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Static Games

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Interdependent decisions

- Food retailing
 - ICA:s optimal price depends on Coop:s price
 - Coop: optimal price depends on ICA:s price
- How analyze?

Interdependent decisions

- Theory of interdependent decision making
(a.k.a Game Theory)
 - How should we expect people to behave when the outcome depends on several persons actions?

Prisoners' Dilemma

Prisoners' Dilemma

- Police arrest two suspects
 - Enough evidence for short conviction (1 month)
 - More evidence needed for long conviction (10 months)
- Can the prisoners be made to confess?

Prisoners' Dilemma

- Prosecutor asks prisoners to volunteer information (to “rat”)
- Prosecutor offers rebate on sentence
 - If both “clam”
 - both get 1 month
 - If one person “rats”
 - the betrayer goes free
 - the other gets 10 months
 - If both “rat”
 - both get 4 months

Prisoners' Dilemma

- Prisoners put in separate cells
 - Simultaneous decisions

Prisoners' Dilemma

An outcome matrix summarizes the game:

		Prisoner 2	
		Clam	Rat
Prisoner 1	Clam	1, 1	10, 0
	Rat	0, 10	4, 4

If prisoner 1 rats and prisoner 2 clams:

- Prisoner 1 goes free
- Prisoner 2 gets 10 months

Prisoners' Dilemma

An outcome matrix summarizes the game:

		Prisoner 2	
		Clam	Rat
Prisoner 1	Clam	1, 1	10, 0
	Rat	0, 10	4, 4

Complete information

- Both prisoners know all facts

Q: Assume you are prisoner 1

- What would you do?

Prisoners' Dilemma

An outcome matrix summarizes the game:

		Prisoner 2	
		Clam	Rat
Prisoner 1	Clam	1, 1	10, 0
	Rat	0, 10	4, 4

If you only care for the other:

- Clam!

If you are selfish:

- Rat!

Prisoners' Dilemma

An outcome matrix summarizes the game:

		Prisoner 2	
		Clam	Rat
Prisoner 1	Clam	1, 1	10, 0
	Rat	0, 10	4, 4

We need to know people's preferences to predict how they will behave!

Prisoners' Dilemma 1

- Alternative representation
 - Utility = 10 - #months
- Payoff matrix

	Clam	Rat
Clam	9, 9	0, 10
Rat	10, 0	6, 6

Selfish

- Prisoners only care about their own sentence

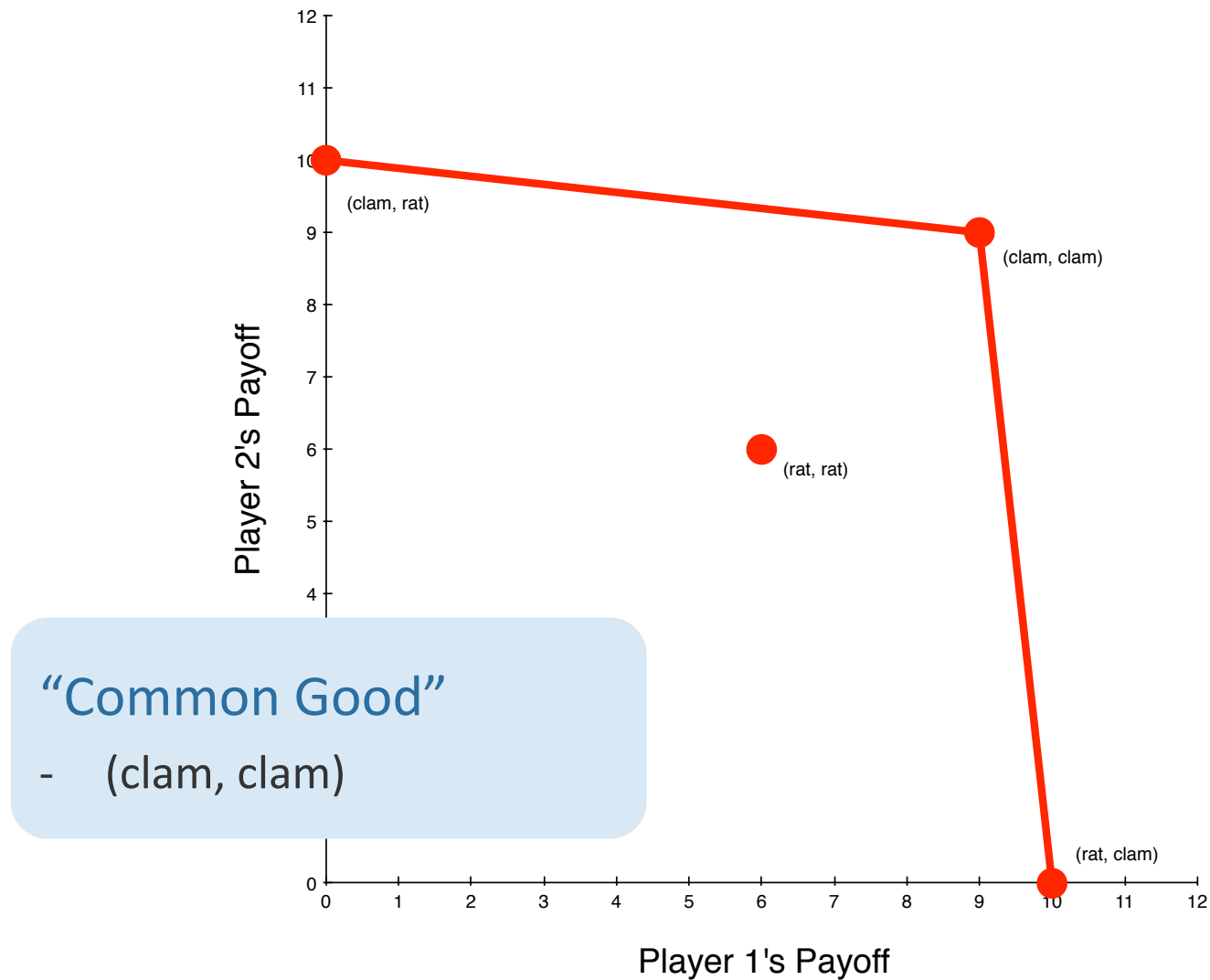
Convention

- Player 1 is row player

Complete information

- Both prisoners know all facts

Prisoners' Dilemma 1



Prisoners' Dilemma 1

- Assume they agreed to clam
 - Will they honor the agreement?

Prisoners' Dilemma 1

- Best-reply function
 - Simple procedure to predict behavior

Prisoners' Dilemma 1

- Player 1

- Q: what is player 1's best choice if 2 would clam?
- A: to rat

	Clam	Rat
Clam	9, 9	0, 10
Rat	<u>10</u> , 0	6, 6

Best reply

= utility maximizing choice for a given behavior by the other

Prisoners' Dilemma 1

- Player 1

- Q: what is player 1's best choice if 2 would rat?
- A: to rat

	Clam	Rat
Clam	9, 9	0, 10
Rat	<u>10</u> , 0	<u>6</u> , 6

Best reply

= utility maximizing choice for a given behavior by the other

Prisoners' Dilemma 1

- Player 1:s best reply *function*
 - IF player 2 clams, THEN player 1:s best reply is to rat
 - IF player 2 rats, THEN player 1:s best reply is to rat

	Clam	Rat
Clam	9, 9	0, 10
Rat	<u>10</u> , 0	<u>6</u> , 6

Best reply

= utility maximizing choice for a **given** behavior by the other

Best reply function

= rule assigning best choice for **every possible** behavior by the other

Prisoners' Dilemma 1

- Here player 1's best-reply function says
 - Rat, independent of what the other player does

Notice: Rat is a strictly dominating strategy.

Definition: A strategy is *strictly dominating* if

- it is strictly better than all other strategies,
- independent of what other people do.

Notice: Very rare

Prisoners' Dilemma 1

- Here player 1's best-reply function says
 - Rat, independent of what the other player does

Notice: Clam is a strictly dominated strategy.

One should never play a strictly dominated strategy

Notice: Quite common.

Prisoners' Dilemma 1

- Player 2
 - Q: what is player 2's best choice if 1 would clam?
 - A: to rat

	Clam	Rat
Clam	9, 9	0, <u>10</u>
Rat	10, 0	6, 6

Prisoners' Dilemma 1

- Player 2
 - Q: what is player 2's best choice if 1 would rat?
 - A: to rat

	Clam	Rat
Clam	9, 9	0, <u>10</u>
Rat	10, <u>0</u>	6, <u>6</u>

Prisoners' Dilemma 1

- Player 2:s best reply *function*
 - IF player 1 clams, THEN player 2:s best reply is to rat
 - IF player 1 rats, THEN player 2:s best reply is to rat

	Clam	Rat
Clam	9, 9	0, <u>10</u>
Rat	10, 0	6, <u>6</u>

Prisoners' Dilemma 1

- Here player 2's best-reply function says
 - Rat, independent of what the other player does
- Conclusion
 - Both will rat

Prisoners' Dilemma 1

- Important insights
 1. Conflict: Private incentives vs. Efficiency
 - Rational choice may lead to bad outcomes
 2. Agreements beforehand do not matter, if players don't have incentives to follow agreement
 3. Sometimes exist dominant strategies

Prisoners' Dilemma 2

Prisoners' Dilemma 2

- Player 1 is a “moral person” (or altruist)
 - Utility = $20 - \Sigma\#months$

- Outcome matrix (months)

	Clam	Rat
Clam	1, 1	10, 0
Rat	0, 10	4, 4

- Payoff matrix

	Clam	Rat
Clam	18, 9	10, 10
Rat	10, 0	12, 6

Prisoners' Dilemma 2

	Clam	Rat
Clam	18, 9	10, 10
Rat	10, 0	12, 6

Q: Does player 1 have strictly dominated strategy?

Prisoners' Dilemma 2

	Clam	Rat
Clam	<u>18</u> , 9	10, 10
Rat	10, 0	<u>12</u> , 6

Q: Does player 1 have strictly dominated strategy?

A: No

- Better to clam if 2 clams
- Better to rat if 2 rats

Prisoners' Dilemma 2

	Clam	Rat
Clam	<u>18</u> , 9	10, 10
Rat	10, 0	<u>12</u> , 6

Q: What should player 1 do?

Prisoners' Dilemma 2

	Clam	Rat
Clam	<u>18</u> , 9	10, <u>10</u>
Rat	10, 0	<u>12</u> , <u>6</u>

A:

- Player 1 knows that player 2 will rat!
- Then better for 1 to also rat!

Prisoners' Dilemma 2

	Clam	Rat
Clam	<u>18</u> , 9	10, <u>10</u>
Rat	10, 0	<u>12</u> , <u>6</u>

Important insight

In a strategic situation, people need to put themselves into other peoples shoes

Prisoners' Dilemma 2

	Clam	Rat
Clam	<u>18</u> , 9	10, <u>10</u>
Rat	10, 0	<u>12</u> , <u>6</u>

Notice: if (rat, rat) would be played

- Player 1 plays a best reply against player 2's behavior
- Player 2 plays a best reply against player 1's behavior

Prisoners' Dilemma 2

We say (rat, rat) is an *equilibrium*

Player 1 maximizes utility, given player 2's behavior

Player 2 maximizes utility, given player 1's behavior

Prisoners' Dilemma 2

- Q: Is any other outcome an equilibrium?
 - A: No!
 - E.g.: (clam, rat) => player 1 has incentive to change behavior

	Clam	Rat
Clam	9, 9	0, <u>10</u>
Rat	<u>10</u> , 0	<u>4</u> , <u>4</u>

Games in normal form

Normal Form

- Game in normal form
 - Players
 - Strategies
 - Payoffs (for all possible combinations of strategies)
- Prisoners Dilemma
 - Players: Prisoner 1, Prisoner 2
 - Strategies: rat, clam
 - Payoffs: $u_1(\text{clam}, \text{rat}) = 10$, and so on.

Normal Form

- Payoff matrix
 - Summarizes normal form (of 2-person game)
- Interpretation
 - Players choose simultaneously
 - Players know the game

Prisoners' Dilemma

- Definition: *Strategy profile*
 - A list of strategies, one for each player
- Example (Prisoners' Dilemma)
 - (rat, rat), (rat, clam), (clam, rat), (clam, clam)

Prisoners' Dilemma

- Definition: *Nash equilibrium*
 - A strategy profile such that
 - i. each player maximizes his utility,
 - ii. given that all other players follow their strategies

Nash Equilibrium

- Formal definition for two-player game

Strategy profile (s_1^*, s_2^*) is a Nash Equilibrium if :

$$u_1(s_1^*, s_2^*) \geq u_1(s_1, s_2^*) \quad \text{for all } s_1 \text{ in } S_1$$

$$u_2(s_1^*, s_2^*) \geq u_2(s_1^*, s_2) \quad \text{for all } s_2 \text{ in } S_2$$

Prisoners' Dilemma

- Why should we expect people to follow equilibrium?
 - Equilibrium behavior is by no means guaranteed,
 - but...

Prisoners' Dilemma

- Assume
 - All people are *rational*
(= they maximize their utilities, given their expectations of what other people will do)
 - All people *know* what will happen, before they make their choices
- Then
 - People must behave according to an equilibrium

Prisoners' Dilemma

- Argument: Assume the opposite
 - All people rational & All people know what will happen
 - Their behavior is not a NE (ex: Clam, Clam)
- Then
 - Then at least one person is supposed not to play best reply
 - Then at least this person will deviate from the prediction, since he is rational
 - Then, after all, people didn't know what was going to happen

Nash Equilibrium

- Formally

Rationality

$$u_1(s_1^*, E_1 s_2) \geq u_1(s_1, E_1 s_2) \quad \text{for all } s_1 \text{ in } S_1$$

Nash Equilibrium

- Formally

Rationality

$$u_1(s_1^*, E_1 s_2) \geq u_1(s_1, E_1 s_2) \quad \text{for all } s_1 \text{ in } S_1$$

Coordination

$$E_1 s_2 = s_2^*$$

Nash Equilibrium

- Formally

Rationality

$$u_1(s_1^*, E_1 s_2) \geq u_1(s_1, E_1 s_2) \quad \text{for all } s_1 \text{ in } S_1$$

Coordination

$$E_1 s_2 = s_2^*$$

Rationality & Coordination \Rightarrow Equilibrium

Nash Equilibrium

- Q: When should we use equilibrium analysis to predict behavior?
 - A: In situations where it is reasonable to assume that
 - People are rational
 - People for some reason understand what the outcome will be

Prisoners' Dilemma

- Exercise (for break)

- Consider Prisoners' Dilemma Game with #months

	Clam	Rat
Clam	1, 1	10, 10 - r1
Rat	10 - r1, 10	10 - r2, 10 - r2

- What “rebates” r_1 and r_2 do you need to give in order to:
 - Guarantee that (Rat, Rat) is an equilibrium?
 - Guarantee that (Rat, Rat) is the only equilibrium?

Prisoners' Dilemma

- Exercise (for break)

- Consider Prisoners' Dilemma Game with #months

	Clam	Rat
Clam	1, 1	10, 10 - r1
Rat	10 - r1, 10	10 - r2, 10 - r2

- What “rebates” r_1 and r_2 do you need to give in order to:

- Guarantee that (Rat, Rat) is an equilibrium?
 - Guarantee that (Rat, Rat) is the only equilibrium?

Answers

Coordination Game

Coordination Game

- Situation
 - Cars meet on roads
 - If all keep to left (or right) they pass
 - Otherwise they crash
 - Sometimes choices are simultaneous
 - curves
 - top of hills

Coordination Game

- Lets try to represent such a situation as a game
- Lets make it as simple as possible

Coordination Game

- Represent situation as a game
 - Q: Three components of game?
 - Game = (Players, Strategies, Payoffs)
 - Q: Players?
 - Players = (driver 1, driver 2)
 - Q: Strategy sets?
 - Strategy set of driver i = (right, left)
 - Q: Payoff functions (and outcomes)?

Coordination Game

- Outcomes

	Left	Right
Left	Pass	Crash
Right	Crash	Pass

- Payoffs

	Left	Right
Left	1, 1	-1, -1
Right	-1, -1	1, 1

Coordination Game

- Q: What outcome should we predict?
 - A: Nash equilibrium
- Q: How do we find equilibrium?
 - A: Best reply analysis

Coordination Game

- Q: Best reply function for player 1?

	Left	Right
Left	1, 1	-1, -1
Right	-1, -1	1, 1

- A: “Do the same”

	Left	Right
Left	<u>1</u> , 1	-1, -1
Right	-1, -1	<u>1</u> , 1

Coordination Game

- Q: Best reply function for player 2

	Left	Right
Left	1, 1	-1, -1
Right	-1, -1	1, 1

- A: “Do the same”

	Left	Right
Left	1, <u>1</u>	-1, -1
Right	-1, -1	1, <u>1</u>

Coordination Game

- Q: What is the equilibrium strategy profile?
- A: (left, left) and (right, right)

	Left	Right
Left	<u>1</u> , <u>1</u>	-1, -1
Right	-1, -1	<u>1</u> , <u>1</u>

Coordination Game

- Multiple equilibria
 - Illustrates importance of coordination
 - Rationality is not enough

Coordination Game

- How does coordination arise?
 - Ordinary game theory has no answer
 - Conventions
 - May be the result of learning
 - Pre-play communication
 - Anderson and Peterson specializing in comp. advantage
 - Self-enforcing agreement

Coordination Game

- Google:
 - Convention
 - Social norm

Chicken

Chicken

- Situation: Single-lane bridge
 - Drivers head for *single-lane* bridge from opposite directions
 - Sometimes two drivers arrive at same time
 - If both continue, they crash
 - If both stop, both are delayed
 - If one stops, he is delayed but the other can pass without delay

Coordination Game

- Represent situation as a game
 - Q: Three components of game?
 - Game = (Players, Strategies, Payoffs)
 - Q: Players?
 - Players = (driver 1, driver 2)
 - Q: Strategy sets?
 - Strategy set of driver i = (continue, stop)
 - Q: Payoff functions (and outcomes)?

Chicken

- Outcomes

	Stop	Continue
Stop	Delay, Delay	Delay, Pass
Continue	Pass, Delay	Crash, Crash

- Payoffs

	Stop	Continue
Stop	0, 0	0, 2
Continue	2, 0	-10, -10

Chicken

- Q: Find equilibrium

	Stop	Continue
Stop	0, 0	0, 2
Continue	2, 0	-10, -10

Chicken

- Two equilibria (Continue, Stop) and (Stop, Continue)

	Stop	Continue
Stop	0, 0	<u>0</u> , <u>2</u>
Continue	<u>2</u> , <u>0</u>	-10, -10

Chicken

- Both equilibria *asymmetric*
 - Despite both players being in the “same situation”
 - They have to behave differently
 - They will receive different payoffs
 - Equilibrium (convention/norm) cannot be “fair”

Chicken

- Coordination
 - Pre-play communication difficult
 - But: with joint coin tossing, expected payoff =1.
 - Conventions/social norms
 - Young let old pass first

If time permits

Stag Hunt

Stag Hunt

- **Situation:** Two hunters are to meet in the forest
 - Two possibilities
 - Bring equipment for hunting stag (= collaboration)
 - Bring equipment for hunting hare (= not)
 - If both choose stag
 - Both get 10 kilos of meat
 - If both choose hare
 - One gets 2 kilos
 - Other gets nothing
 - Equal probabilities
 - If one chooses stag and the other hare
 - One with stag equipment gets nothing
 - One with hare equipment gets 2 kilos

Coordination Game

- Represent situation as a game
 - Q: Players?
 - Players = (hunter 1, hunter 2)
 - Q: Strategy sets?
 - Strategy set = (stag, hare)
 - Q: Payoff functions (and outcomes)?
 - Payoff = expected kilos of meat

Stag Hunt

- Payoff matrix

	Stag	Hare
Stag	10, 10	0, 2
Hare	2, 0	1, 1

Stag Hunt

- Q: Equilibria?

	Stag	Hare
Stag	10, 10	0, 2
Hare	2, 0	1, 1

- A: (stag, stag) & (hare, hare)

	Stag	Hare
Stag	<u>10, 10</u>	0, 2
Hare	2, 0	<u>1, 1</u>

Stag Hunt

- Q: Which should we believe in?

	Stag	Hare
Stag	<u>10</u> , <u>10</u>	0, 2
Hare	2, 0	<u>1</u> , <u>1</u>

- Stag equilibrium - Pareto dominates
- Hare equilibrium - less risky

Stag Hunt

- Q: Would pre-play communication work?

	Stag	Hare
Stag	10, 10	0, 2
Hare	2, 0	1, 1

- Not clear
 - Both would prefer stag-equilibrium
 - Player 1 may promise to bring stag equipment
 - But he would say so also if he plans to go for hare

Football Penalty Game

Football Penalties

- Situation
 - Two players: Shooter and Goal keeper
 - Shooter decides which side to shoot
 - Goalie decides which side to defend
 - Q: Simultaneous choices?

Football Penalties

- Outcomes

	Defend Left	Defend Right
Shoot Left	No goal	Goal
Shoot Right	Goal	No goal

- Payoffs

	Defend Left	Defend Right
Shoot Left	-1, 1	1, -1
Shoot Right	1, -1	-1, 1

Football Penalties

- Q: Find equilibria!

	Defend Left	Defend Right
Shoot Left	-1, 1	1, -1
Shoot Right	1, -1	-1, 1

Football Penalties

- Best-reply analysis

	Defend Left	Defend Right
Shoot Left	-1, <u>1</u>	<u>1</u> , -1
Shoot Right	<u>1</u> , -1	-1, <u>1</u>

- Conclusion
 - No equilibrium exists

Football Penalties

- Interpretation
 - Extreme competition: One player's gain is the other player's loss
 - Zero-sum game
 - Players don't want to be predictable

Football Penalties

- What happens if goalie tosses a coin?
 - If shooter goes left \Rightarrow probability of goal = 50%
 - If shooter goes right \Rightarrow probability of goal = 50%
 - I.e. Probability of goal = 50%,
independent of which side the shooter goes
 - Expected utility to both = 0,
independent of which side the shooter goes

Football Penalties

- New game:

	Defend Left	Toss Coin	Defend Right
Shoot Left	-1, 1	0, 0	1, -1
Shoot Right	1, -1	0, 0	-1, 1

Football Penalties

- What happens if shooter tosses a coin?
 - Probability of goal = 50%,
independent of which side the goalie goes
 - Expected utility to both = 0,
independent of which side the goalie goes

Football Penalties

- New game

	Defend Left	Toss Coin	Defend Right
Shoot Left	-1, 1	0, 0	1, -1
Toss Coin	0, 0	0, 0	0, 0
Shoot Right	1, -1	0, 0	-1, 1

Football Penalties

- Best-reply analysis

	Defend Left	Toss Coin	Defend Right
Shoot Left	-1, <u>1</u>	<u>0</u> , 0	<u>1</u> , -1
Toss Coin	0, <u>0</u>	<u>0</u> , <u>0</u>	0, <u>0</u>
Shoot Right	<u>1</u> , -1	<u>0</u> , 0	-1, <u>1</u>

- Conclusion
 - Both tossing coin is equilibrium

Football Penalties

- Allowing players to toss coin restores equilibrium!
 - This is true in general...
 - ...but we need to allow players to choose probabilities of different alternatives freely

Interpretation

- But, do people “toss coins”?
 - Not literally...
 - ...but in football penalty games the players sometimes go left and sometimes right
 - they try to be unpredictable
 - they behave *as if* they toss coins

Mixed Strategies and Existence of Equilibrium

Not included this year !

Existence of Equilibrium

- If game has
 - Finitely many players
 - Each player has finitely many strategies
- Then, game has at least one Nash equilibrium
 - Possibly in mixed strategies

Existence of Equilibrium

- Example

- 2 players
- Player 1 has two pure strategies: Up
- Player 2 has two pure strategies: Left
- Player 1's Payoffs: $B > A, C > D,$
- Player 2's Payoffs: $a > c, d > b$

Exercise:

Find the Nash equilibria

	Left	Right
Up	A, a	C, c
Down	B, b	D, d

Existence of Equilibrium

- Example

- 2 players
- Player 1 has two pure strategies: Up
- Player 2 has two pure strategies: Left
- Player 1's Payoffs: $B > A, C > D,$
- Player 2's Payoffs: $a > c, d > b$

Solution:

No Nash equilibria

	Left	Right
Up	A, <u>a</u>	<u>C</u> , c
Down	<u>B</u> , b	D, <u>d</u>

Existence of Equilibrium

- Game in mixed strategies
 - Let us now define a *new game*, which acknowledges that *people may randomize* their choices if they want to.
- Q: New game
 - Players: Same as before
 - Strategies: All possible probability distributions over “pure strategies”
 - Payoffs: Expected payoff

Existence of Equilibrium

- Mixed strategies
 - Player 2 selects Left with probability p (where $0 \leq p \leq 1$)
 - Player 1 selects Up with probability q (where $0 \leq q \leq 1$)

Existence of Equilibrium

- Expected utility

$p \cdot q = \text{Prob (Up \& Left)}$

$$U_1(q, p) = A \cdot p \cdot q + B \cdot p \cdot (1 - q) + C \cdot (1 - p) \cdot q + D \cdot (1 - p) \cdot (1 - q)$$

Where

$$p = \text{Prob}\{\text{Left}\}$$

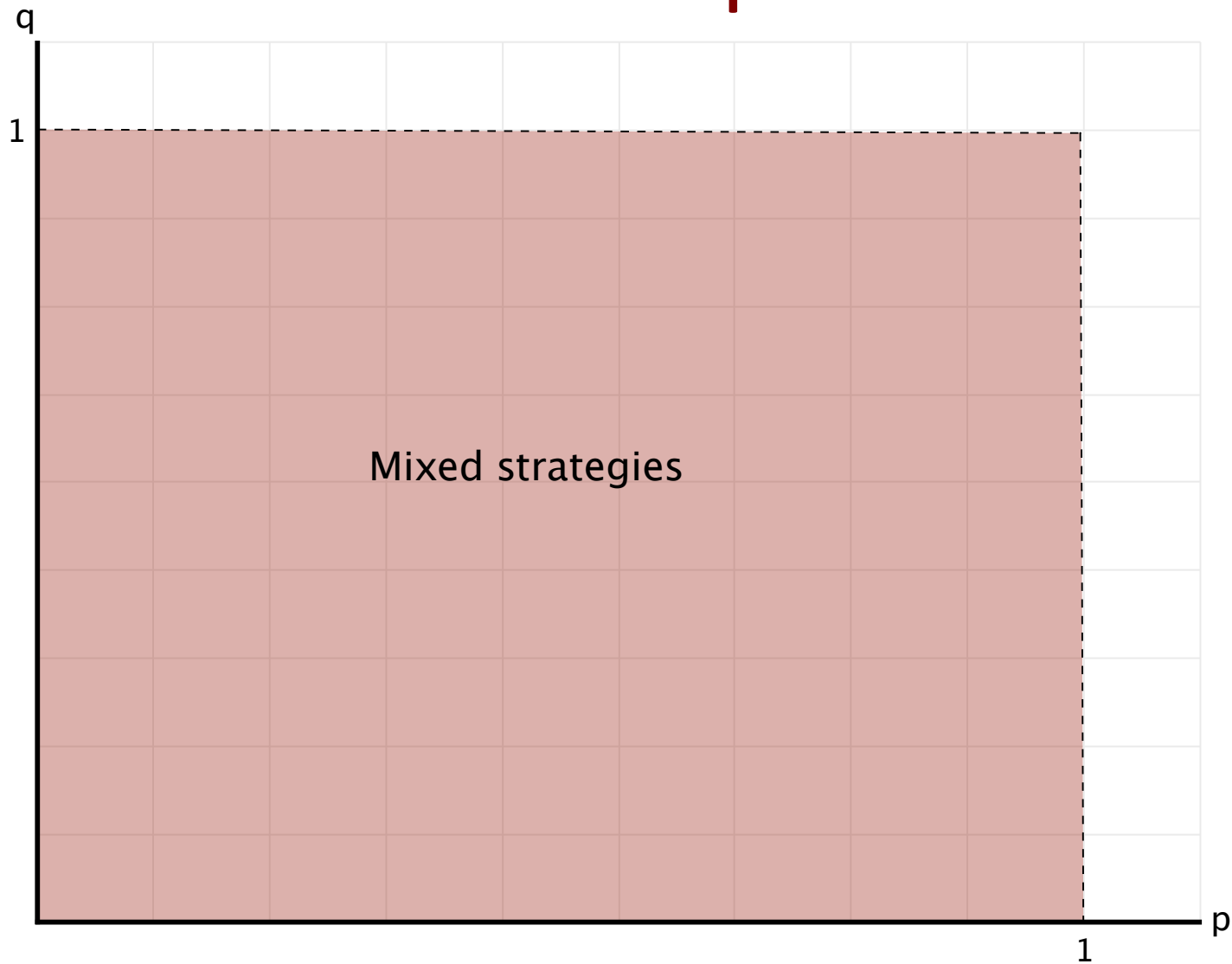
$$q = \text{Prob}\{\text{Up}\}$$

	Left	Right
Up	A, a	C, c
Down	B, b	D, d

Existence of Equilibrium

- Game in mixed strategies
 - Players: 1 and 2
 - Strategies: p in $[0, 1]$ and q in $[0, 1]$
 - Payoffs: $U_1(p,q)$; $U_2(p,q)$

Existence of Equilibrium



Existence of Equilibrium

- Q: How do we make predictions?
 - Find Nash equilibria in the new game
- Q: What procedure do we use?
 - Derive best-reply functions

Existence of Equilibrium

- Notice: “the pure strategies are still there”
 - Player 2 going Right corresponds to $p = 0$
 - Player 2 going Left corresponds to $p = 1$
 - Player 1 going Down corresponds to $q = 0$
 - Player 1 going Up corresponds to $q = 1$

Existence of Equilibrium

- A useful “trick”
 - It turns out to be convenient to start out studying when the “pure strategies” are better than one another

Existence of Equilibrium

- Expected utility of pure strategies

$$U_1(p,1) = A \cdot p + C \cdot (1 - p)$$

$$q = 1 \Leftrightarrow \text{"Up"}$$

$$U_1(p,0) = B \cdot p + D \cdot (1 - p)$$

$$q = 0 \Leftrightarrow \text{"Down"}$$

$$p = \text{Prob}\{\text{Left}\}$$

	Left	Right
Up	A, a	C, c
Down	B, b	D, d

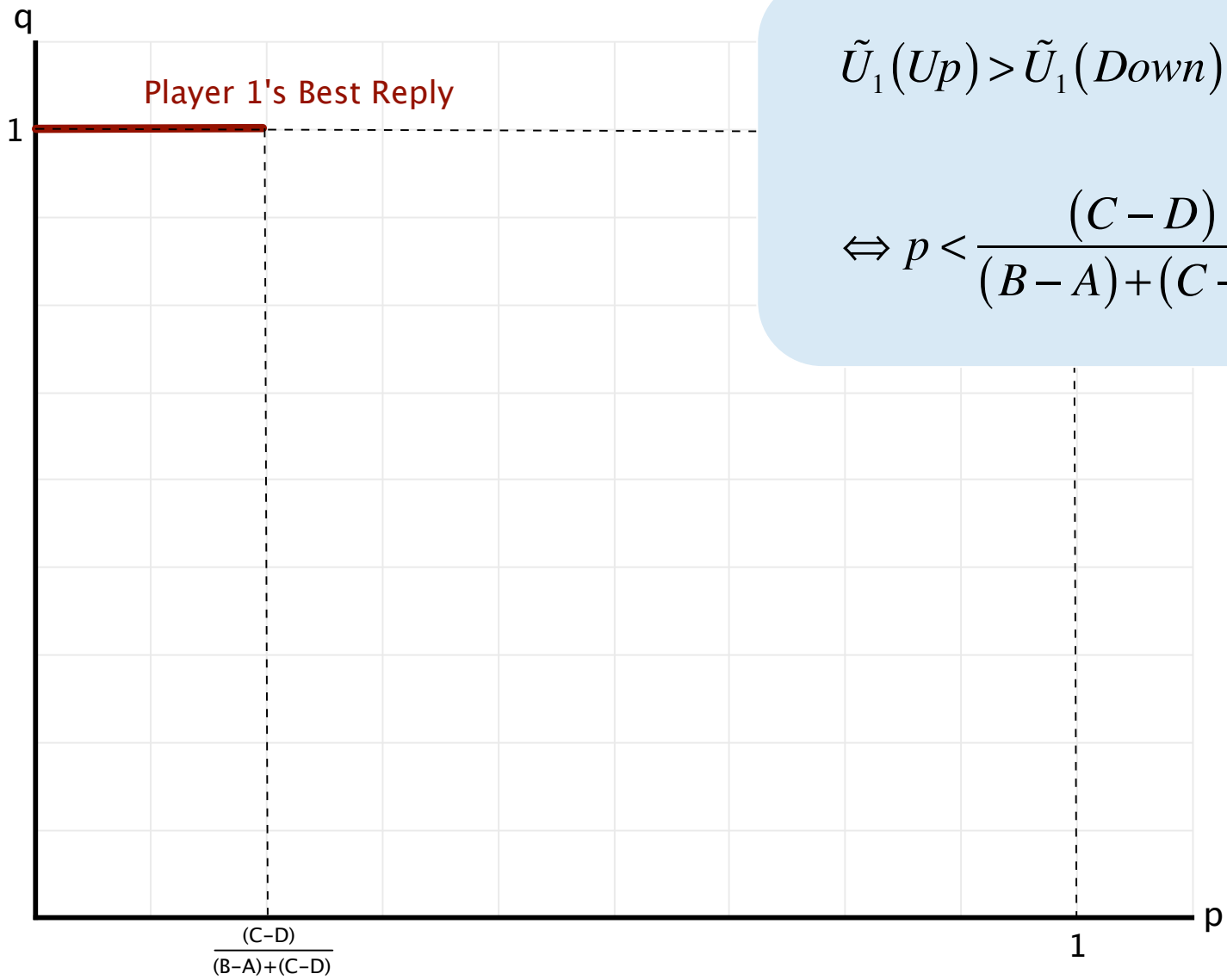
Existence of Equilibrium

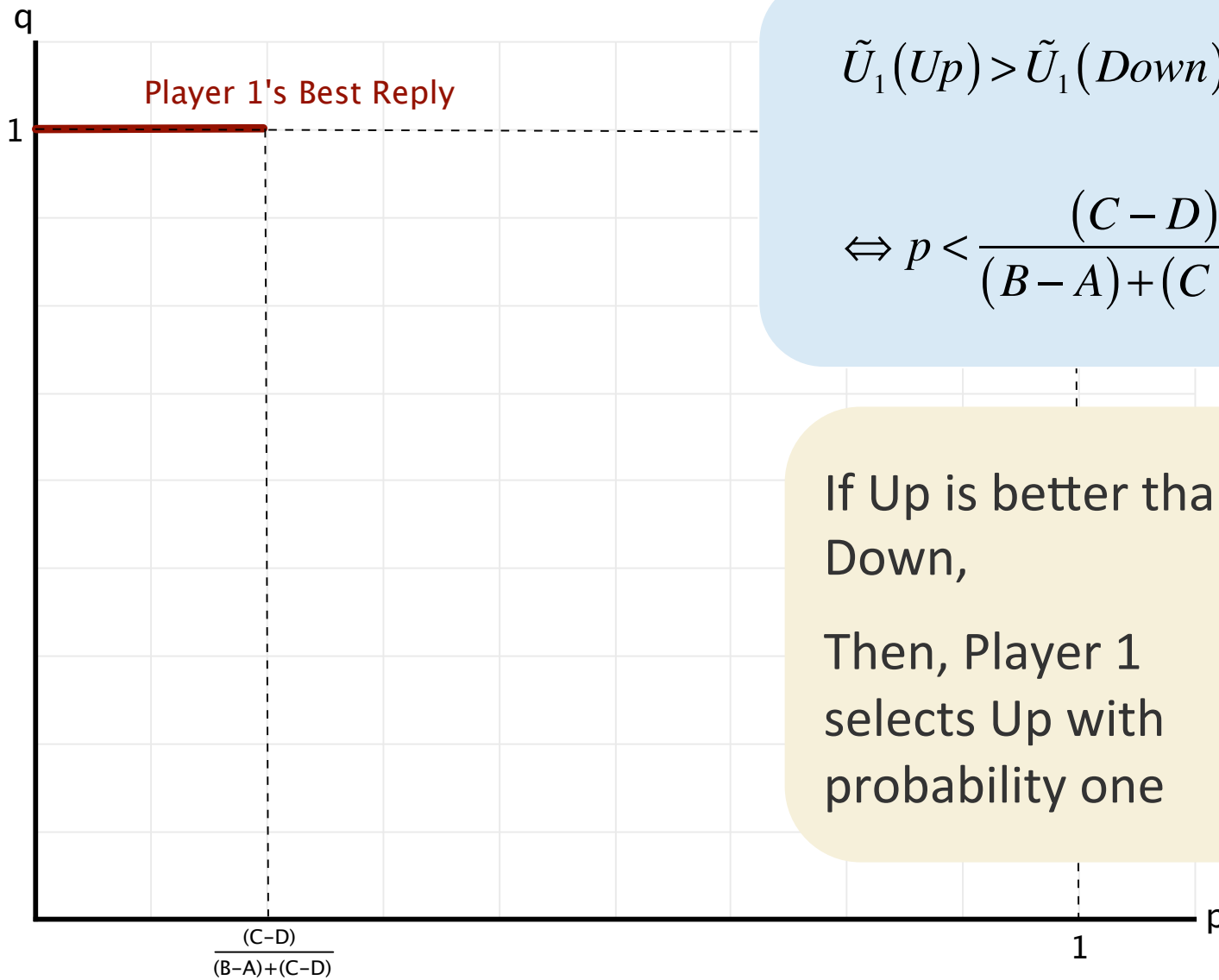
- Player 1 prefers Up (ie $q=1$) if

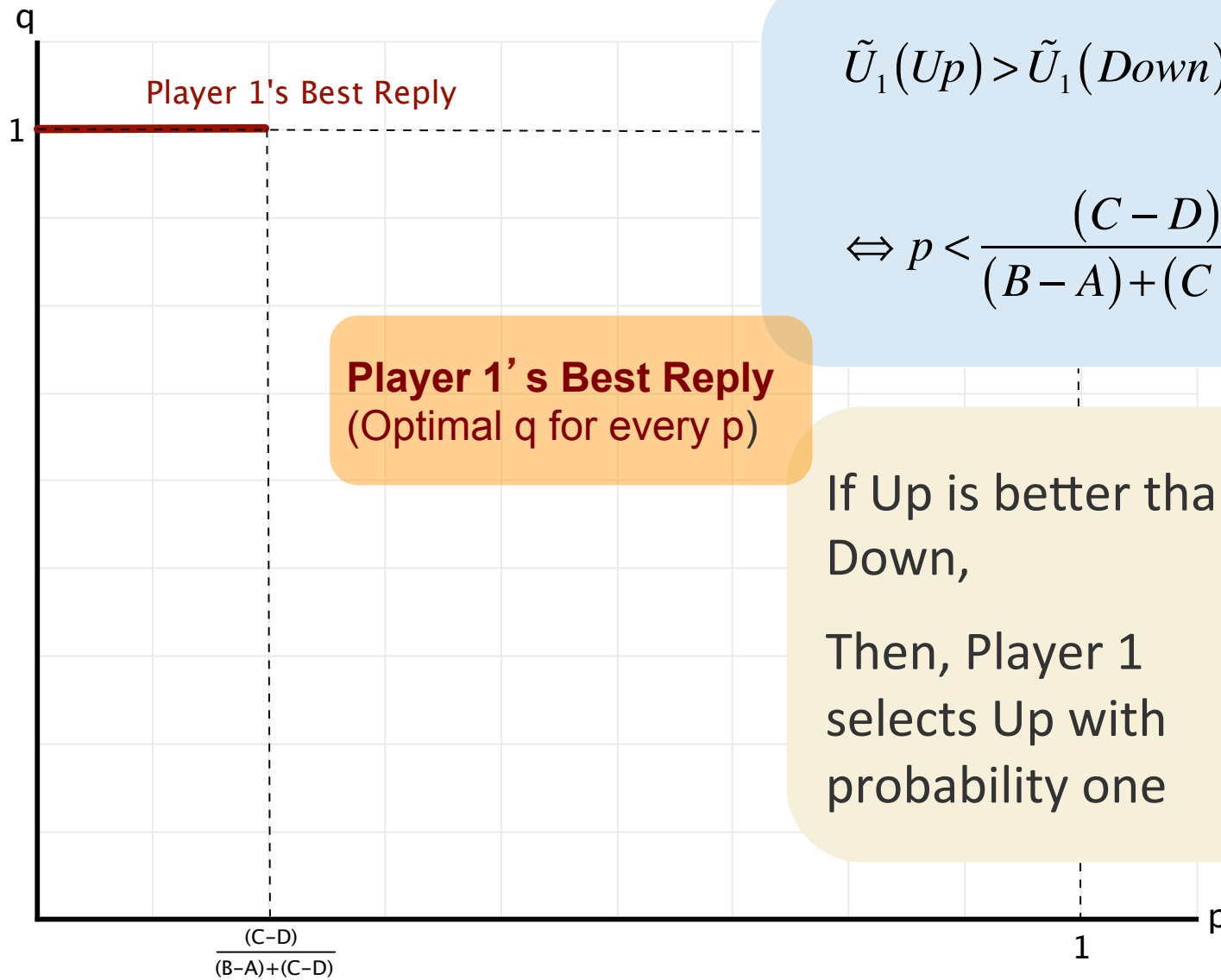
$$\tilde{U}_1(Up) > \tilde{U}_1(Down)$$

$$\Leftrightarrow A \cdot p + C \cdot (1 - p) > B \cdot p + D \cdot (1 - p)$$

$$\Leftrightarrow p < \frac{(C - D)}{(B - A) + (C - D)}$$







Existence of Equilibrium

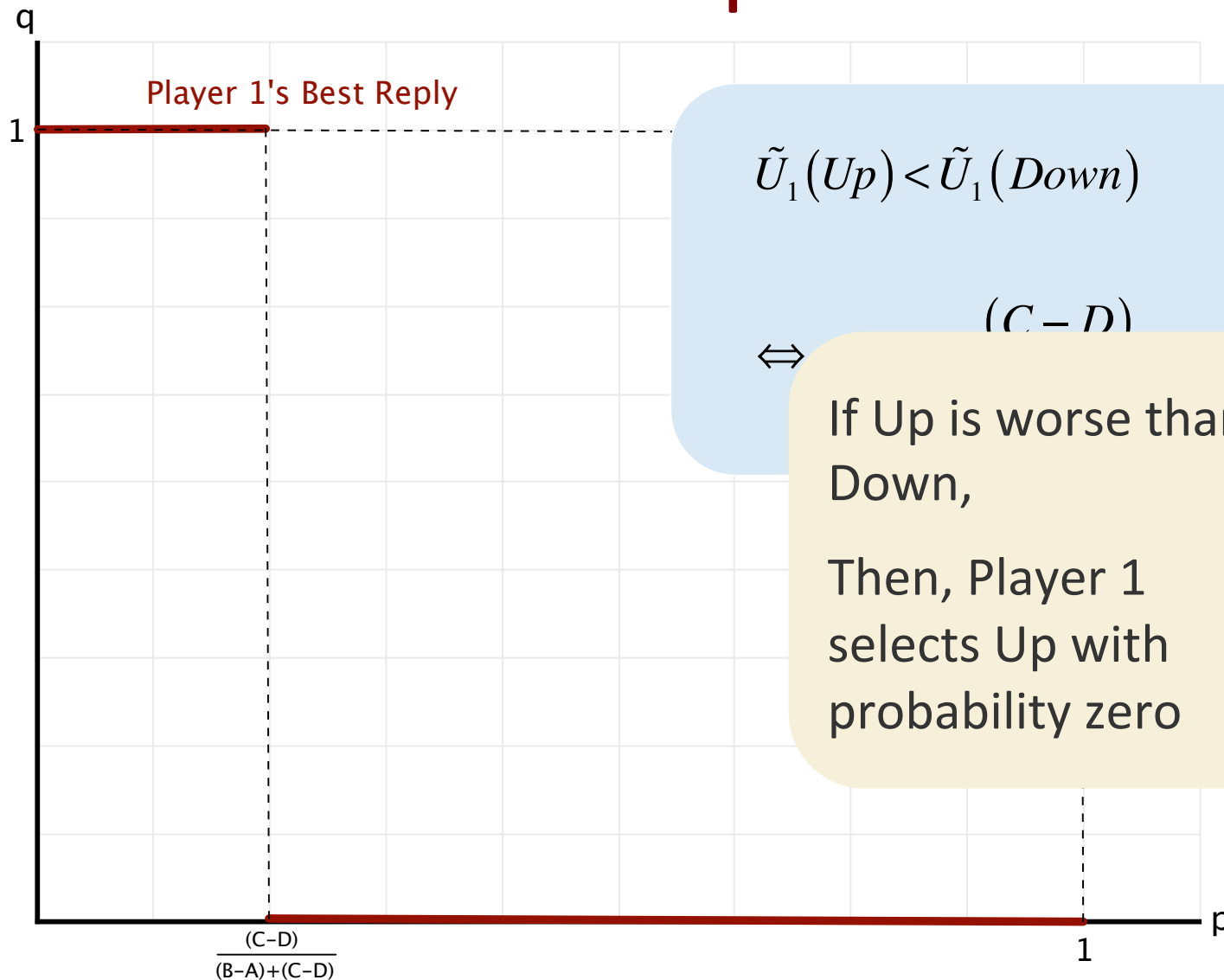
- Player 1 prefers Down (ie $q=0$) if

$$\tilde{U}_1(Up) < \tilde{U}_1(Down)$$

$$\Leftrightarrow A \cdot p + C \cdot (1 - p) < B \cdot p + D \cdot (1 - p)$$

$$\Leftrightarrow p > \frac{(C - D)}{(B - A) + (C - D)}$$

Existence of Equilibrium



Existence of Equilibrium

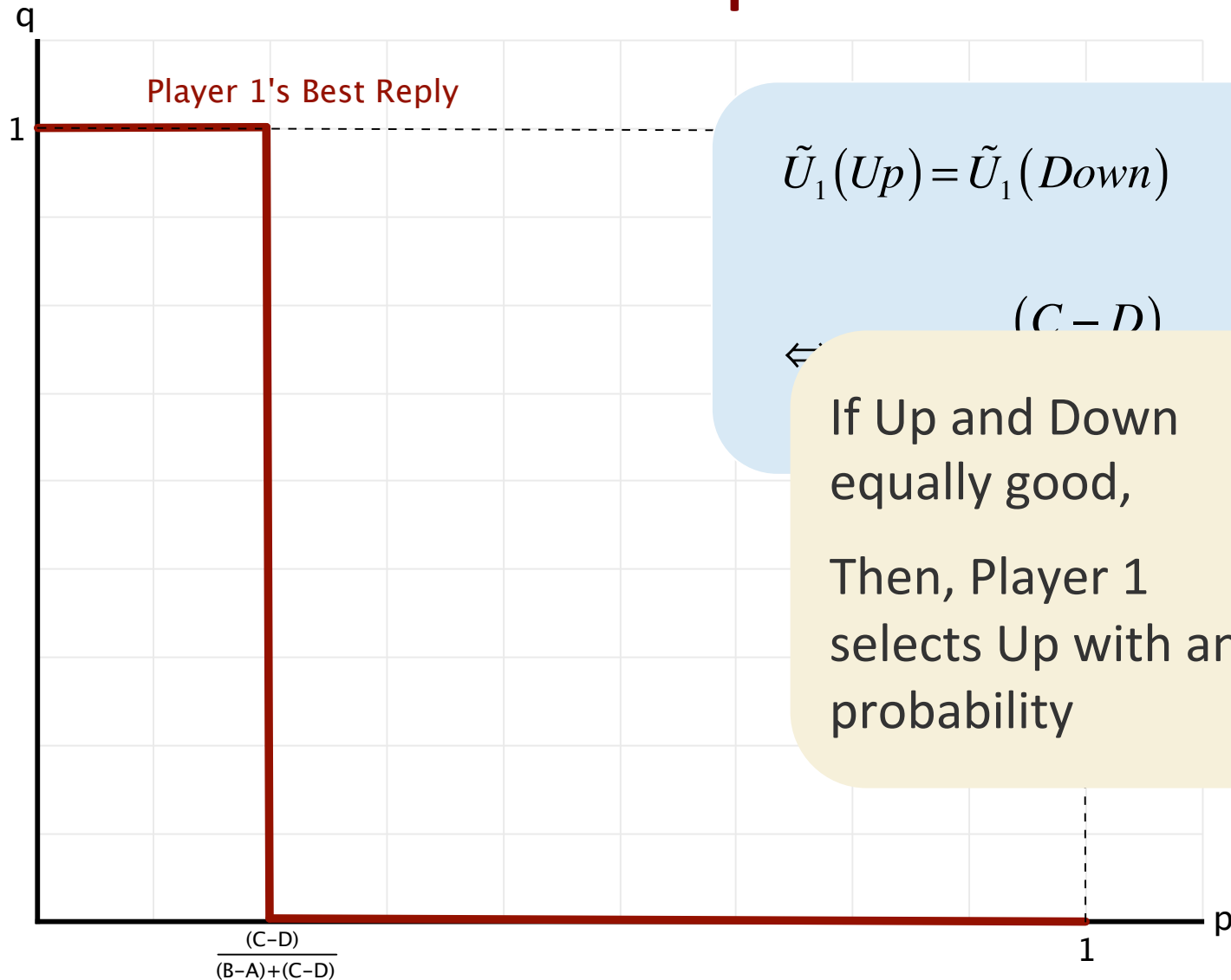
- Player 1 indifferent if

$$\tilde{U}_1(Up) = \tilde{U}_1(Down)$$

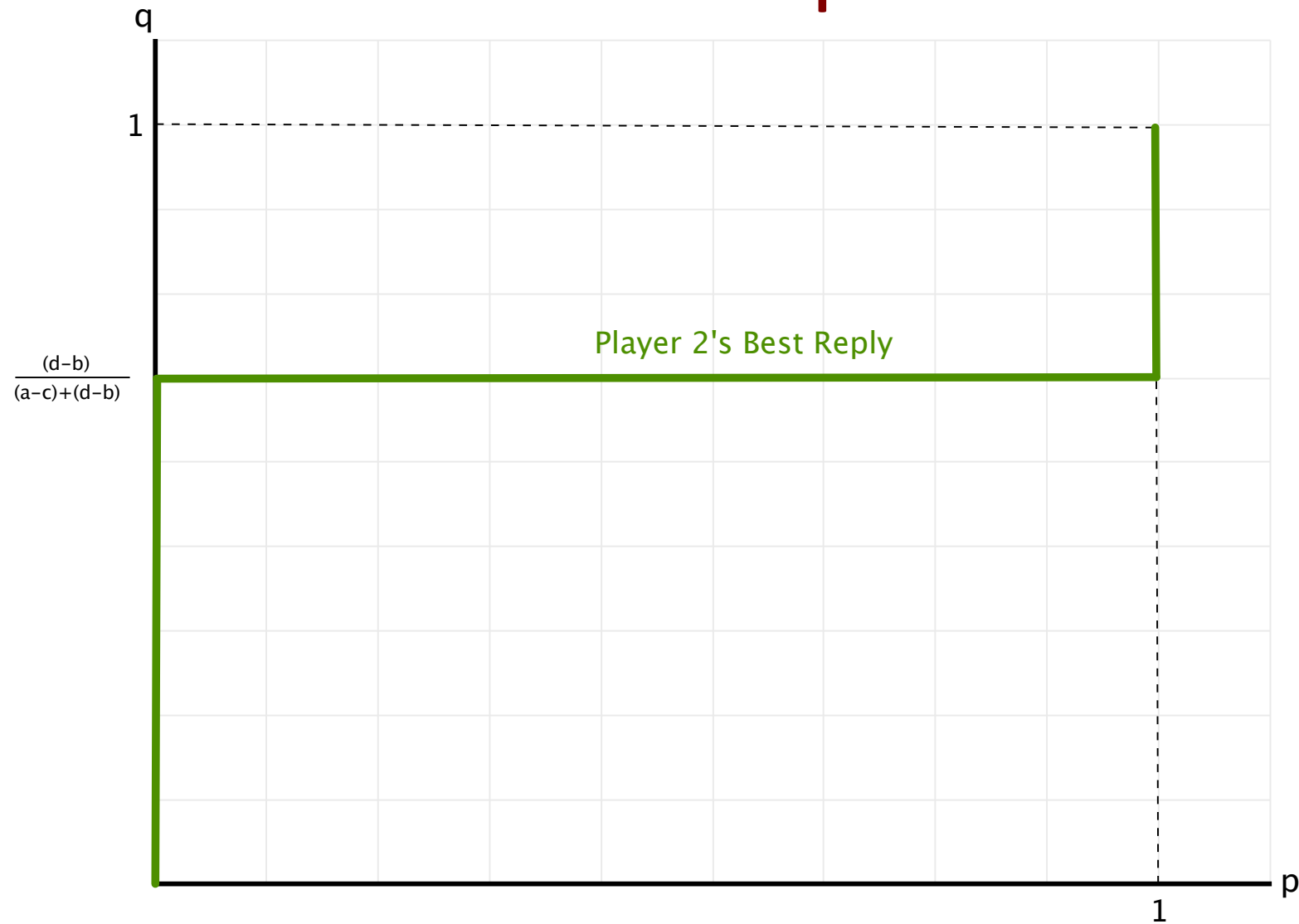
$$\Leftrightarrow A \cdot p + C \cdot (1 - p) = B \cdot p + D \cdot (1 - p)$$

$$\Leftrightarrow p = \frac{(C - D)}{(B - A) + (C - D)}$$

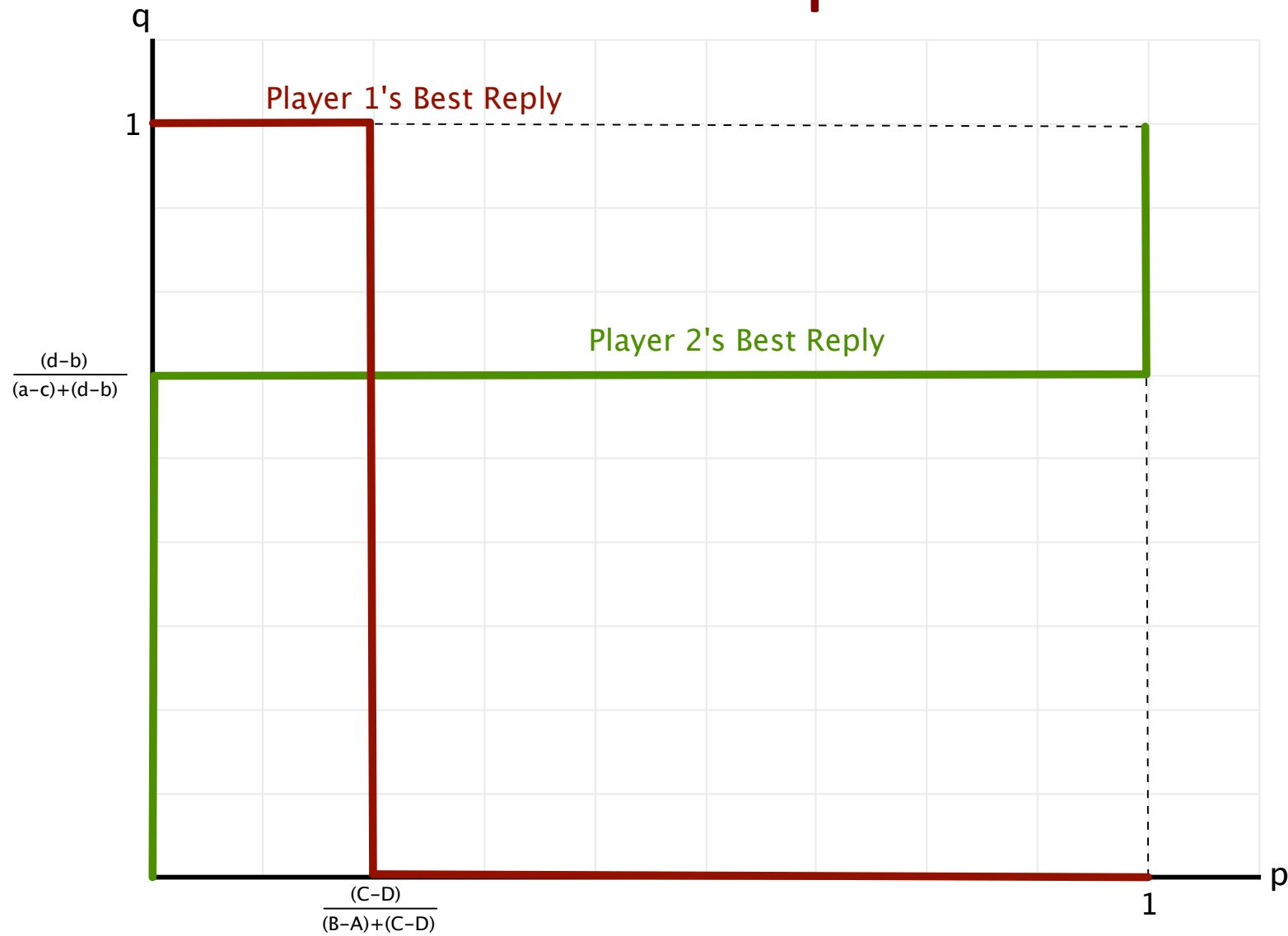
Existence of Equilibrium



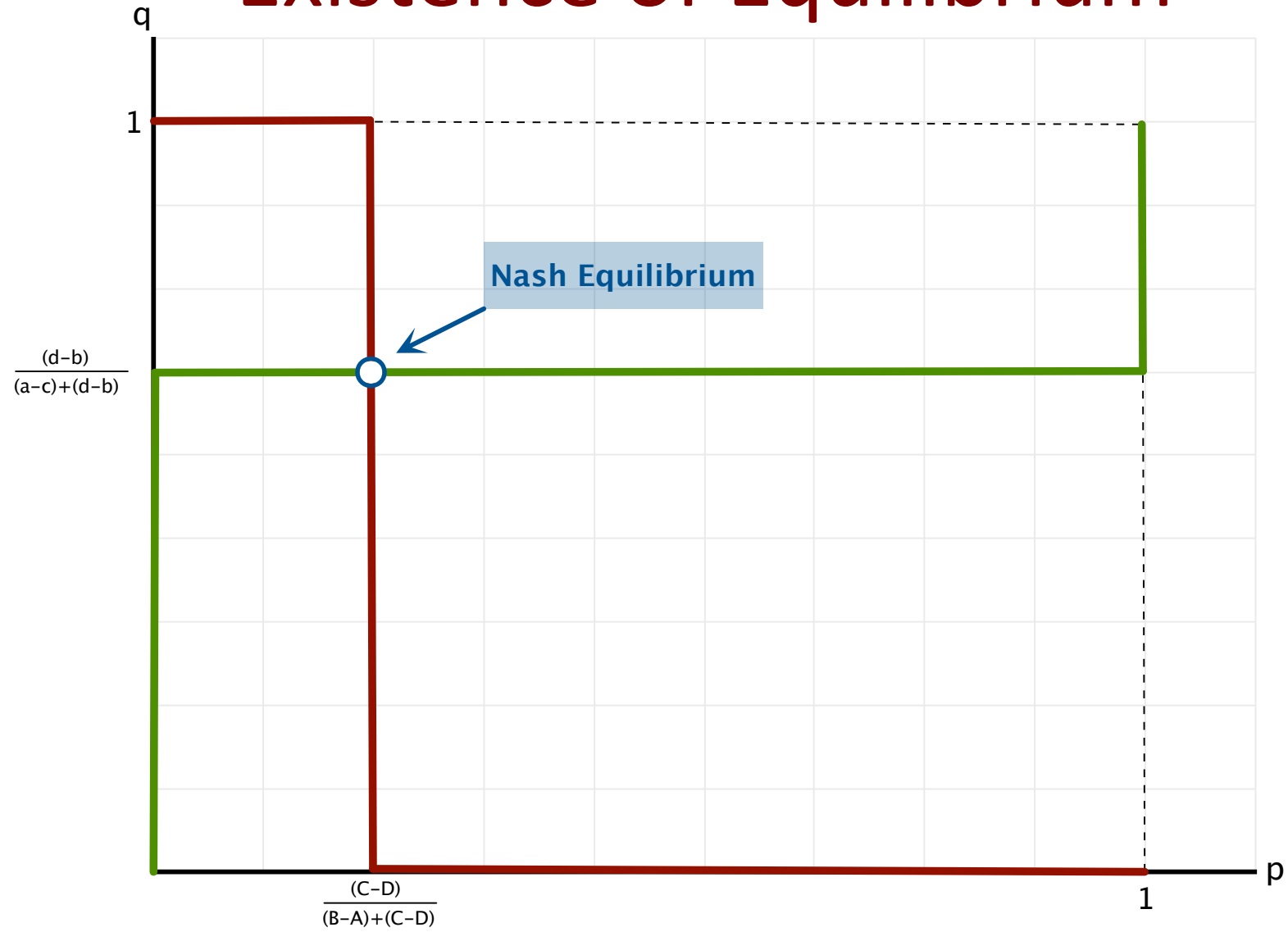
Existence of Equilibrium



Existence of Equilibrium



Existence of Equilibrium



Exercise

Exercise

- Battle of the sexes
 - Two spouses want to go out, either to see a football game or a theater play
 - The man enjoys football (but not theater)
 - The woman enjoys theater (but not football)
 - They both enjoy each other's company

Existence of Equilibrium

- Payoff matrix

- Man is player one
- v = value of preferred alternative (0 is value of other)
- t = value of being together
- Assume $t > v$.

	Football	Theater
Football	$v+t, t$	v, v
Theater	$0, 0$	$t, v+t$

Existence of Equilibrium

- To do
 - Define the game in mixed strategies
 - Find the man's best-reply function. Display in diagram
 - Same for woman
 - Find equilibria
 - Which is more plausible?

	Football	Theater
Football	$v+t, t$	v, v
Theater	$0, 0$	$t, v+t$