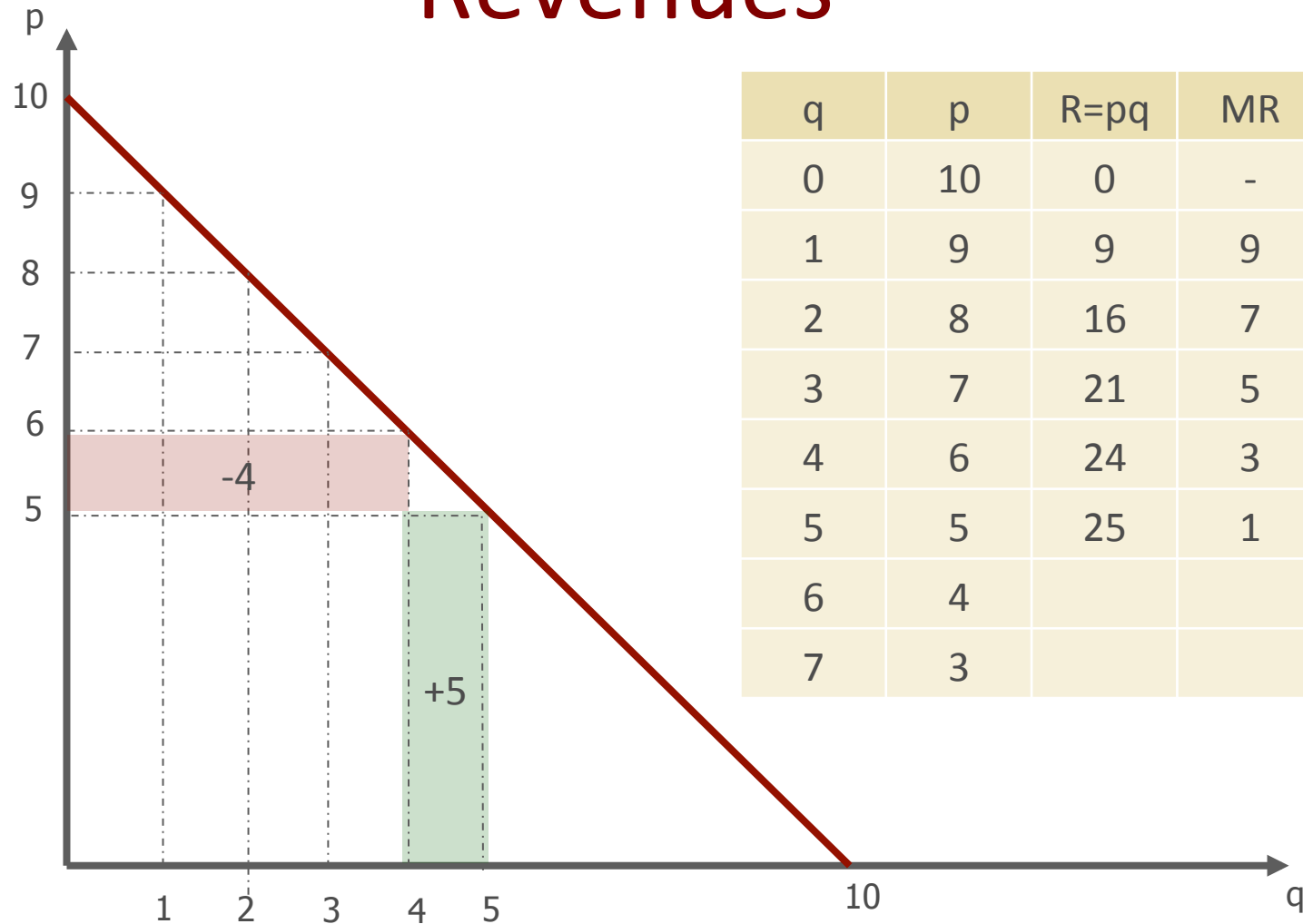
# Revenues



# Revenues



# Revenues



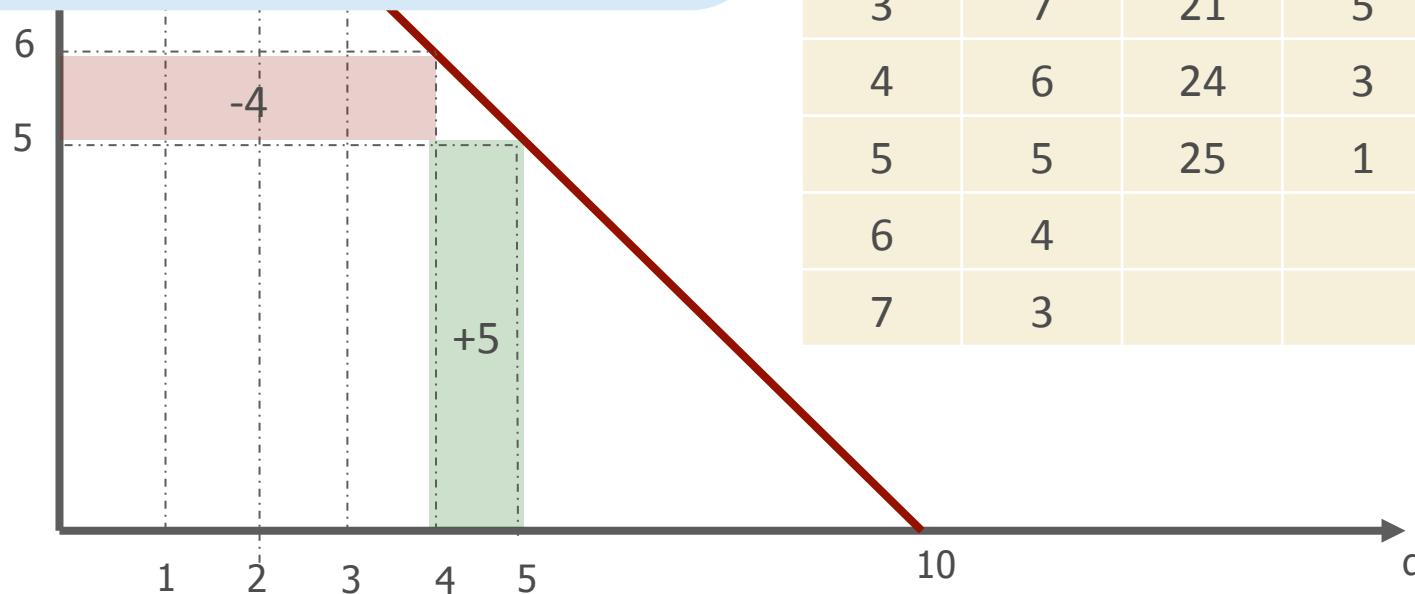
# Revenues

The more I sell, the more costly it is to lower price by €1

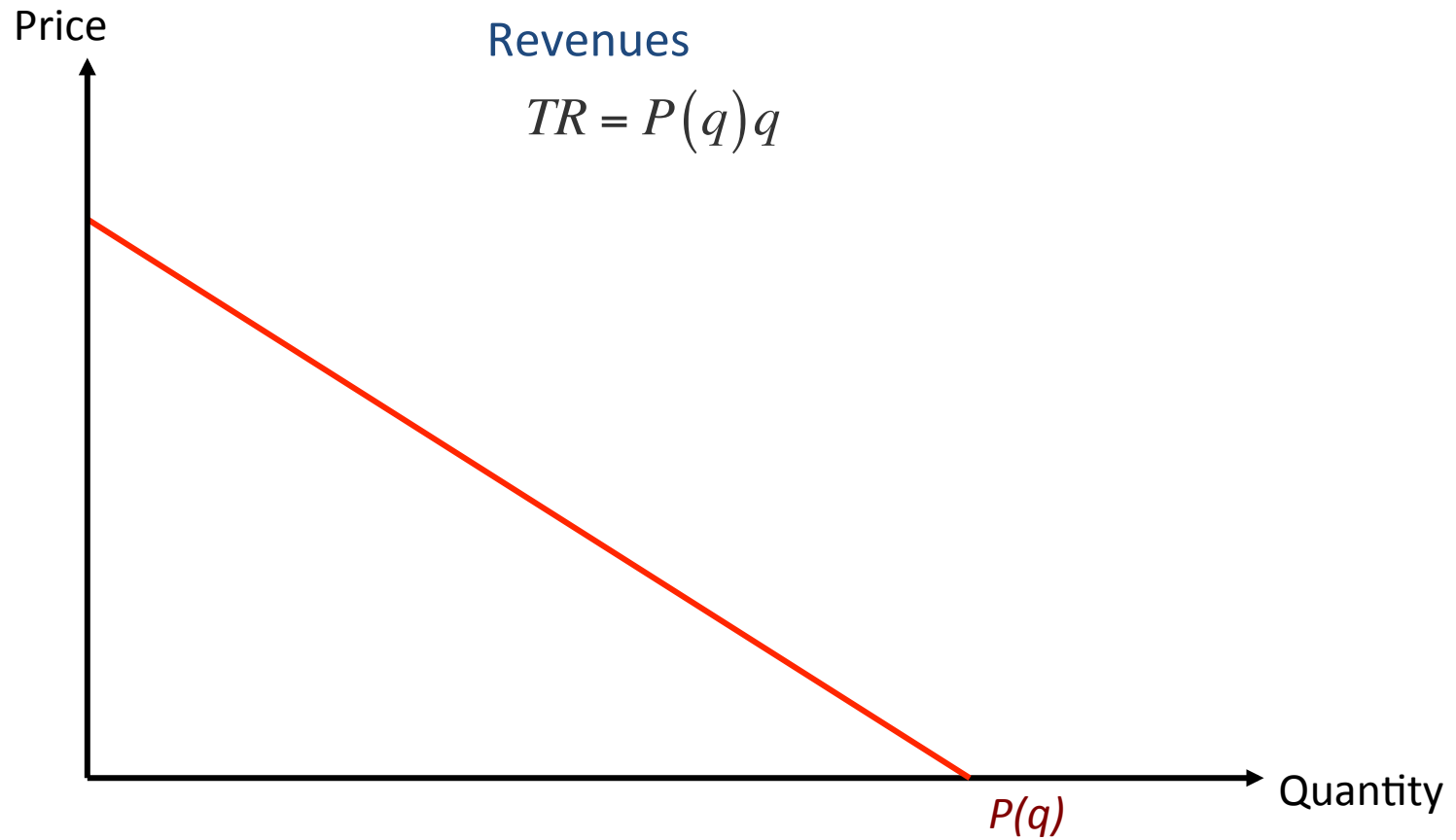
=>

MR is falling (normally)

q	p	R=pq	MR
0	10	0	-
1	9	9	9
2	8	16	7
3	7	21	5
4	6	24	3
5	5	25	1
6	4		
7	3		

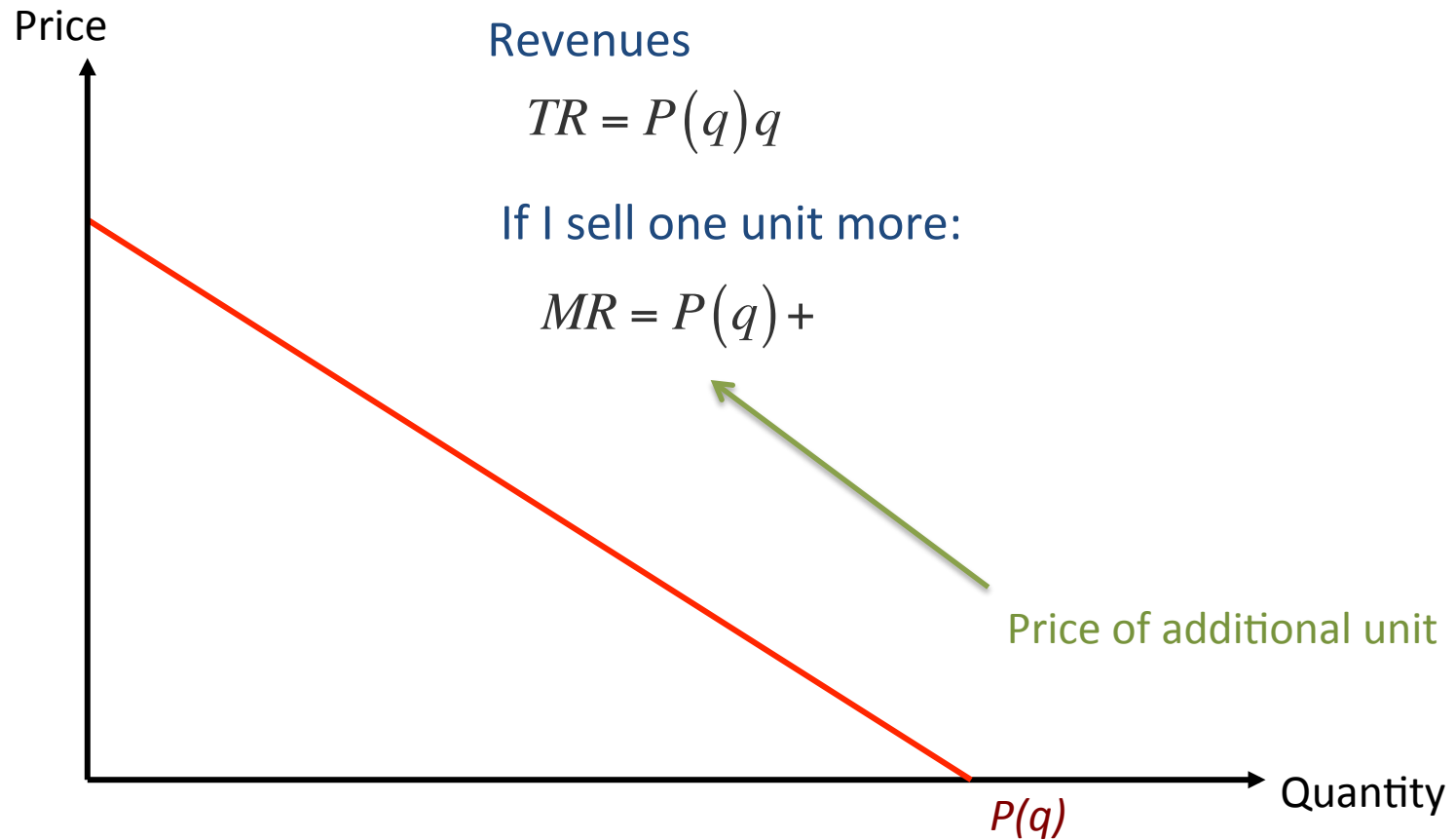


# Revenues

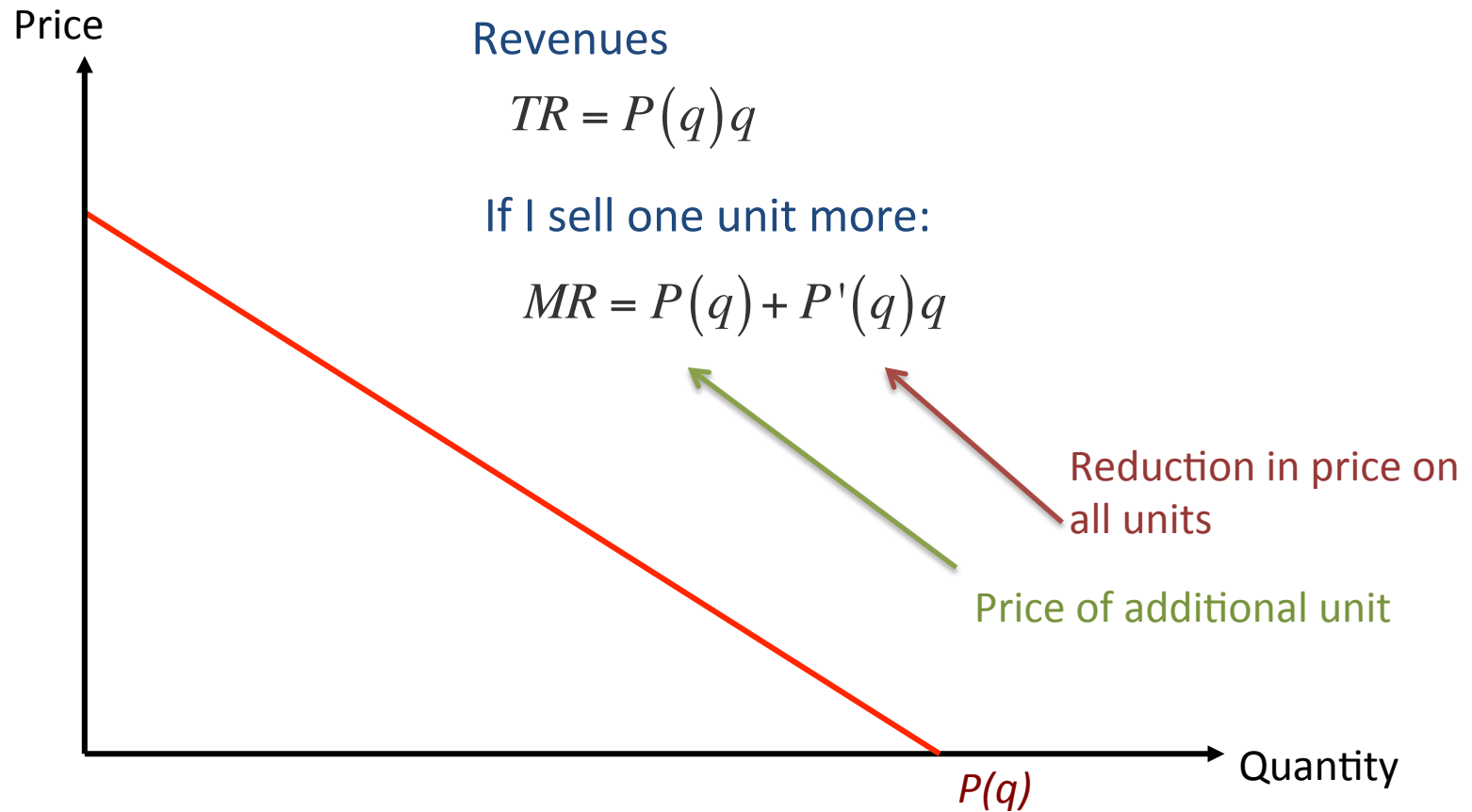




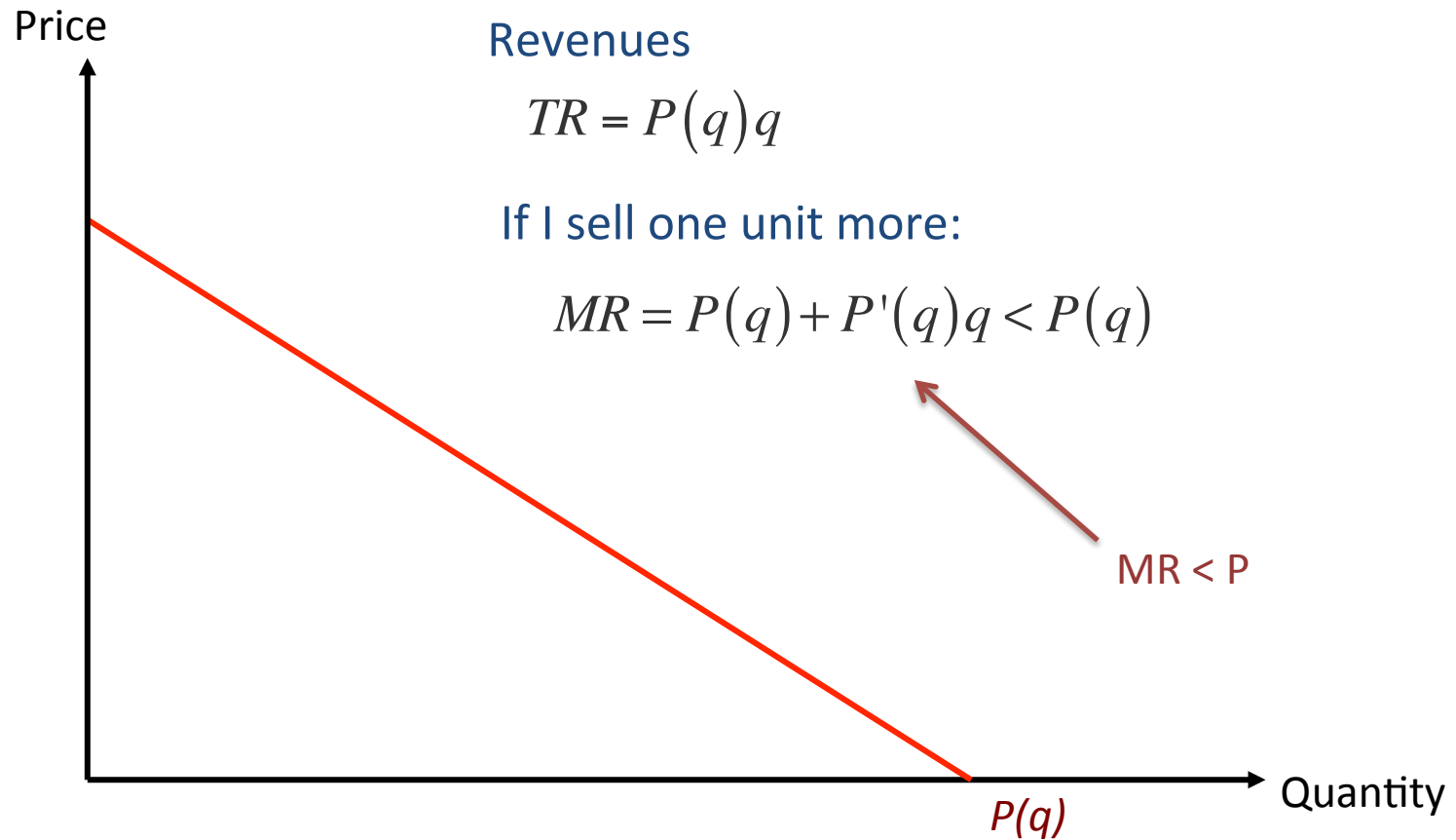
# Revenues



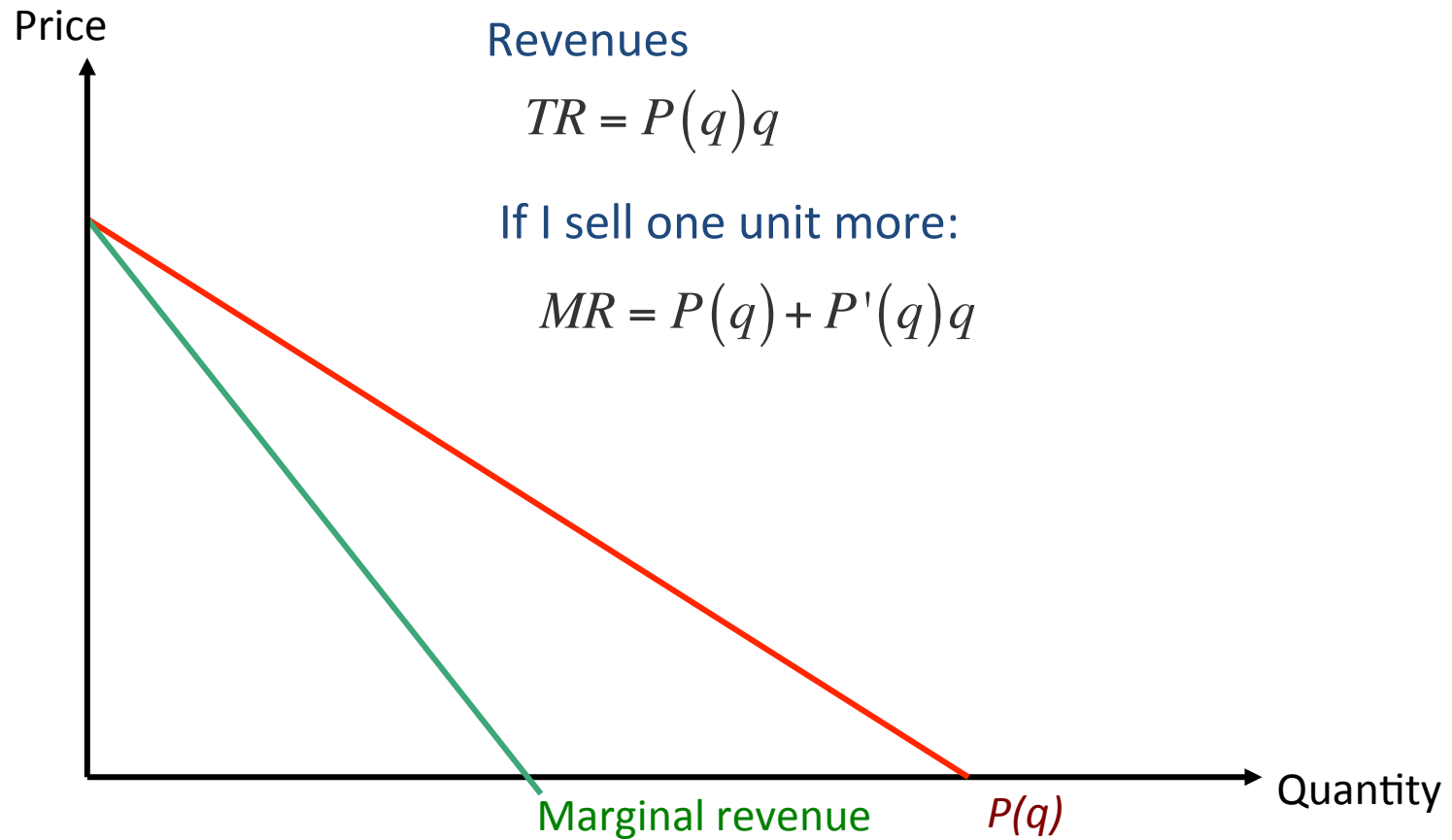
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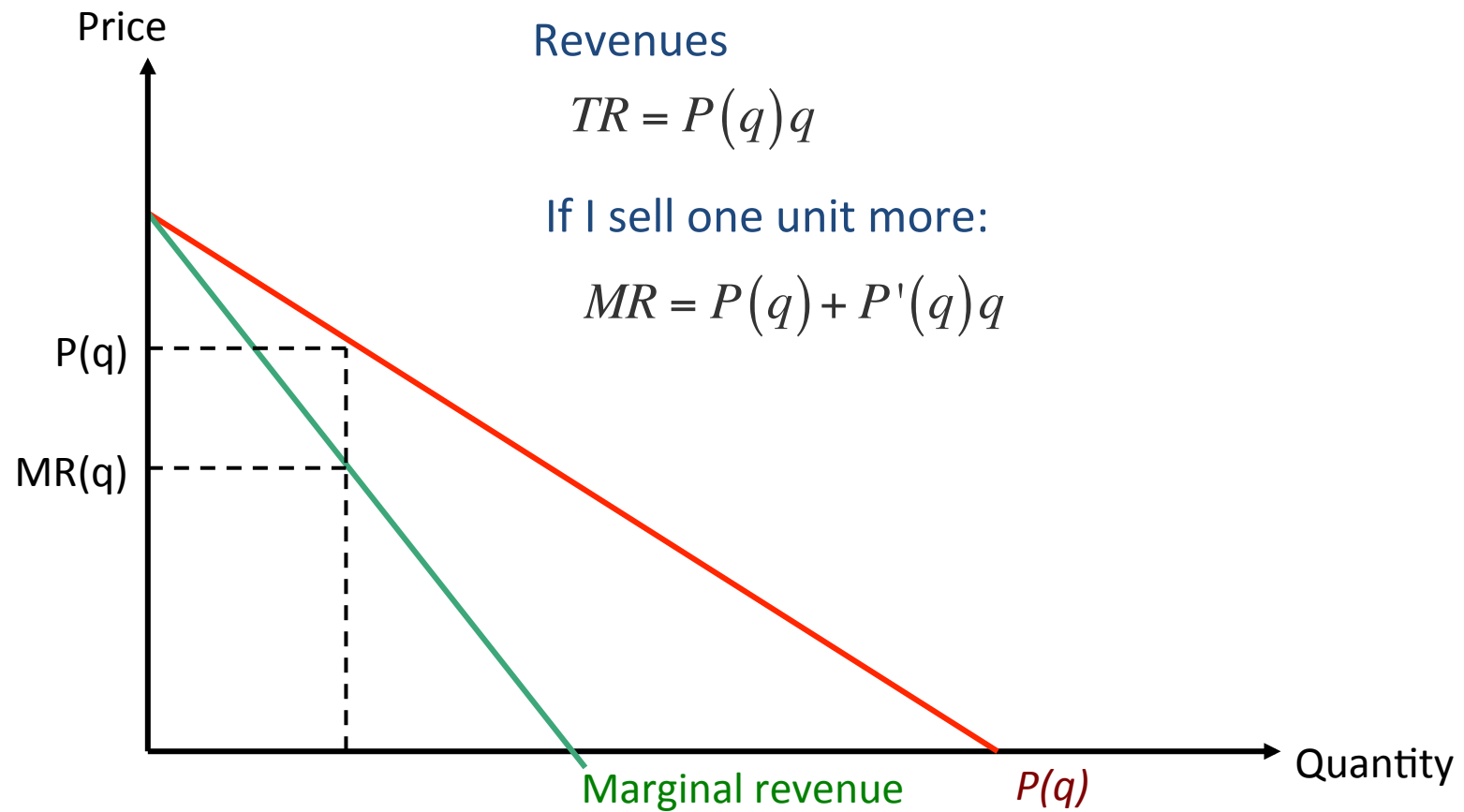
# Revenues



# Revenues



# Revenues



# Monopolist's choice of quantity

# Choice of quantity

- Exercise: Set up monopoly problem and solve for optimal quantity!
  - Cost function:  $C(q)$
  - Inverse demand:  $P(q)$

# Choice of quantity

Profit

$$\pi(q) = P(q) \cdot q - C(q)$$



# Choice of quantity

Profit

$$\pi(q) = P(q) \cdot q - C(q)$$

First order condition

$$\pi_q(q) = P(q) + P_q(q) \cdot q - C_q(q) = 0$$

# Choice of quantity

Profit

$$\pi(q) = P(q) \cdot q - C(q)$$

First order condition

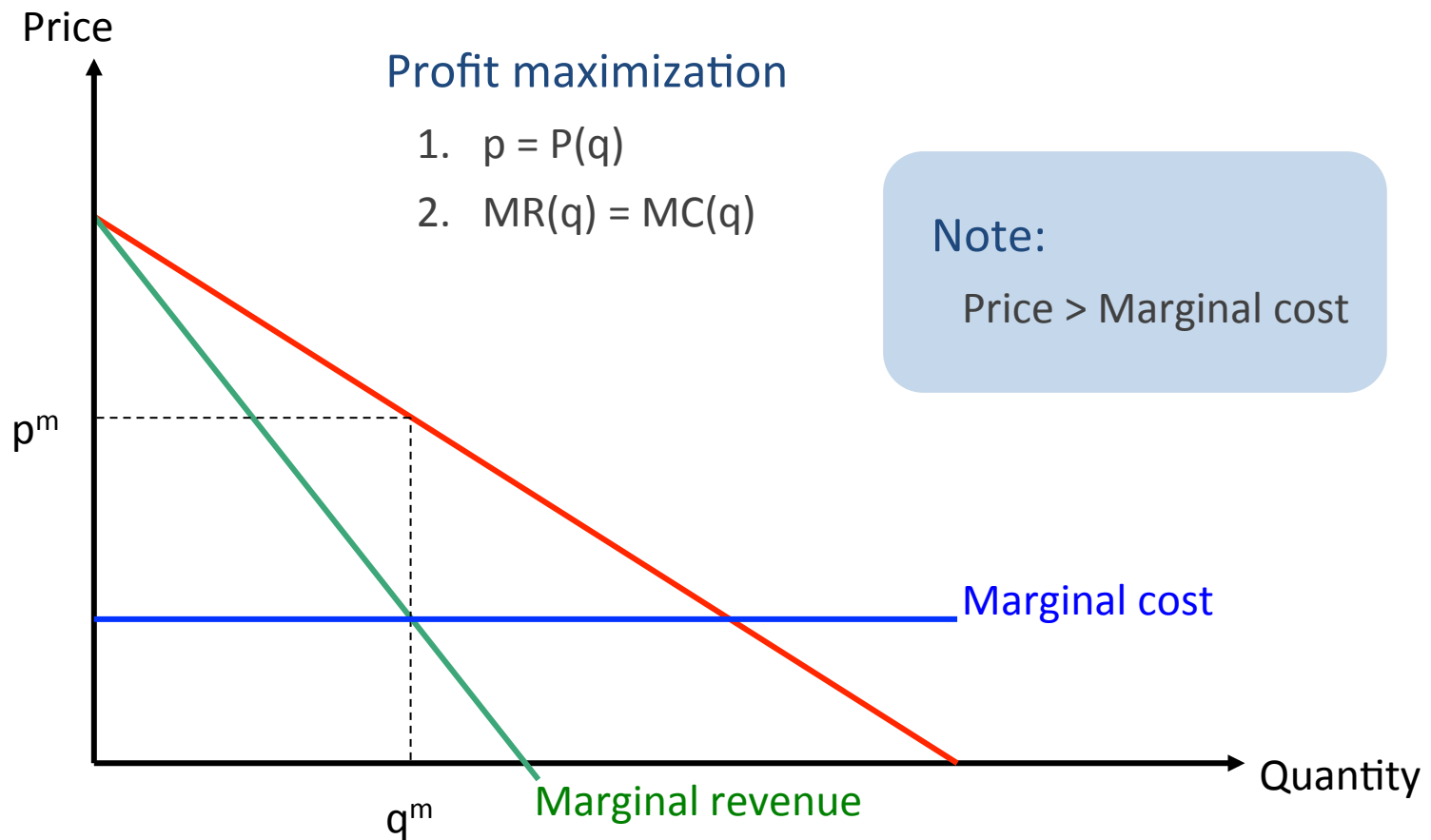
$$\pi_q(q) = P(q) + P_q(q) \cdot q - C_q(q) = 0$$

Rewrite

$$P(q) + P_q(q) \cdot q = C_q(q)$$

Interpretation?

# Choice of quantity



# Monopoly

- Definition

- A firm has *market power* if it can set a price above marginal cost, without losing all sales

# Choice of quantity

First order condition

$$\pi_q(q) = P(q) + P_q(q) \cdot q - C_q(q) = 0$$

Second order condition

$$\pi_{qq}(q) = 2 \cdot P_q(q) + P_{qq}(q) \cdot q - C_{qq}(q) < 0$$

Example:

Marginal cost constant or increasing  $\Leftrightarrow C_{qq} \geq 0$

Demand linear or concave  $\Leftrightarrow P_{qq} \leq 0$

# Choice of quantity

- Exercise: Set up monopoly problem and solve for optimal quantity and price!

- Constant unit cost:  $c$

- Linear inverse demand:  $p = a - b \cdot q$

(No need to check 2<sup>nd</sup> order condition)

# Choice of quantity

Profit

$$\pi(q) = P(q) \cdot q - C(q) = [a - b \cdot q] \cdot q - c \cdot q$$

First order condition

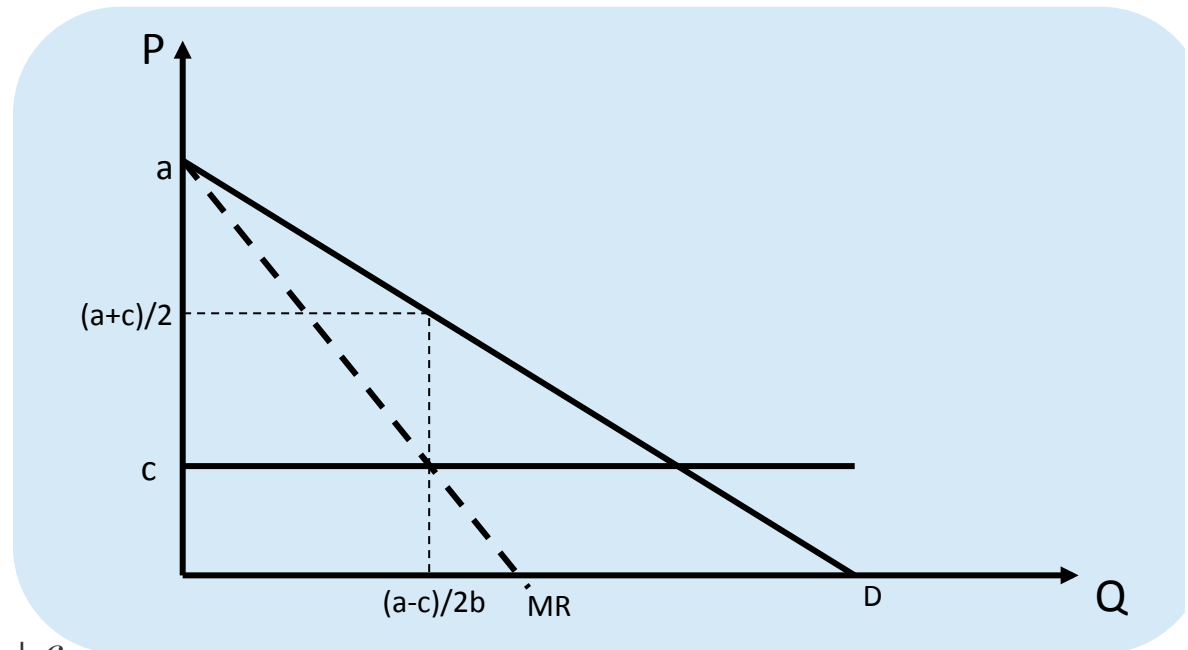
$$\pi_q(q) = [a - b \cdot q] - b \cdot q - c = 0$$

Solve for q

$$q = \frac{a - c}{2 \cdot b}$$

Find p

$$P(q) = a - b \cdot q = a - b \cdot \left[ \frac{a - c}{2 \cdot b} \right] = \frac{a + c}{2}$$

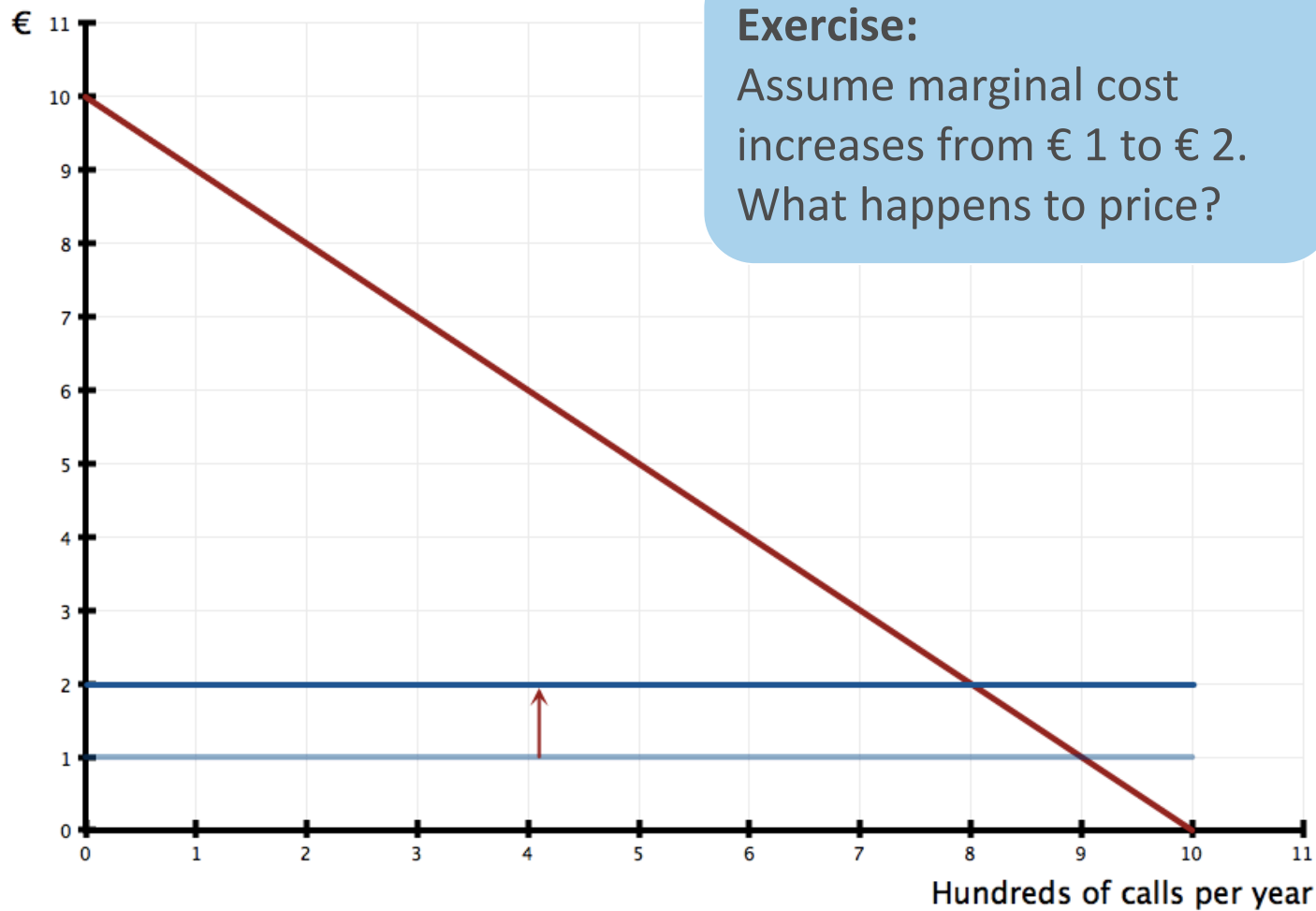


What determines price?



# 1. Cost

# What determines price?



## Exercise:

Assume marginal cost increases from € 1 to € 2.  
What happens to price?

# What determines price?



# What determines price?

- Conclusion: Price is increasing in cost
  - Marginal cost (but not fixed cost)
  - Pass through =  $1/2$  (but only in linear case)
  - In general: pass through  $0 - \infty$
  - By symmetry
    - If cost reduced, firms reduce price
    - but not necessarily by same amount

# What determines price?

- Questions
  - So, don't fixed costs matter at all for prices?
- Answer
  - Short term: No!
    - Only marginal cost.
  - Long run: Yes!
    - If average costs are not covered => exit => less competition => higher prices

# Formal analysis

Profit

$$\pi(q) = (P(q) - c) \cdot q$$

First order condition

$$\pi_q(q) = (P(q) - c) + P_q(q) \cdot q = 0$$

Rewrite

$$P(q) + P_q(q) \cdot q = c$$

Differentiate to study effect of change in cost

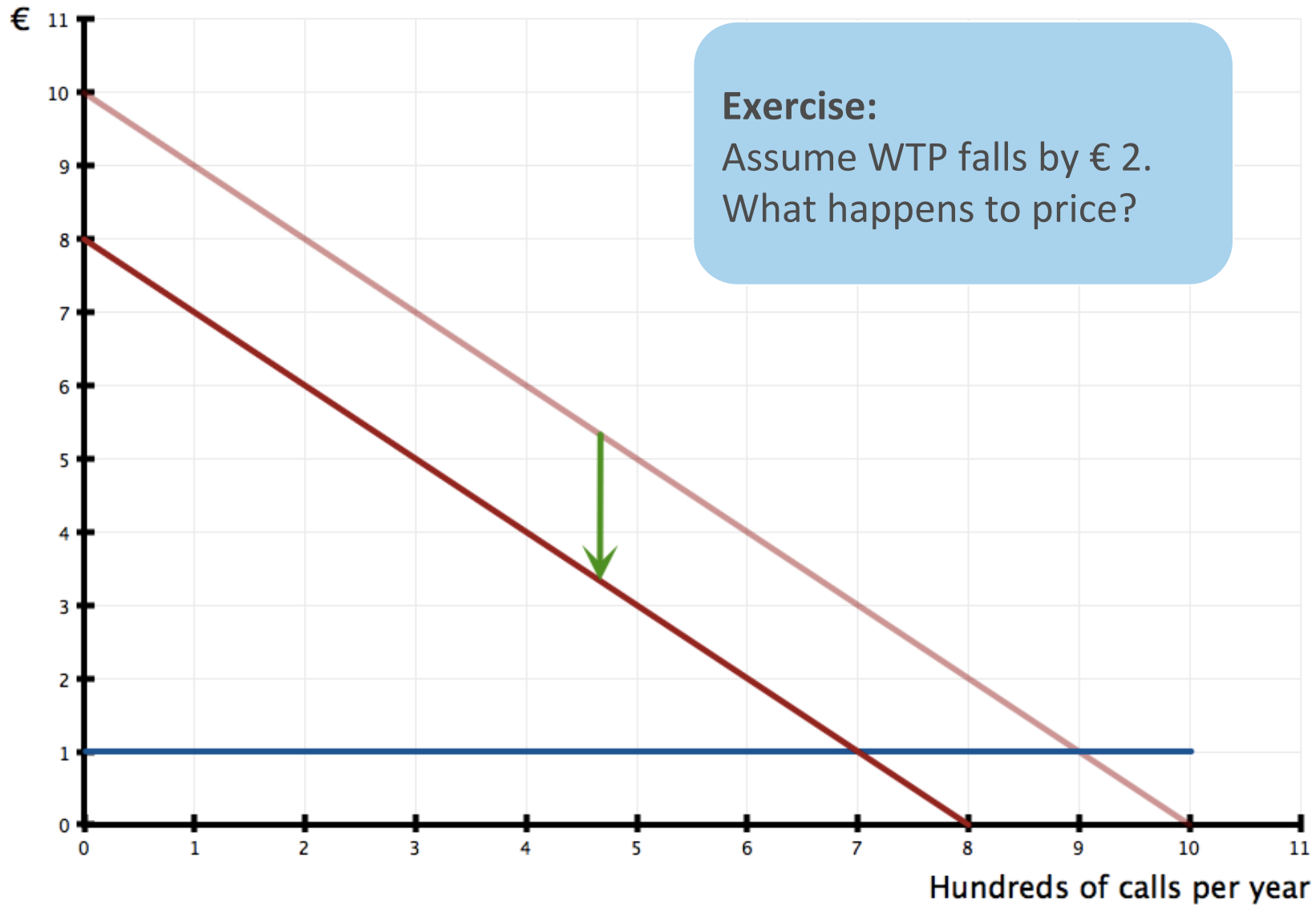
$$2 \cdot P_q(q) \cdot dq + P_{qq}(q) \cdot q \cdot dq = dc$$

Rewrite

$$\frac{dq}{dc} = \frac{1}{2 \cdot P_q(q) + P_{qq}(q) \cdot q} < 0 \quad (\text{Second order condition for maximization})$$

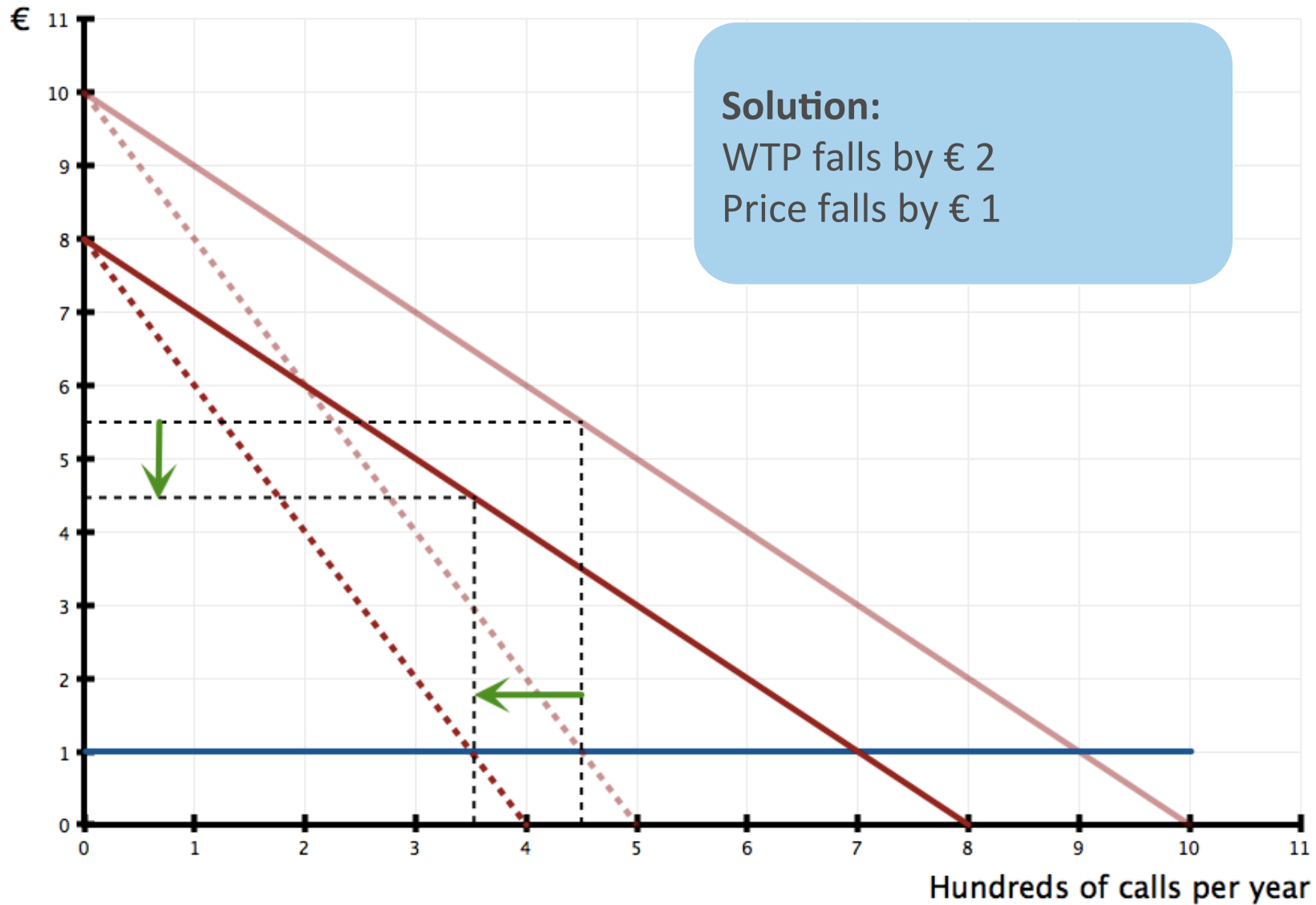
## 2. Demand

# What determines price?

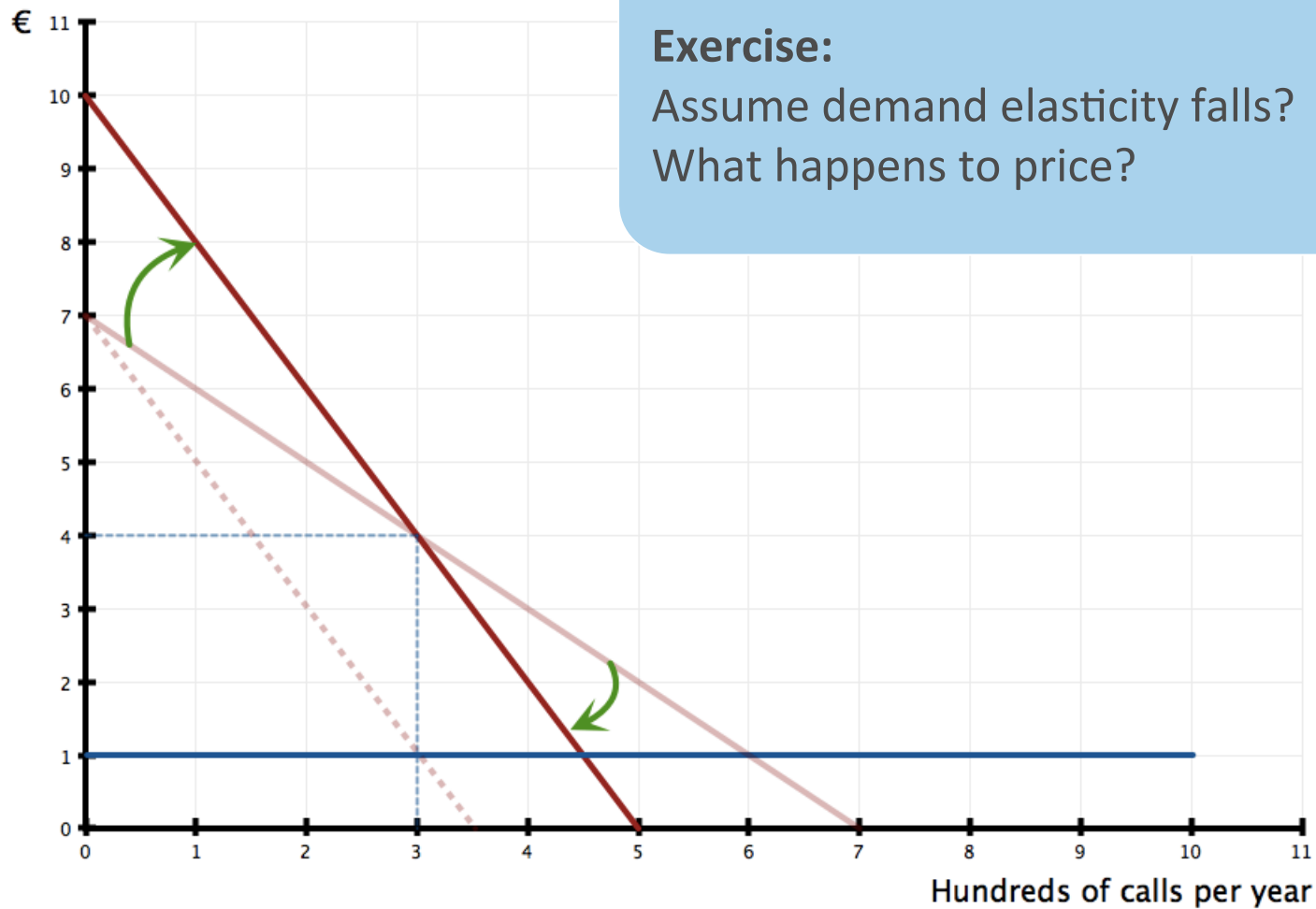




# What determines price?



# What determines price?



## Exercise:

Assume demand elasticity falls?

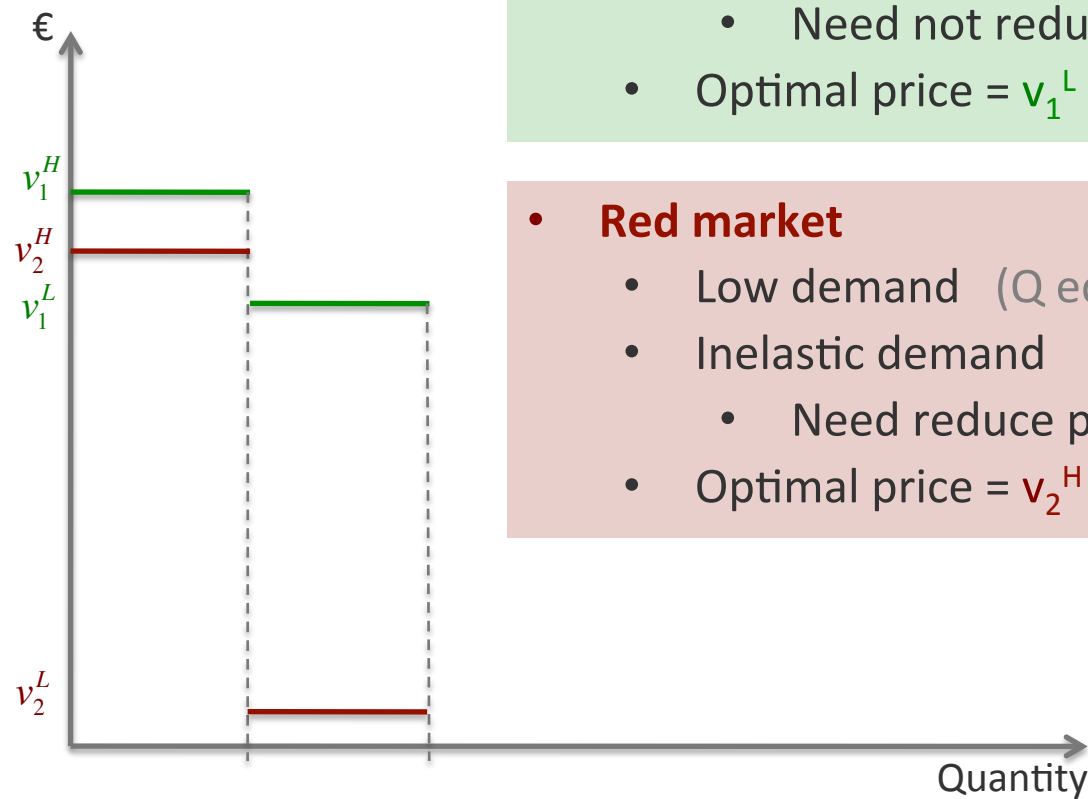
What happens to price?

# What determines price?



**Solution:**  
Price is increased!

# What determines price?



- **Green market**

- High demand
- Elastic demand
  - Need not reduce price much to sell 2<sup>nd</sup> unit
- Optimal price =  $v_1^L$

- **Red market**

- Low demand (Q equal or lower at every price)
- Inelastic demand
  - Need reduce price much to sell 2<sup>nd</sup> unit
- Optimal price =  $v_2^H > v_1^L$

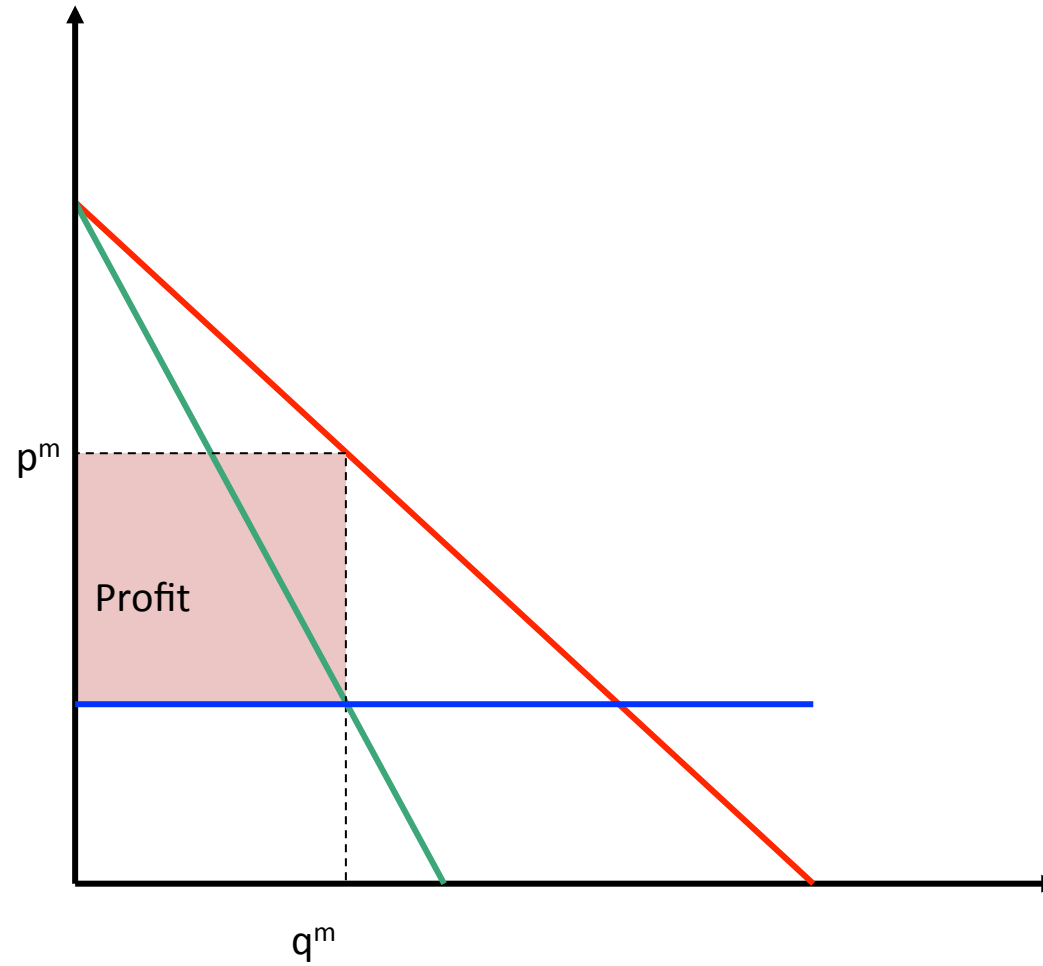
# Welfare & Efficiency

# Welfare

- Q: How much welfare is created in a market?
  - Firm owners?
    - = profit
  - Consumers?
    - = consumer's surplus (Q: define CS)
    - consumer's surplus =  $WTP - p$
  - Employees?
    - = no gain if  $w = \text{cost of working}$  (which is assumed)

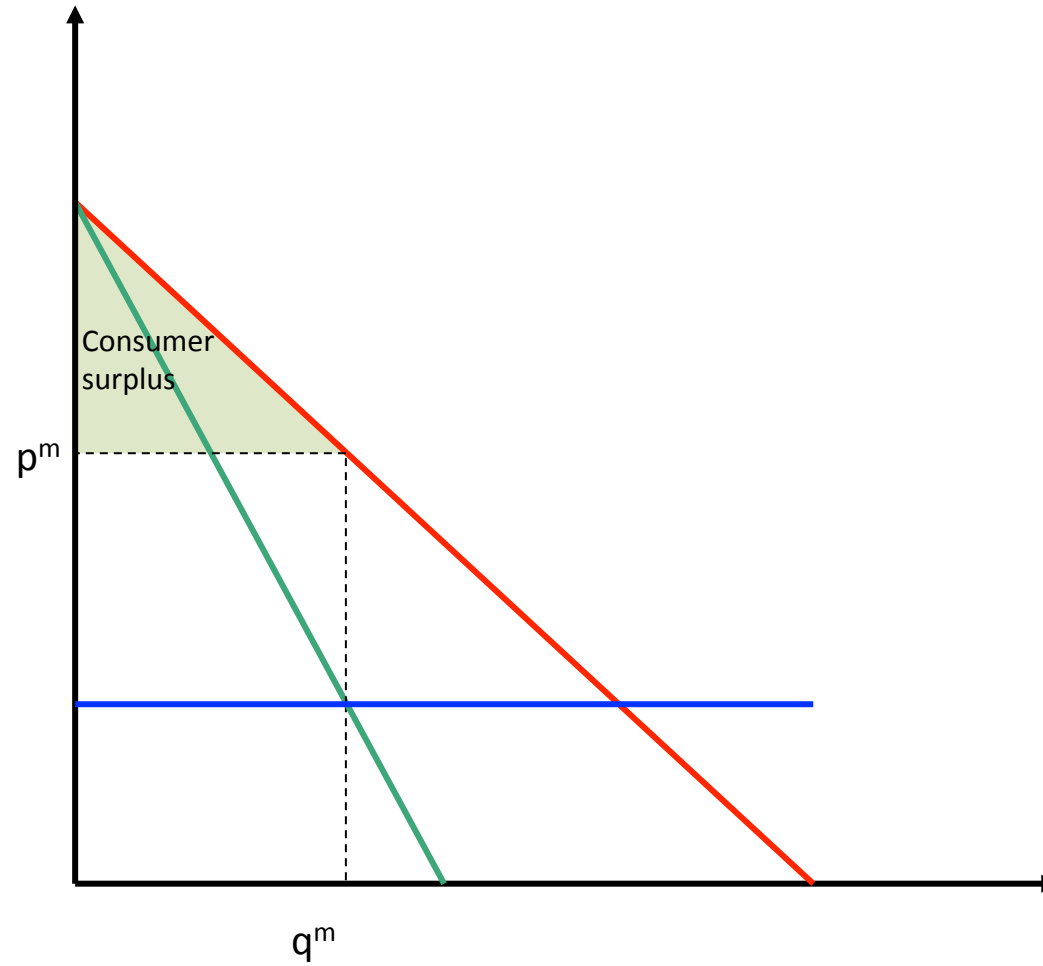
# Monopoly

## Welfare



# Monopoly

## Welfare

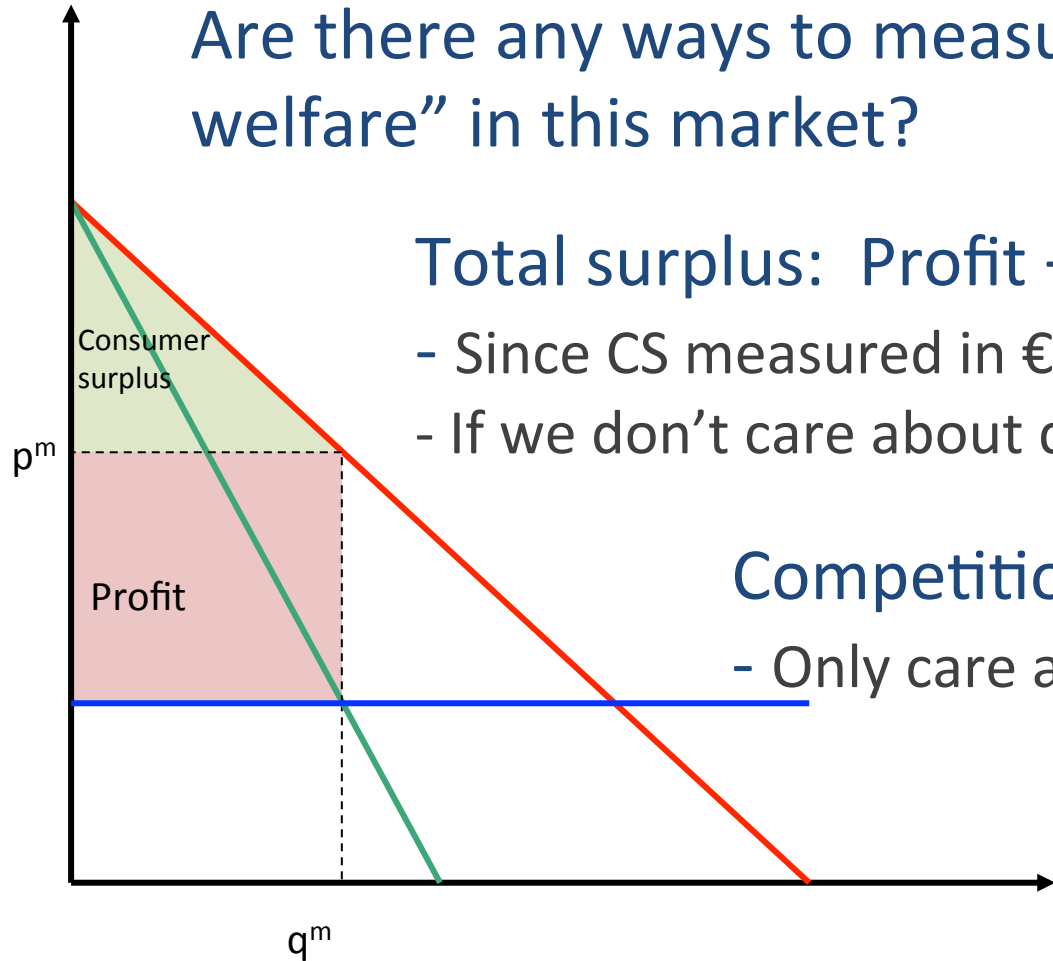




# Monopoly

## Welfare

Are there any ways to measure the “total welfare” in this market?



Total surplus: Profit + CS

- Since CS measured in €
- If we don't care about distribution

Competition authorities?

- Only care about CS!

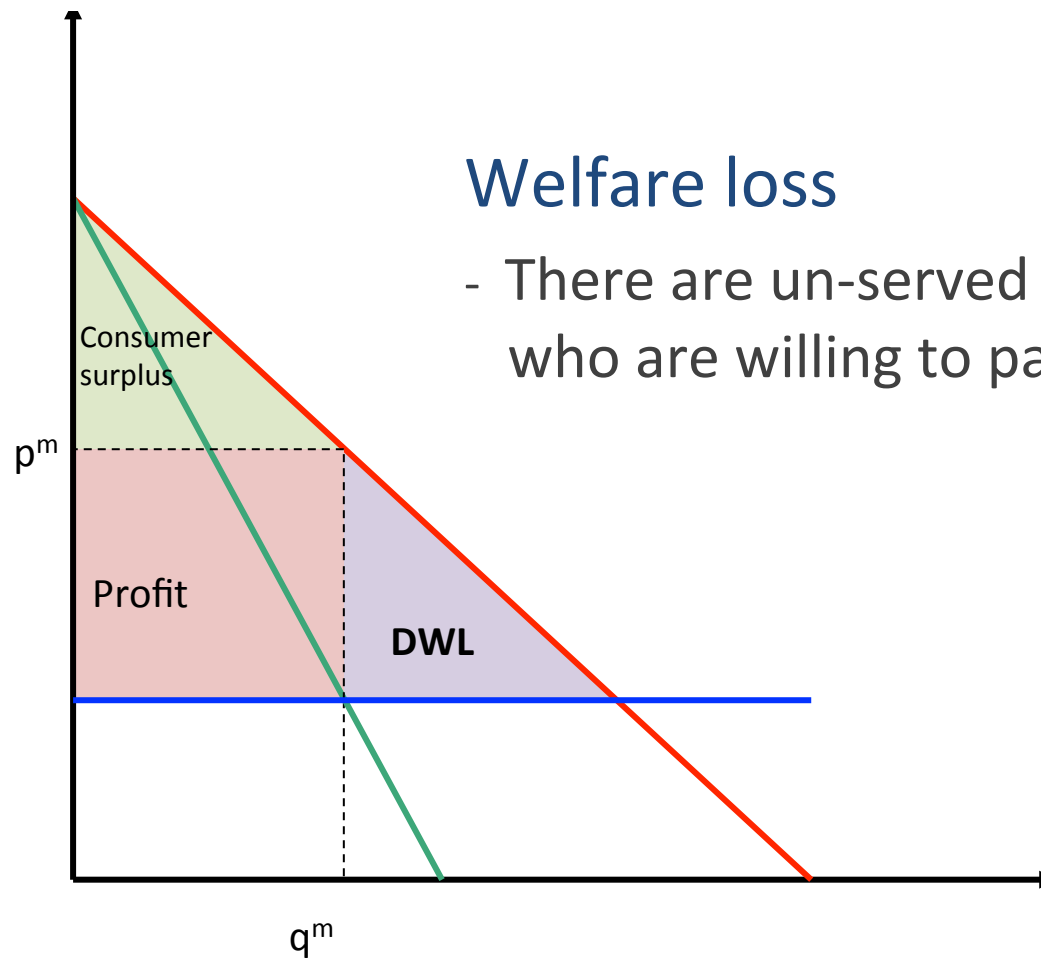
# Efficiency

- Is it possible to increase welfare in this market?
  - Q: Define Pareto efficiency
    - Allocation is in-efficient if it is possible to improve situation for one agent without making it worse for somebody else
  - Q: Define Compensation principle
    - Allocation is in-efficient if it can be changed in such a way that those who gain could compensate those who lose
    - Akin to “Total Surplus”

# Efficiency

- Q: Is it possible to increase welfare in this market?
  - Pareto efficiency
  - Compensation principle

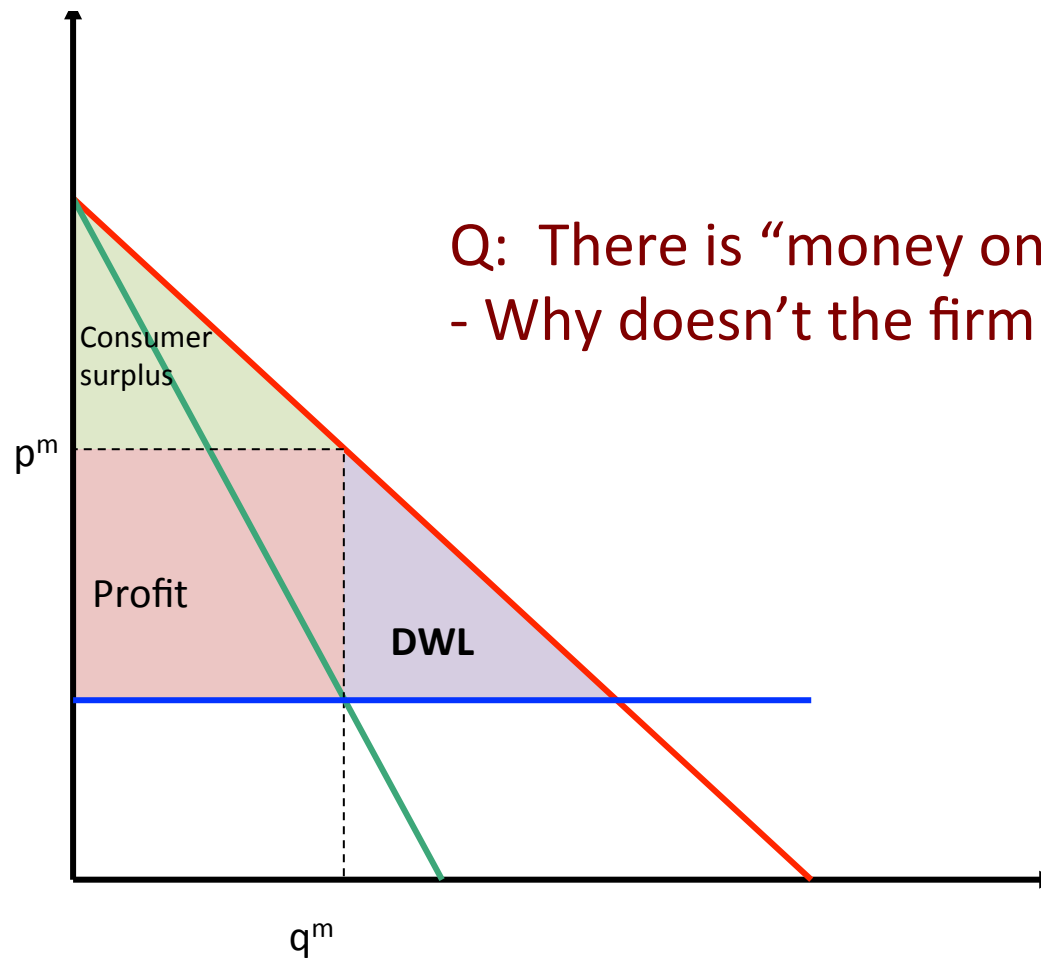
# Efficiency



## Welfare loss

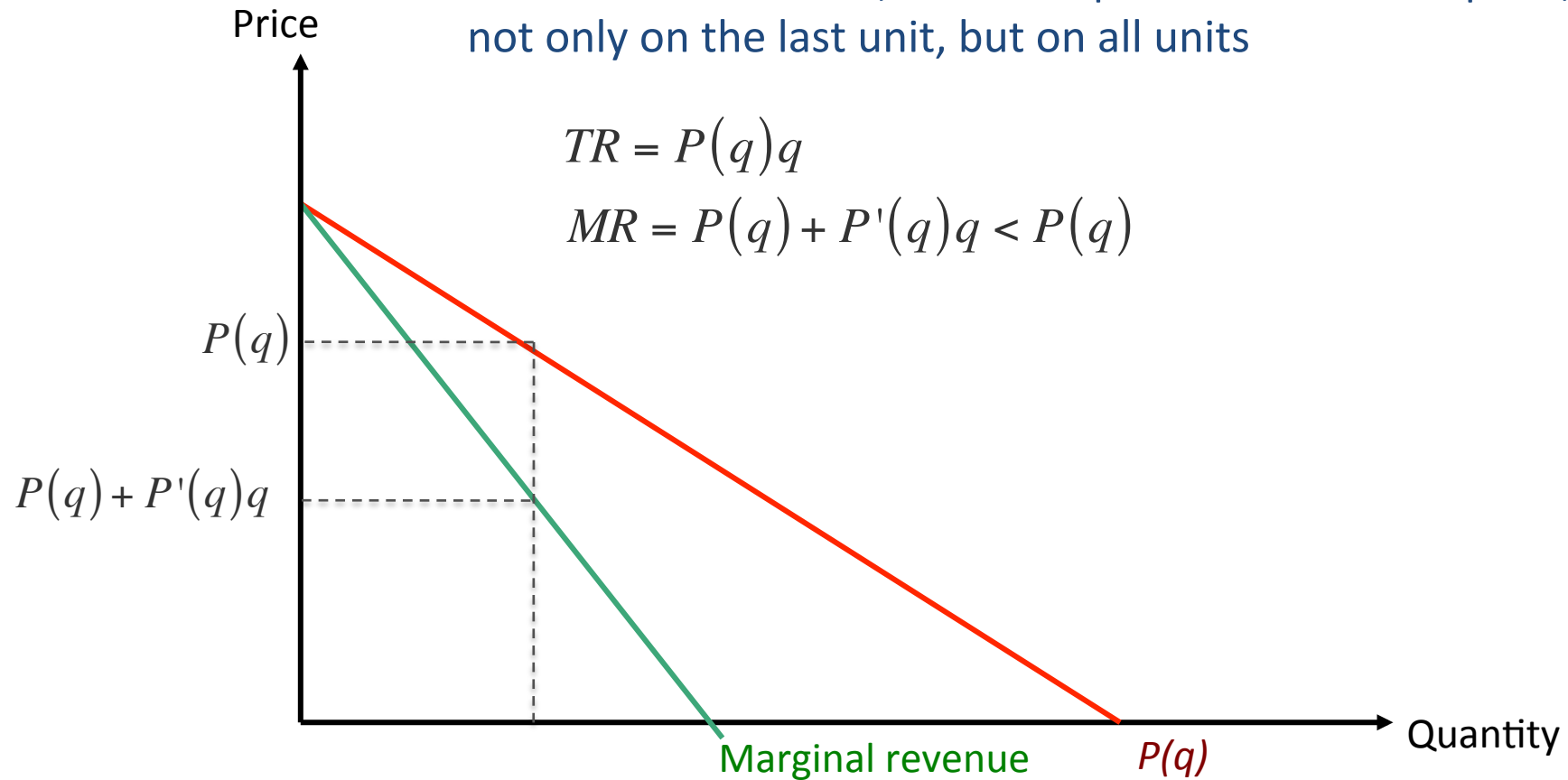
- There are un-served customers, who are willing to pay more than cost

# Efficiency



# Efficiency

A: To sell one more unit, the monopolist has to lower price, not only on the last unit, but on all units



# Efficiency

- Q: Other inefficiencies caused by monopoly?
  - Dead weight loss
  - Cost: Can pass on cost increases to consumers
  - Rent-seeking: Monopoly profit worth lobbying for
  - Other
    - Choice of quality
    - Investment
    - ...

# Price setting

Same question as before – slightly different analysis  
Derive convenient formula



# Price setting

- Previously

$$\max_q \pi(q) = P(q) \cdot q - C(q)$$

- Q: How do we rewrite as decision over  $p$ ?

$$\pi(p) = p \cdot D(p) - C(D(p))$$

Here we use the demand function  $D(p)$   
not the indirect demand function  $P(q)$

Composite function:  $C(D(p))$

# Price setting

Profit

$$\pi(p) = p \cdot D(p) - C(D(p))$$

Q: First order condition?

# Price setting

Profit

$$\pi(p) = (p - c)D(p)$$

First order condition

$$\pi_p(p) = D(p) + p \cdot D_p(p) - C_q(D(p)) \cdot D_p(p) = 0$$



Recall: Chain rule

# Price setting

Profit

$$\pi(p) = (p - c)D(p)$$

First order condition

$$\pi_p(p) = D(p) + p \cdot D_p(p) - C_q(D(p)) \cdot D_p(p) = 0$$

Factor out  $D_p(p)$

$$\pi_p(p) = D(p) + [p - C_q(D(p))] \cdot D_p(p) = 0$$

# Price setting

Profit

$$\pi(p) = (p - c)D(p)$$

First order condition

$$\pi_p(p) = D(p) + p \cdot D_p(p) - C_q(D(p)) \cdot D_p(p) = 0$$

Factor out  $D_p(p)$

$$\pi_p(p) = D(p) + [p - C_q(D(p))] \cdot D_p(p) = 0$$

Rewrite

$$\frac{p - C_q}{p} = -\frac{D(p)}{p \cdot D_p(p)}$$

# Price setting

Rewrite

$$\frac{p - C_q}{p} = - \frac{D(p)}{p \cdot D_p(p)}$$



Q: What is this?

# Price setting

Rewrite

$$\frac{p - C_q}{p} = - \frac{D(p)}{p \cdot D_p(p)}$$

Elasticity of demand

$$\eta(p) \equiv \frac{p \cdot D_p(p)}{D(p)}$$

Market power (Lerner index)

$$L \equiv \frac{p - MC}{p}$$

# Price setting

Rewrite

$$\frac{p - C_q}{p} = -\frac{D(p)}{p \cdot D_p(p)}$$

Interpretation

$$L = -\frac{1}{\eta(p)}$$



## Inverse elasticity rule

Monopolist's market power determined by consumers' price sensitivity

Elasticity of demand

## Caution

This expression "hides" the fact that the level of demand also matters

$$L = \frac{p}{p}$$



3<sup>rd</sup> degree price discrimination

# 3<sup>rd</sup> degree price discrimination

- Conclusion: Price depends on demand
  - High demand  $\Leftrightarrow$  high WTP  $\Rightarrow$  high price (typically)
  - Low price sensitivity  $\Rightarrow$  High price (typically)
- 3<sup>rd</sup> degree price discrimination
  - Recall pharmaceutical market
    - Low prices in Greece, Spain, Portugal
    - High prices in Switzerland, Germany, UK
  - Definition of P.D:
    - Charge different price for same product to different consumers

# 3<sup>rd</sup> degree price discrimination

- Q: Under what conditions can firms charge different prices from different consumers based on WTP?
  - Information about WTP
  - No arbitrage (but internal market)

# 3<sup>rd</sup> degree price discrimination

- Q: Is it a good or a bad thing that prices of pharmaceuticals is lower in Greece than in Sweden?
  - Bad: Inefficient distribution of given amount of goods
  - Good: If price discrimination illegal, firms may set high price, and not sell in poor countries

But: Even better if  $p_{\text{Greece}} = p_{\text{Switzerland}} = mc$

# 3<sup>rd</sup> degree price discrimination

- What if firm must earn  $p > c$  to finance R&D.  
Are price differences then good or bad?
  - Good: It may be fair that countries with low income pays less
  - Good: To minimize total global welfare loss, charge high price in country with low price sensitivity (Ramsey pricing)

# Price Regulation

# Price Regulation

- Q: Current regulation
  - Competition law
    - Abuse of dominant position
    - Dominant firms may not “impose unfair prices”
    - Never used
  - Sector specific regulation
    - Rental apartments
    - Telecom; District heating (has been discussed)
    - On-patent medicines; Pharmacies
  - Rationing and price regulation during crisis
    - If Sweden cut off from imports (food, oil, ... )
    - Removed?

# Price Regulation

- Q: Why so little price regulation?
- Q: Problems with price regulation?
  1.  $P = MC$  may not work when there are fixed costs
  2. Information
  3. Incentives for innovation
  4. Regulatory uncertainty
  5. Administrative costs



# Price Regulation

- Fixed costs
  - DWL overestimates potential gain from regulation
  - $P > MC$  to finance fixed costs
  - Alternative: subsidize & use taxes  $\Rightarrow$  DWL moved

# Price Regulation

- Q: What information would regulator need?
  - If no fixed costs only MC
  - Otherwise
    - Cost function
    - Demand function

# Price Regulation

- Incentives for innovation
  - Monopoly: High WTP  $\Rightarrow$  high price
  - Firms incentives to invent new products that people are willing to pay for

# Price Regulation

- Regulatory uncertainty
  - 2013 Swedish Market Court decided a case about what prices TeliaSonera was allowed to charge for broadband services in 2000

# Price Regulation

- Administrative costs
  - Example: TeliaSonera's external legal advice at least €1mn

Case study:  
Value-Based Pricing of Medicines

# VBP

- Dilemma
  - Efficient use of existing medicines
    - $p = MC$
  - Incentives to develop new medicines
    - Huge fixed costs  $\Rightarrow p > MC$
    - Efficient incentives  $\Rightarrow p$  must be related to WTP

# VBP

- Solution: Patents  $\Rightarrow p > MC$ 
  - Pros: Investment incentives
  - Cons: Large DWL, since
    - WTP high
    - MC low
- Solution 2: Subsidize medicines
  - Average subsidy in Sweden 80%
  - People will consume despite high price!



# VBP

- Exercise: Compute monopoly price
  - Demand:  $q = v - p^{\text{Consumer}}$
  - Cost:  $C = c \cdot q$
  - Subsidy:  $p^{\text{Consumer}} = \lambda \cdot p^{\text{Producer}}$ ,
- Exercise: Compare
  - No subsidy  $\lambda = 1$  and  $\lambda = 0.2$
  - Assume:  $v = 10; c = 1$

# VBP

- Monopoly solution

$$\pi = (p^P - c) \cdot (v - \lambda \cdot p^P)$$

$$\frac{\partial \pi}{\partial p^P} = (v - \lambda \cdot p^P) - \lambda \cdot (p^P - c) = 0$$

$$p^P = \frac{\frac{v}{\lambda} + c}{2} \quad p^C = \frac{v + \lambda \cdot c}{2} \quad q = v - \frac{v + \lambda \cdot c}{2} = \frac{v - \lambda \cdot c}{2}$$

- Comparison

$$p^P = \frac{10+1}{2} = 5.5$$

$$p^C = \frac{10+1}{2} = 5.5$$

$$q = \frac{10-1}{2} = 4.5$$

$$p^P = \frac{\frac{10}{0.2} + 1}{2} = 25.5$$

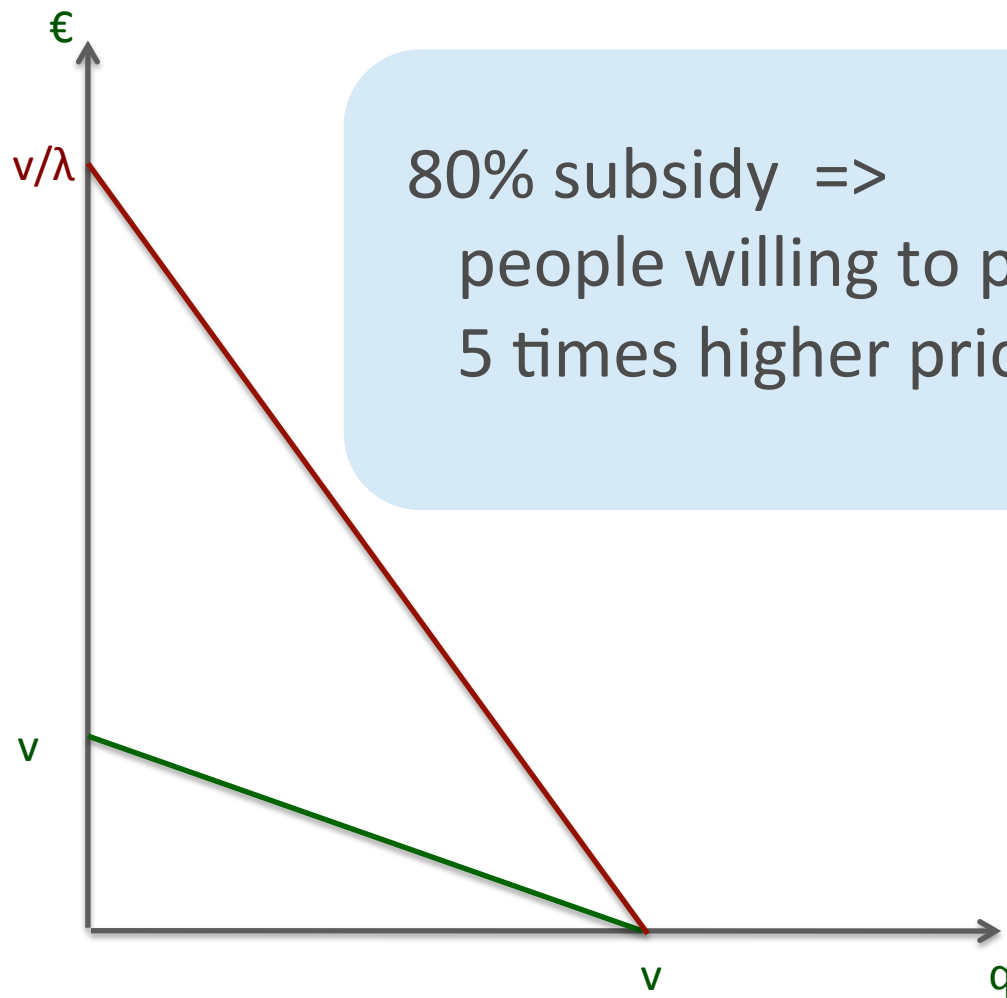
$$p^C = \frac{10+0.2 \cdot 1}{2} = 5.1$$

$$q = \frac{10-0.2 \cdot 1}{2} = 4.8$$

# VBP

- Subsidy + Monopoly pricing
  - Subsidy turned into gift to firms
  - Little effect on DWL
  - Little insurance to citizens

# VBP



# VBP

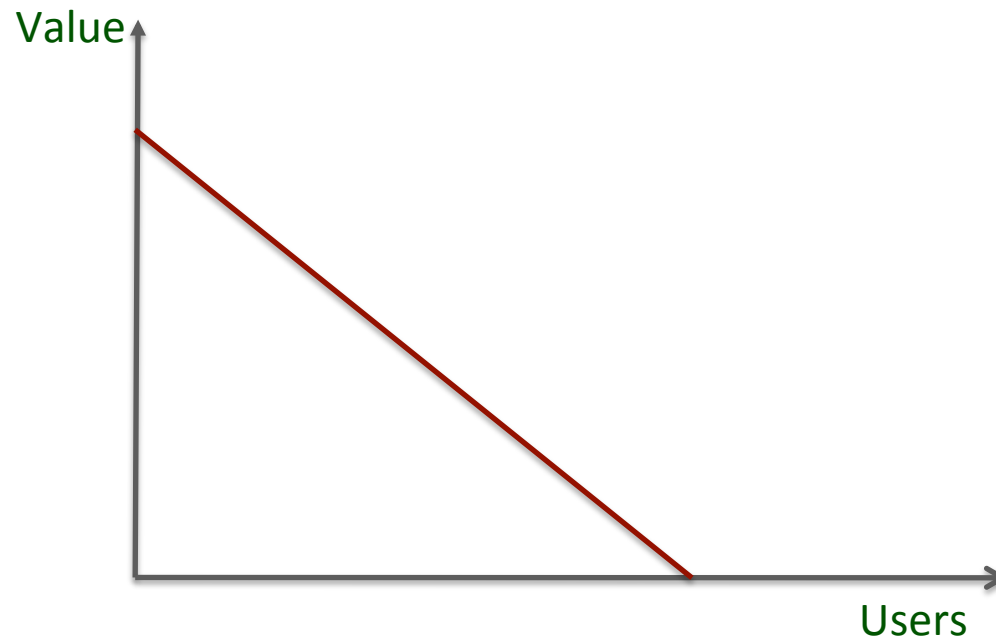
- Solution: VBP (= form of price regulation)
  - Company apply to be included in the subsidy
  - Tandvårds- och Läkemedelsförmånsverket (TLV)

# VBP

- Company provides information about value of drug
  - People with different diseases
  - People with different side-effects

# VBP

- Company provides information about value of drug
  - People with different diseases
  - People with different side-effects



# VBP

- Note 1
  - Value is for average individual  
(Income differences are assumed away)



# VBP

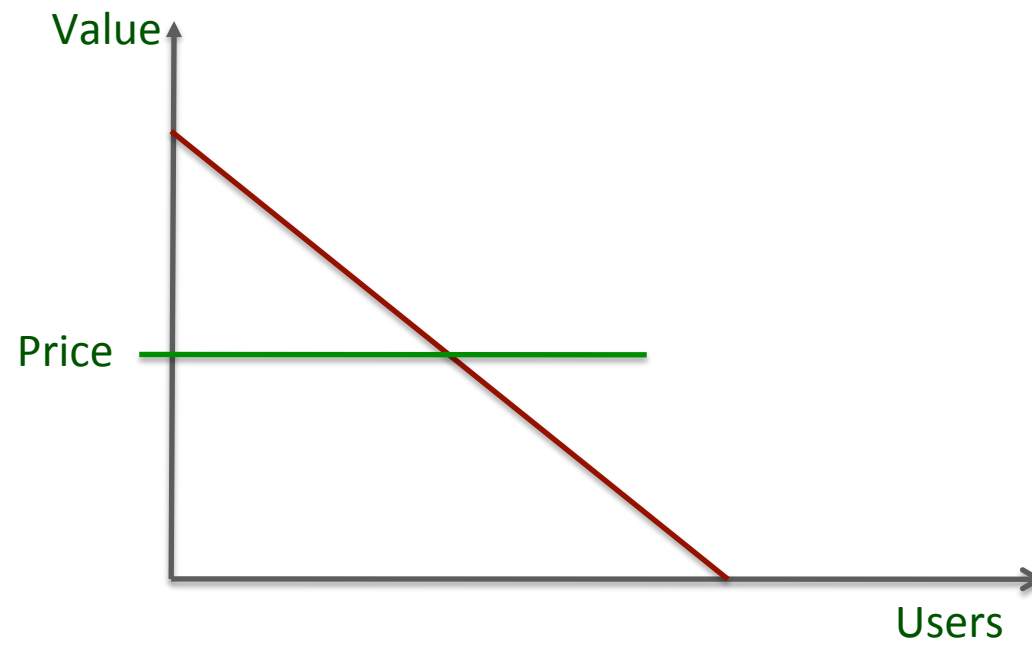
- Note 2
  - Companies must undertake substantial research to prove value
    - Medical effects
    - Economic value of medical effects

# VBP

- Price
  - Company sets price
  - TLV decides which users get the drug subsidized

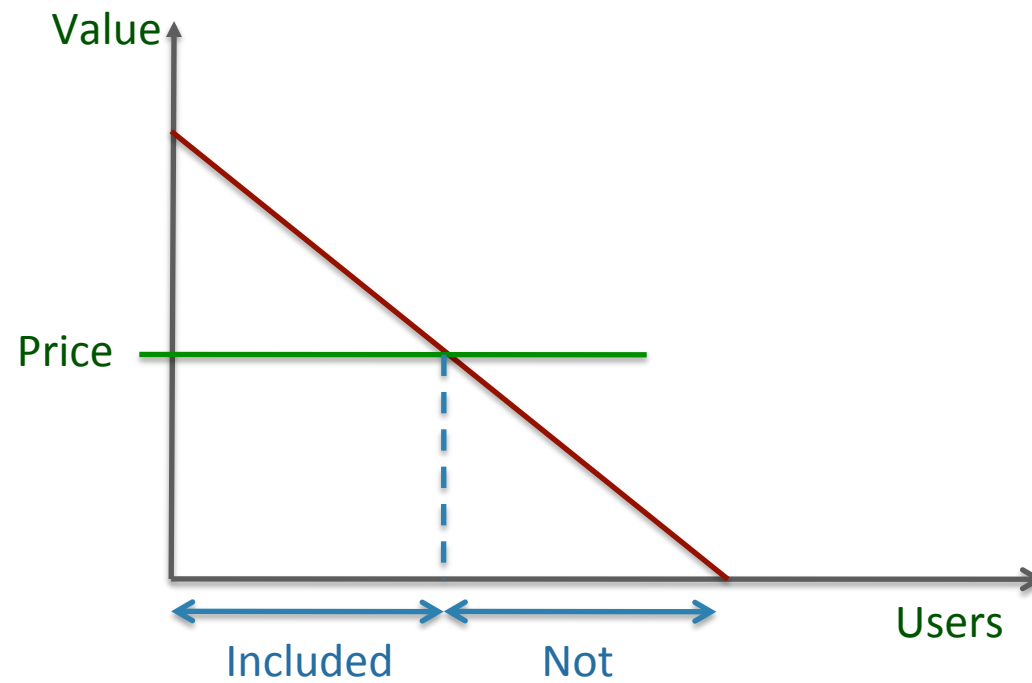
# VBP

Firm sets price



# VBP

TLV sets quantity



# VBP

- Conclusion
  - Value-based pricing = normal “monopoly” pricing
  - But the firm cannot “steal” the subsidy
- Motivation
  - $P = \text{“social value of drug”}$  gives firms incentives to develop drugs creating value